

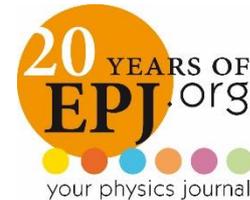
**Congresso Nazionale della Società Italiana di Fisica
Università della Calabria 17/21 Settembre 2018**

SYNTHETIC GAUGE FIELDS IN ULTRACOLD ATOMIC GASES



Università di Trento

Sandro Stringari



- **Bose-Einstein condensation in atomic gases has been a long sought goal for decades before 1995.**

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- **At low temperature all the systems existing in nature (with the exception of liquid Helium) undergo a transition to the **crystal phase**.**

- **Atomic gases are available in conditions of metastability and quantum degeneracy only if their density is extremely small to avoid crystallization. This sets **challenging conditions for density** ($10^{13} - 10^{15} \text{ cm}^{-3}$) and **temperaure** ($10^{-6} - 10^{-8} \text{ K}$)**

- **Bose-Einstein condensation in atomic gases has been a long sought goal for decades before 1995.**

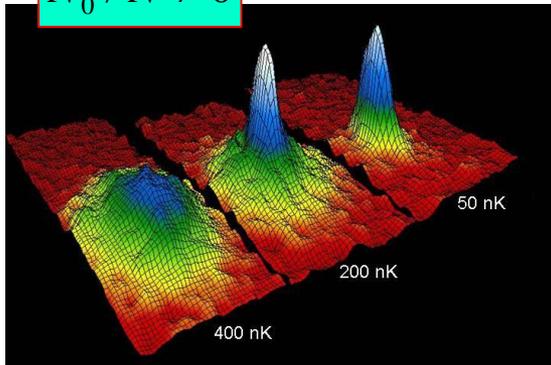
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- **After the first realization of Bose-Einstein condensation in alkali atoms in 1995 the experimental and theoretical activities in the field of **ultracold atomic gases have grown in an impressive way**, giving rise to a well established new field of research of fundamental interest for the investigation of **quantum phenomena****

-Some major achievements of ultra-cold atomic physics

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$$N_0 / N \neq 0$$

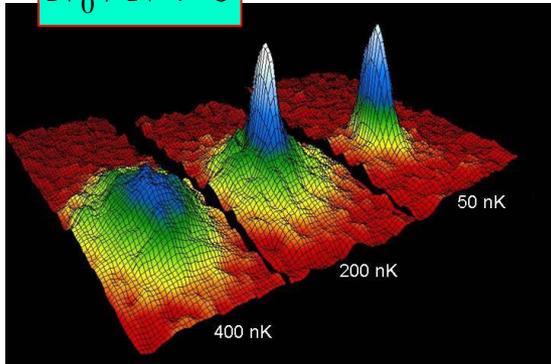


1995
(Jila+MIT)

Macroscopic
occupation
of sp state (Bose-
Einstein condensation)

-Some major achievements of ultra-cold atomic physics

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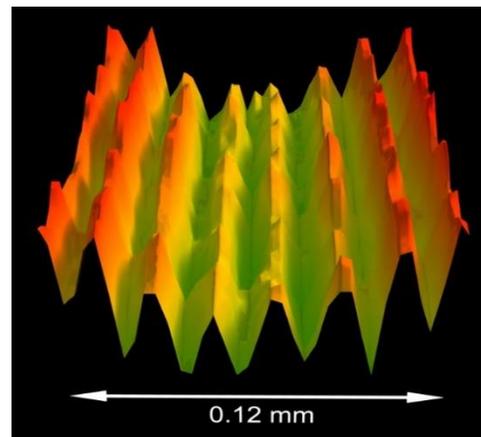


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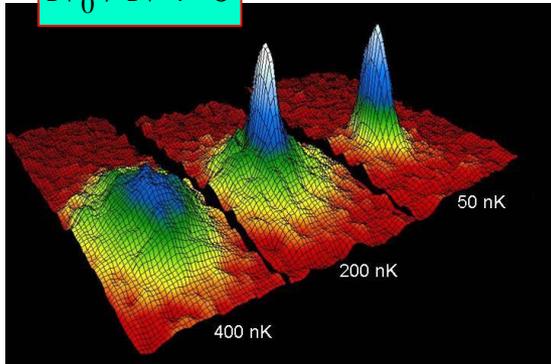
1996
(MIT)

Interference
and quantum
coherence



-Some major achievements of ultra-cold atomic physics

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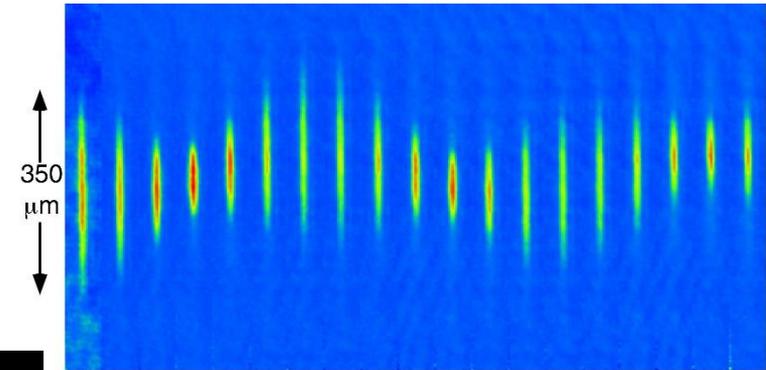
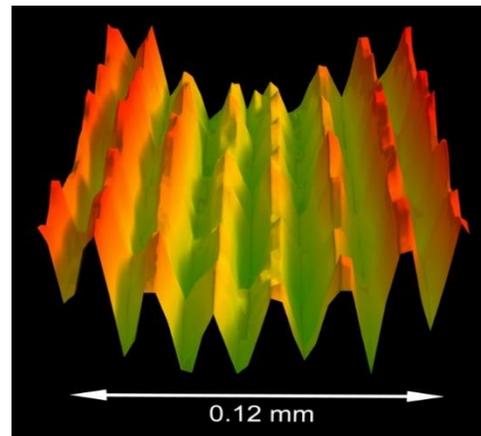


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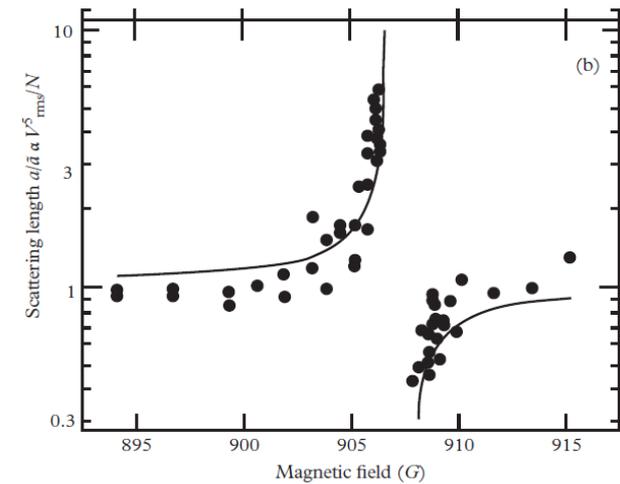
Interference
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coherence



5 milliseconds per frame

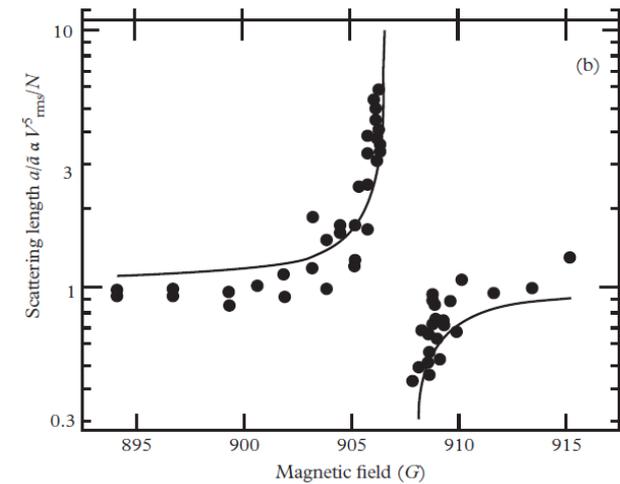
1996
(MIT)

Collective
oscillations

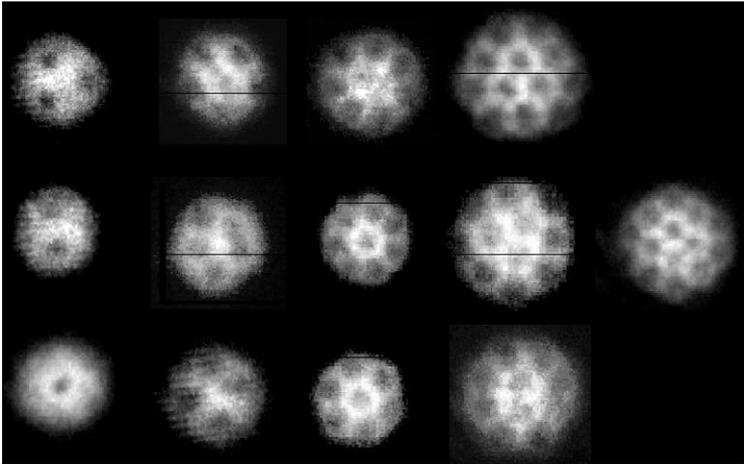


1999
(MIT)

Feshbach
resonances
and tuning
of scattering
length

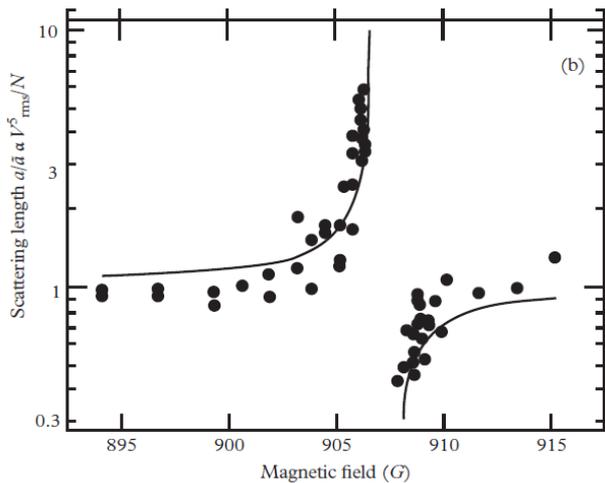


2000
(ENS
Quantized
vortices in BEC

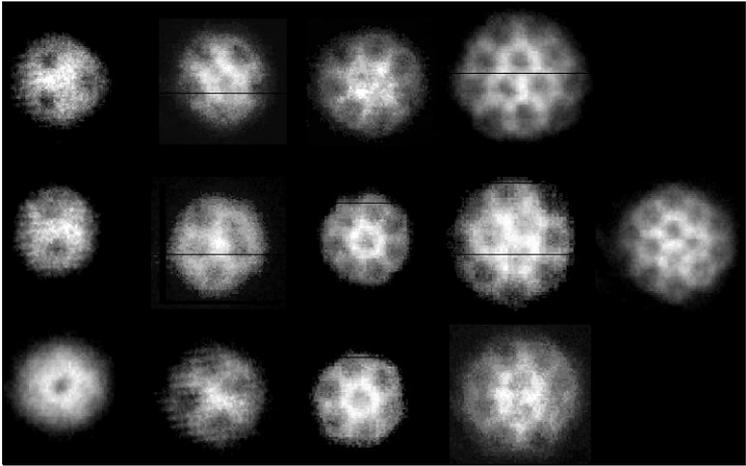


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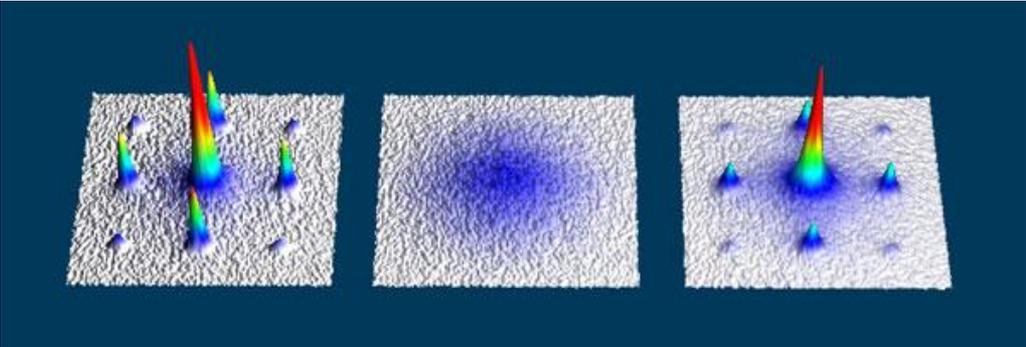
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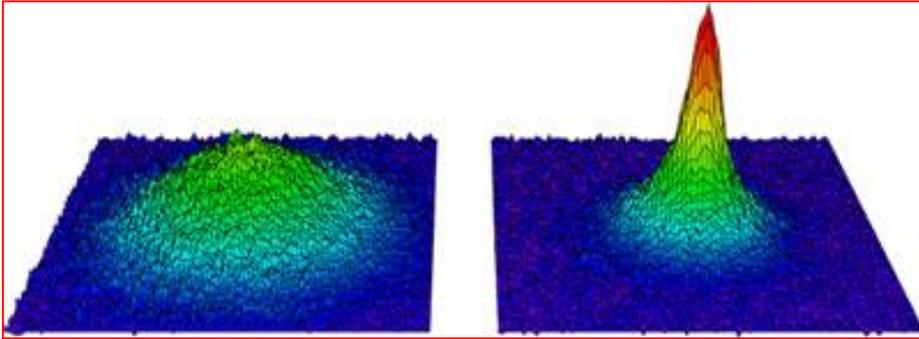
1999
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 Feshbach
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2001
 (MPI Munich)
 Superfluid-insulator
 transition

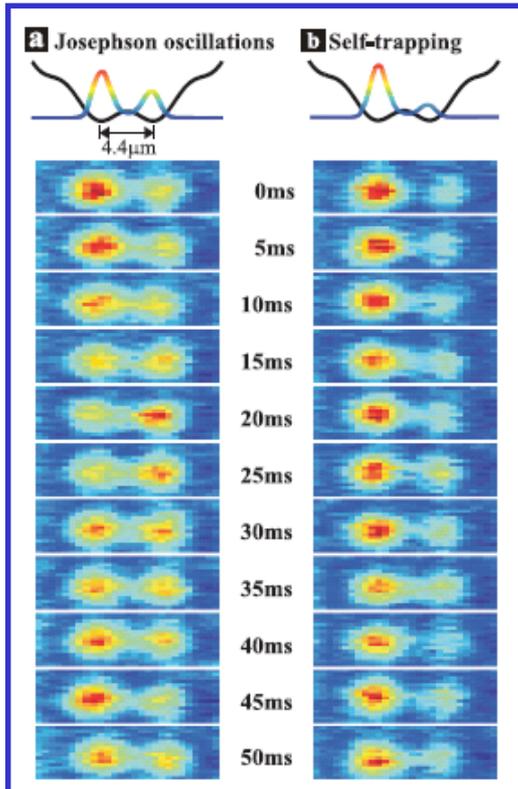
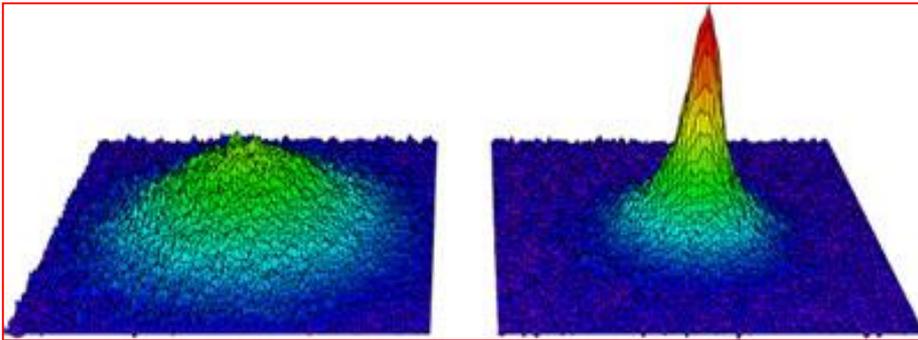
2003
(JILA-ENS-
Innsbruck)

BEC of molecules
emerging from Fermi sea



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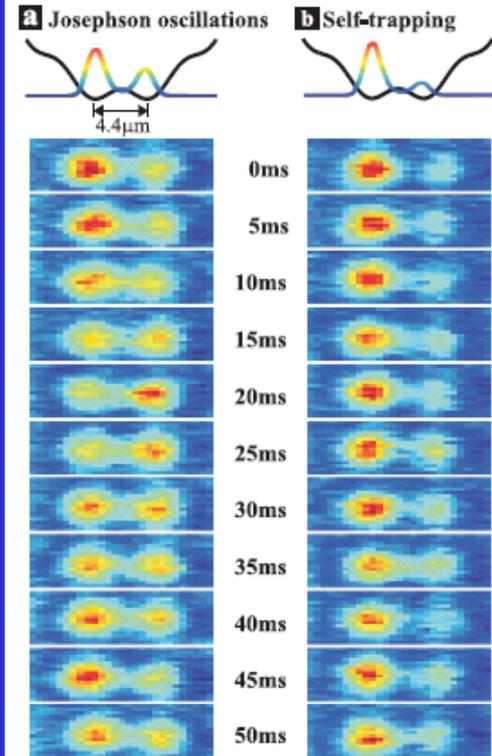
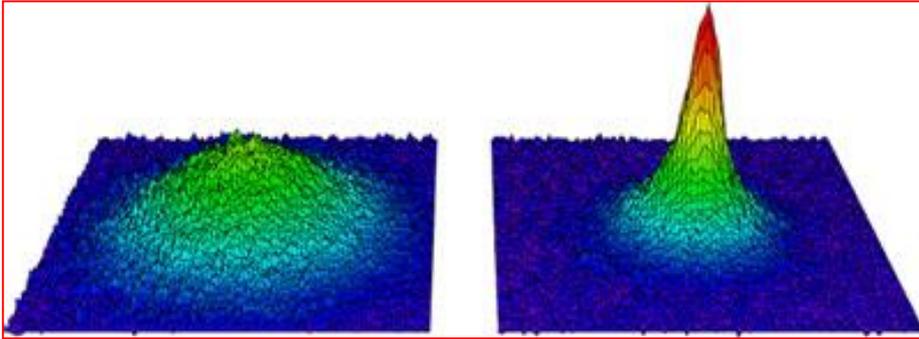


2004
(Heidelberg)

Josephson
oscillation

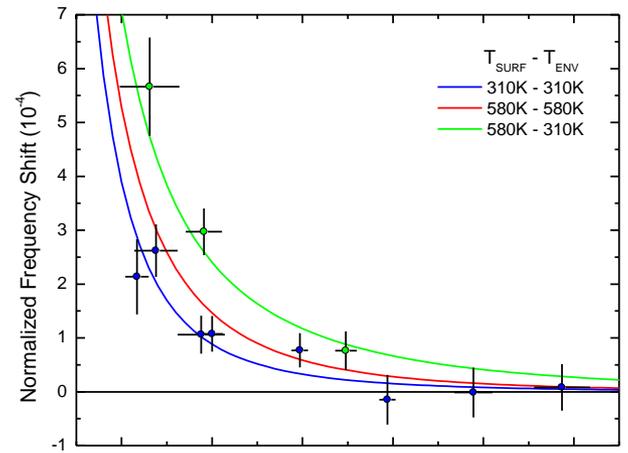
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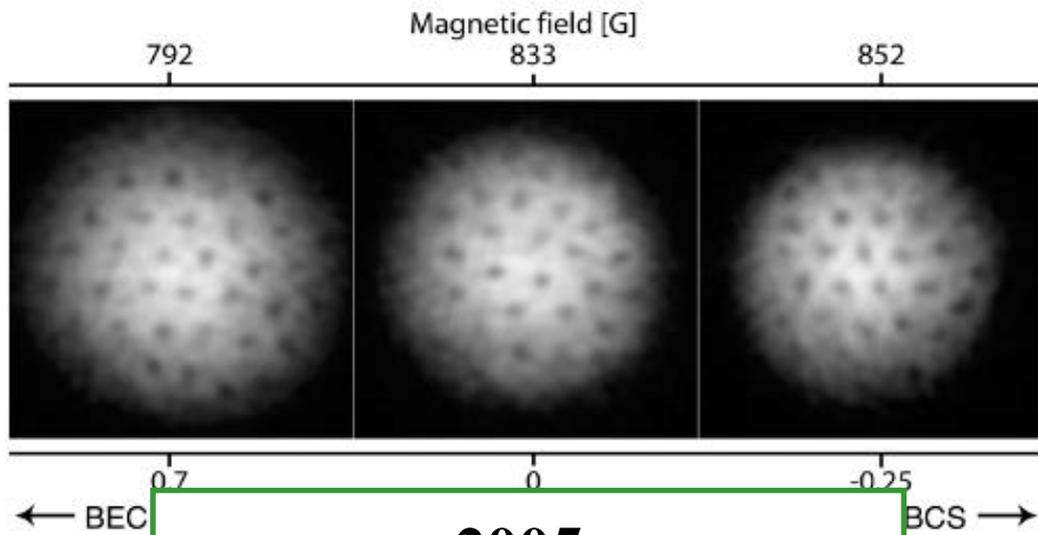
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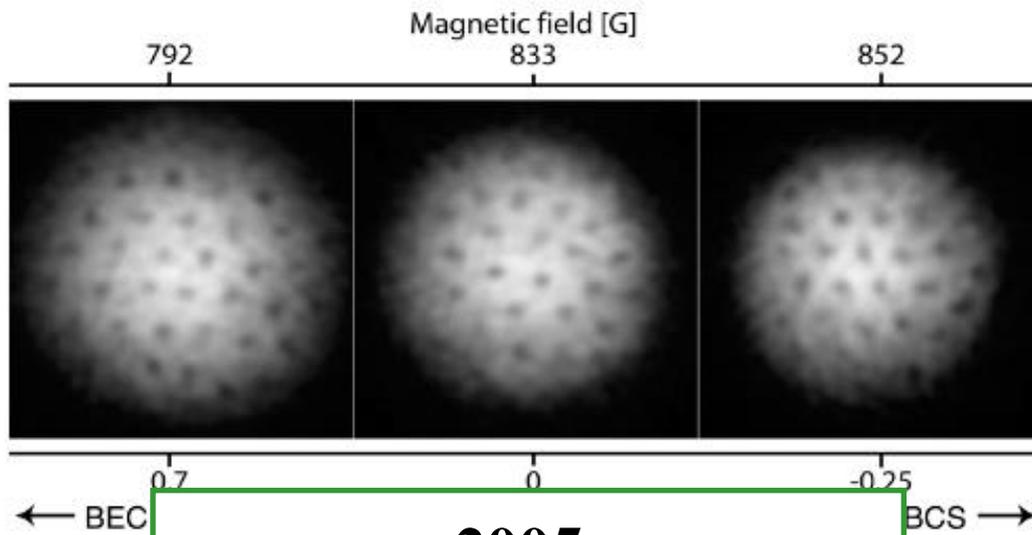
2004
(JILA)

Temperature dependence
of Casimir-Polder force



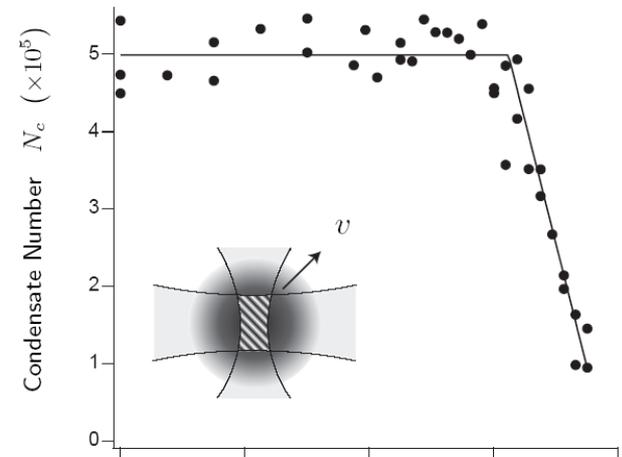
2005
(MIT)

Vortices in a Fermi superfluid



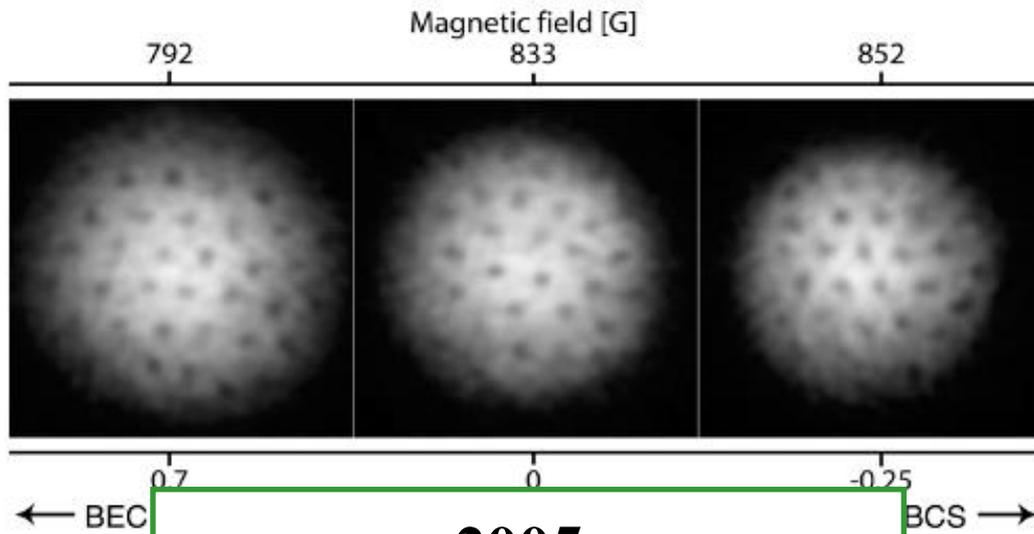
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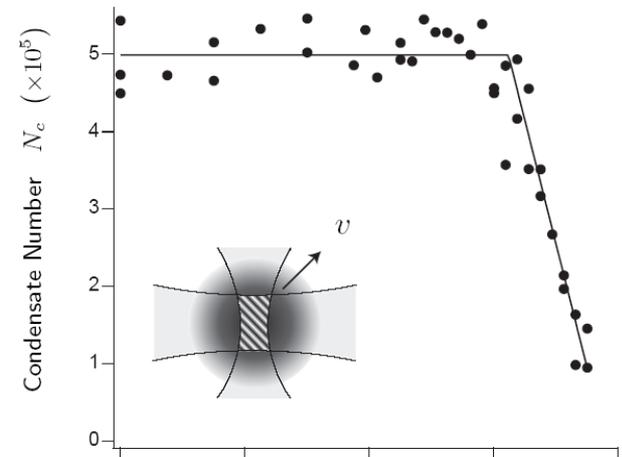
2007
(MIT)

Absence of viscosity
in the unitary Fermi
superfluid



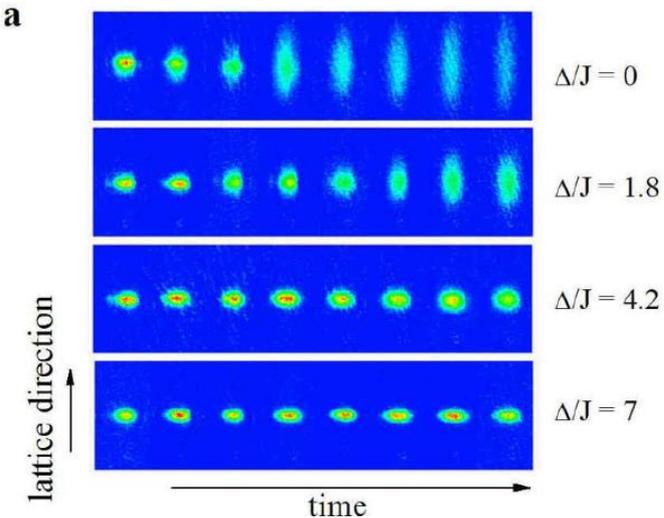
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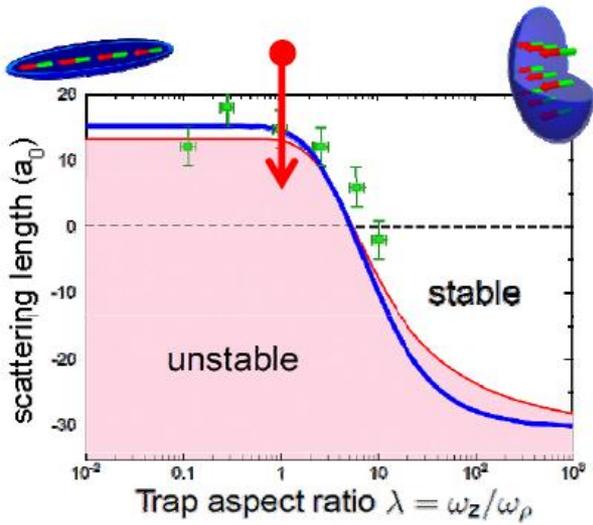
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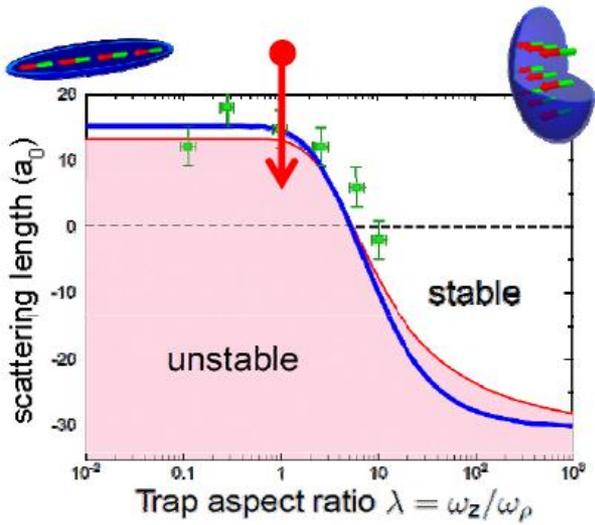
2008
(Florence-
Palaiseau)

Anderson localization

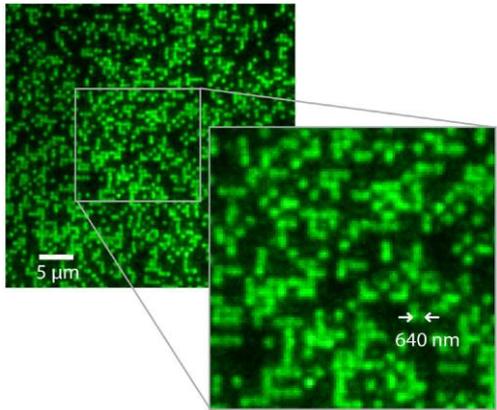


2008
(Stuttgart)

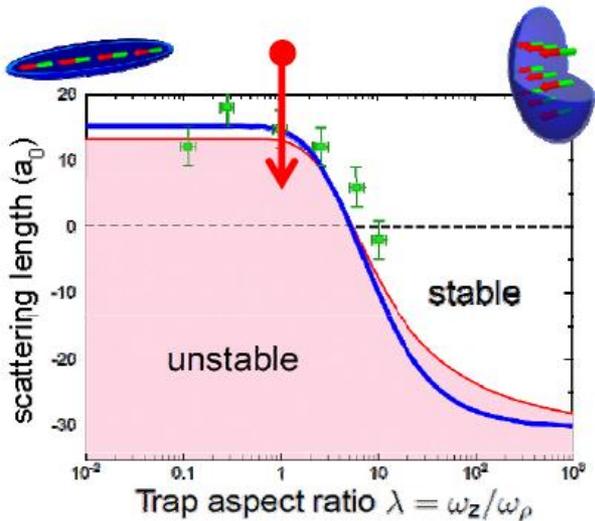
Dipolar gases
(anisotropy and
long range)



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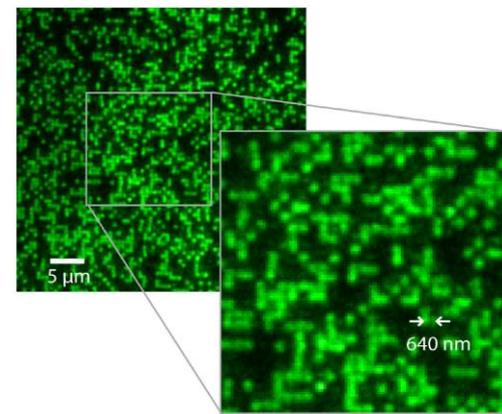


2009
 (Harvard)
 Quantum gas
 microscope



2008
(Stuttgart)

Dipolar gases
(anisotropy and long range)

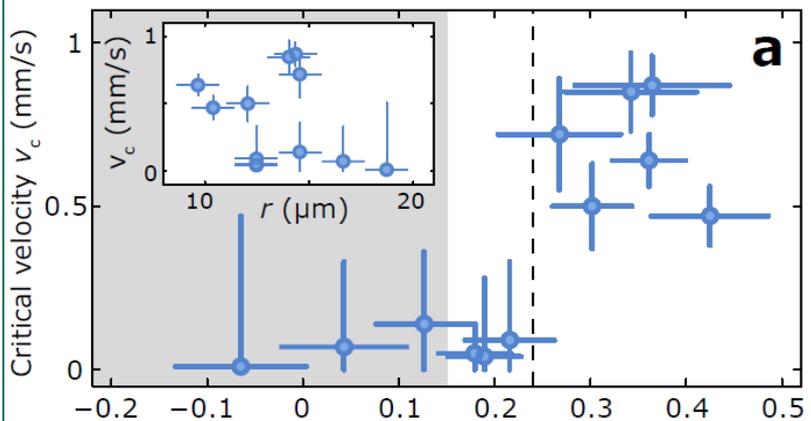


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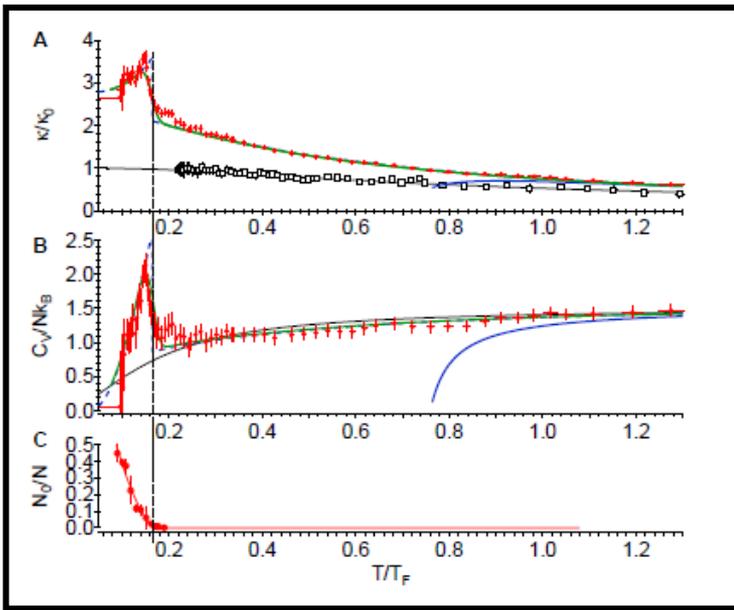
2012
(ENS)

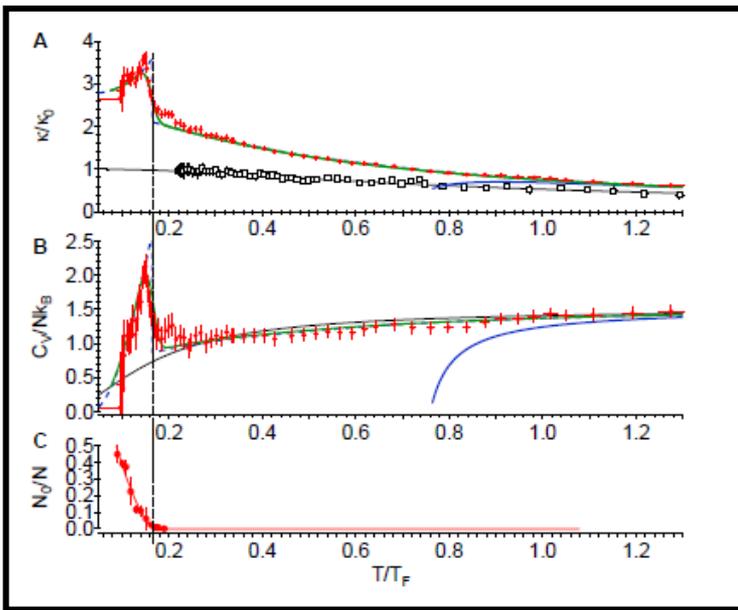
BKT transition in 2D Bose gas



2012
(MIT)

Lambda
transition in
superfluid
Fermi gas





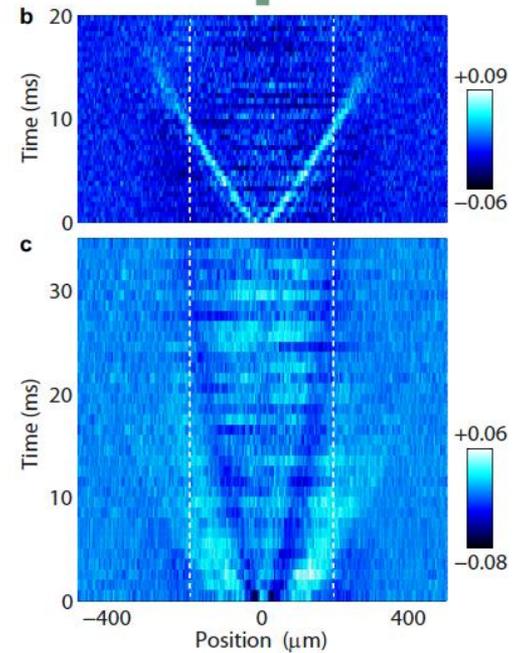
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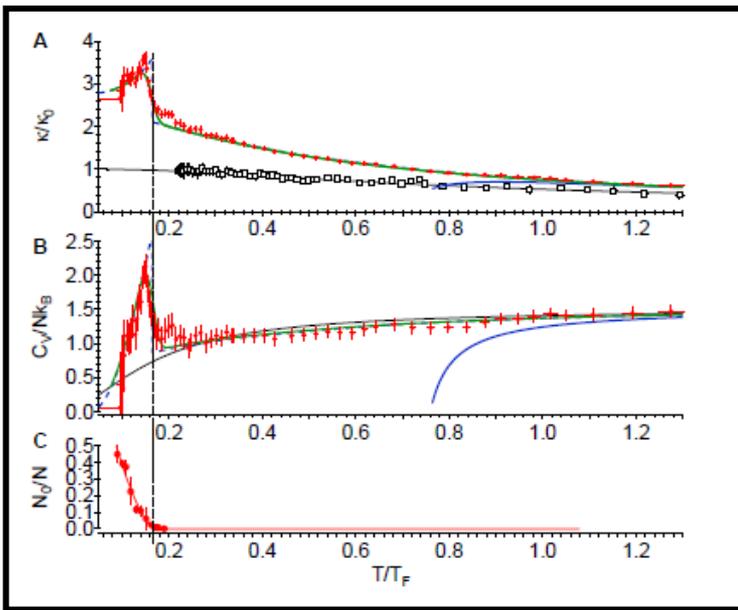
Lambda
transition in
superfluid
Fermi gas

2013

(Innsbruck)

Propagation of
second sound in
a Fermi superfluid





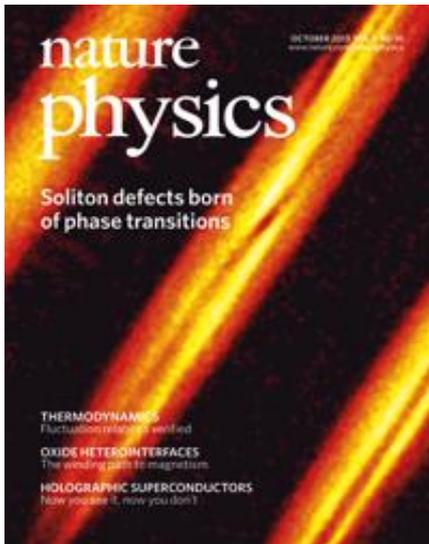
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(MIT)

Lambda
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superfluid
Fermi gas

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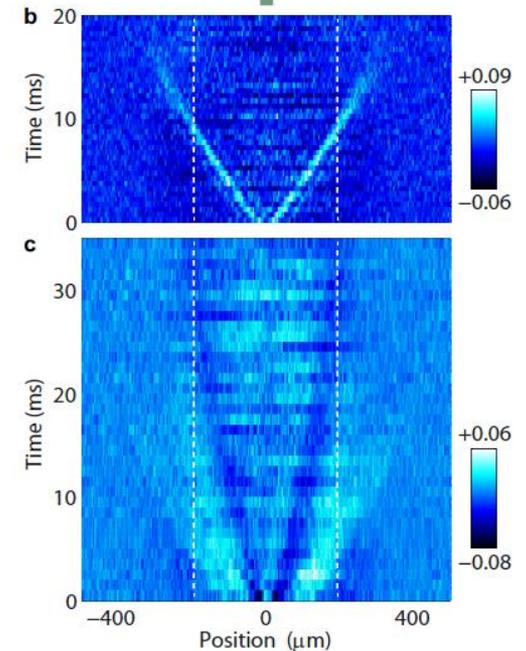
(Innsbruck)

Propagation of
second sound in
a Fermi superfluid



2013
(Trento)

Kibble Zurek generation
of quantum defects



Atoms are **neutral objects** and are **not sensitive to Lorentz force** which in charged systems is at the basis of important many-body phenomena (ex: Quantum Hall effect)

It is now possible to **create artificial gauge fields** which simulate in neutral systems the effect of a magnetic field on a charged particle

For a recent review see

Jean Dalibard:

Introduction to the physics of artificial gauge fields

[Proceedings of the International School of Physics "Enrico Fermi" of July 2014, "Quantum matter at ultralow temperatures"]

In the presence of a magnetic field the kinetic energy of a charged particle can be written as

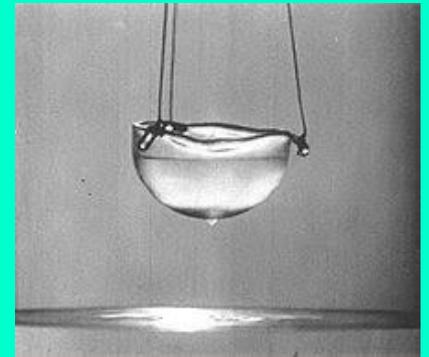
$$H = \frac{(\vec{p} - e\vec{A})^2}{2m}$$

Where p is canonical momentum operator. In the case of a uniform magnetic field oriented along the z -direction one has $A_y = Bx$, $A_x = A_z = 0$ (Landau gauge)

**Can we produce
similar Hamiltonians employing
neutral atoms and explore the
effects at the many-body level**

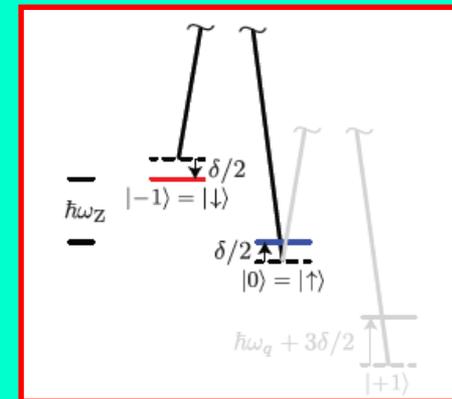
The simplest example:
Rotating a trapped gas

Analogy with bucket
experiment of superfluid Helium



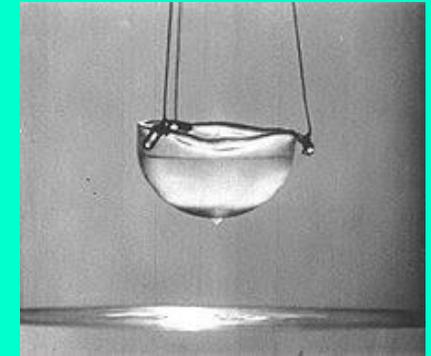
A more advanced example:
Spin-orbit coupling

Raman transitions between
two hyperfine states



The simplest example: **Rotating a trapped gas**

Analogy with bucket
experiment of superfluid Helium



This approach takes advantage of the similarity between the **magnetic Lorentz force** and the **Coriolis force** which appears in the rotating frame.

In practice one confines the gas in an isotropic harmonic trap and adds a slightly deformed potential which rotates at angular velocity Ω . The system is expected to thermalize in the rotating frame where the Hamiltonian takes the form:

$$H = \frac{\vec{p}^2}{2m} + \frac{1}{2} m \omega_{ho}^2 \vec{r}^2 - \Omega L_z \quad \text{with} \quad L_z = xp_y - yp_x$$

In rotating frame the Hamiltonian can be also written as

$$H = \frac{(\vec{p} - e\vec{A})^2}{2m} + \frac{1}{2}m\omega_{ho}^2 r^2 + V_{centrif.}$$

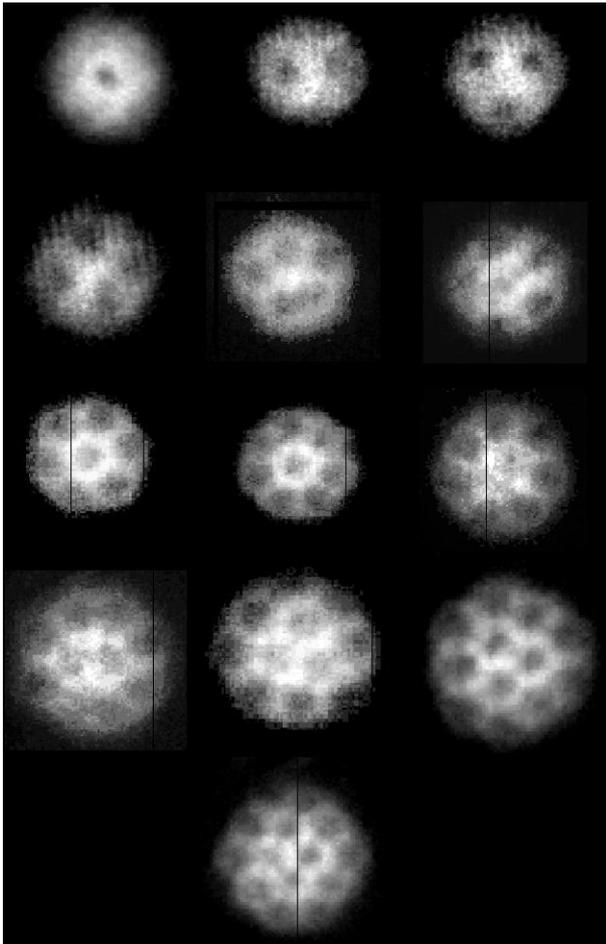
with $e\vec{A} = m\Omega(x\vec{j} - y\vec{i})$

$$V_{centrif.} = -\frac{1}{2}m\Omega^2(x^2 + y^2)$$

The rotation then gives rise to an **effective gauge field** of magnetic-type with the additional presence of a **centrifugal term**.

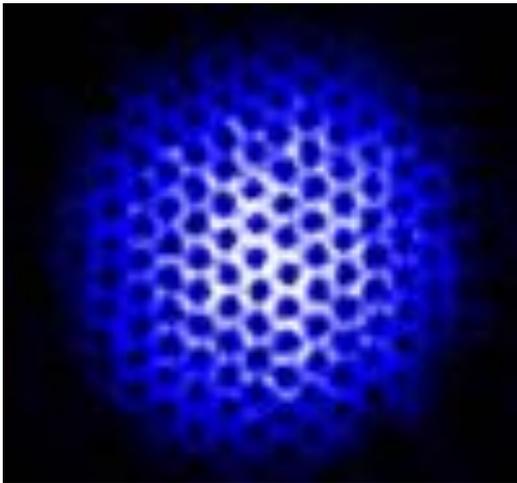
The centrifugal term contrasts the confinement provided by the harmonic trap and sets a limit to the available values of angular velocity

For sufficiently large angular velocity the **gauge field**, applied to a Bose-Einstein condensed gas, causes the appearance of **quantized vortices**

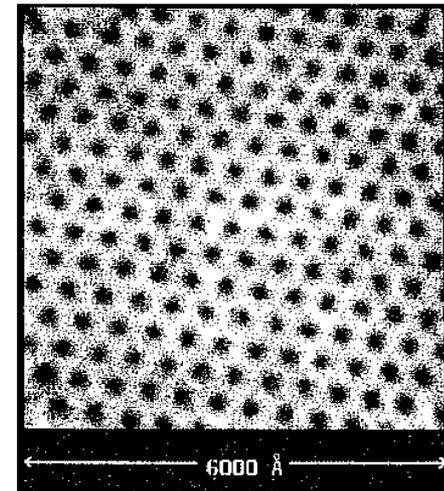


Quantized vortices obtained by rotating the confining trap at different angular velocities (ENS, 2000)

At higher angular velocity one can nucleate more vortices which form a **triangular lattice** (similar to **Abrikosov** lattice in superconductors)



Vortex lattice created in a rotating Bose-Einstein condensate
MIT, Jila (2001-2002)



STM image of vortex lattice in superconductor
(Bell Lab 1989)

The density of vortices is fixed by the angular velocity according to

$$n_v = \frac{N_v}{V} = \frac{m}{\pi\hbar} \Omega$$

If $N_v \ll N$ the system can be described by mean field regime (Gross-Pitaevskii theory)

If $N_v \approx N$ one enters the **Quantum Hall Regime** (so far inaccessible in rotating Bose-Einstein condensates)

Look for alternative methods to generate gauge fields

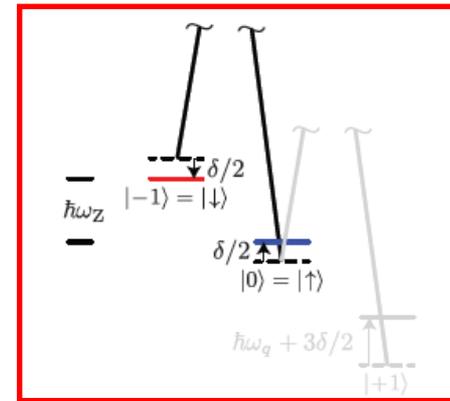
A more advanced example of generation of artificial
gauge fields:

Spin-orbit coupling

Simplest realization of spin-orbit coupling in a binary mixture ($s=1/2$) of Bose-Einstein condensates (Spielman, Nist, 2009)



Two detuned and **polarized** laser beams + non linear Zeeman field provide Raman transitions between two spin states, giving rise to new s.p. Hamiltonian



The Hamiltonian is invariant with respect to **helical (skew) translation** (**continuous** symmetry)

$$e^{id(p_x - k_0 \sigma_z)}$$

Rigid **translation** plus **rotation** in **spin space**

$$h_0^{lab} = \frac{\vec{p}^2}{2m} + \frac{\hbar\Omega}{2} \sigma_x \cos(2k_0 x - \Delta\omega_L t) + \hbar \frac{\Omega}{2} \sigma_y \sin(2k_0 x - \Delta\omega_L t) - \hbar \frac{\omega_Z}{2} \sigma_z$$

Unitary transformation
transforms h_0^{lab}

$$e^{i\Theta\sigma_z/2}$$

with $\Theta = 2k_0x - \Delta\omega_L t$

into **translationally invariant, time independent**
spin-orbit Hamiltonian

$$h_0 = \frac{1}{2m} [(p_x - k_0\sigma_z)^2 + p_{\perp}^2] + \frac{1}{2}\hbar\Omega\sigma_x + \frac{1}{2}\hbar\delta\sigma_z$$

$p_x = -i\hbar\partial_x$ is canonical momentum
 k_0 is laser wave vector difference
 Ω is strength of Raman coupling
 $\delta = \Delta\omega_L - \omega_Z$ is effective Zeeman field

physical momentum (and
physical velocity) equal to

$$P_x = mv_x = (p_x - k_0\sigma_z)$$

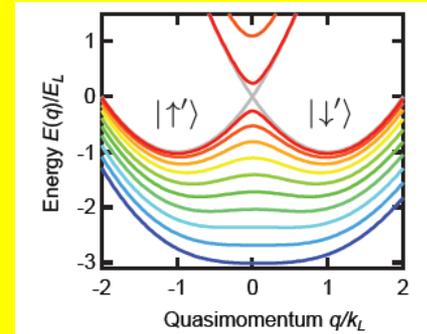
Spin orbit Hamiltonian is
translationally invariant.

However it breaks

- **Galilean** invariance
as well as

- **Parity & Time Reversal**

Single particle spin-orbit
Hamiltonian is characterized
by a novel
two band structure



- **Novel many-body physics** caused by the profound modification of the single particle Hamiltonian and by the presence of a **spin dependent gauge field**
- Many properties of the **ground state** as well as of the **excited states** are now investigated both theoretically and experimentally.

Different strategies to realize novel quantum phases

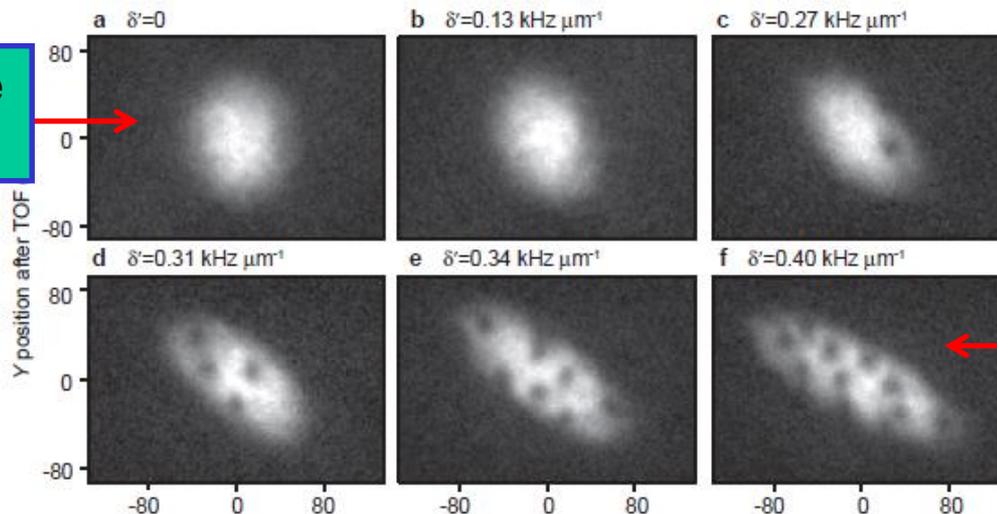
- **First strategy** (Lin et al., Nature 2009).

Spatially dependent detuning ($\delta(y)$) in strong Raman coupling ($\Omega \gg k_0^2$) regime yields position dependent vector potential

$$h_0 = \frac{1}{2m^*} (p_x - A_x(y))^2 \quad \text{and} \quad \text{effective Lorentz force in neutral atoms.}$$

This causes the appearance of quantized vortices (**no need to rotate the confining trap**)

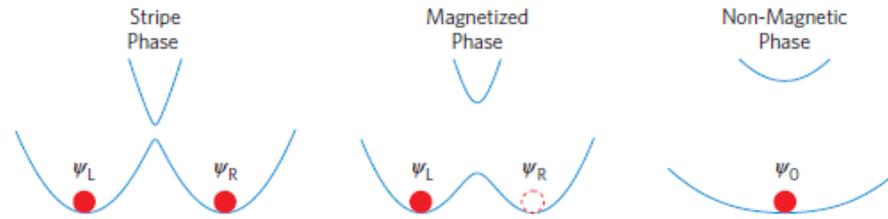
No y-dependence
In detuning



strong
y-dependence
In detuning

Second strategy (Lin et al. Nature 2011). At small Raman coupling lowest band exhibits **two degenerate minima** which can host a BEC.

As a function of coupling one predicts different phases



Order parameter in the new phases

I) Stripe phase

$$\Psi = \sqrt{\frac{N}{2V}} \left[\begin{pmatrix} \cos \theta \\ -\sin \theta \end{pmatrix} e^{ik_1 x} + \begin{pmatrix} \sin \theta \\ -\cos \theta \end{pmatrix} e^{-ik_1 x} \right]$$

II) Plane wave phase

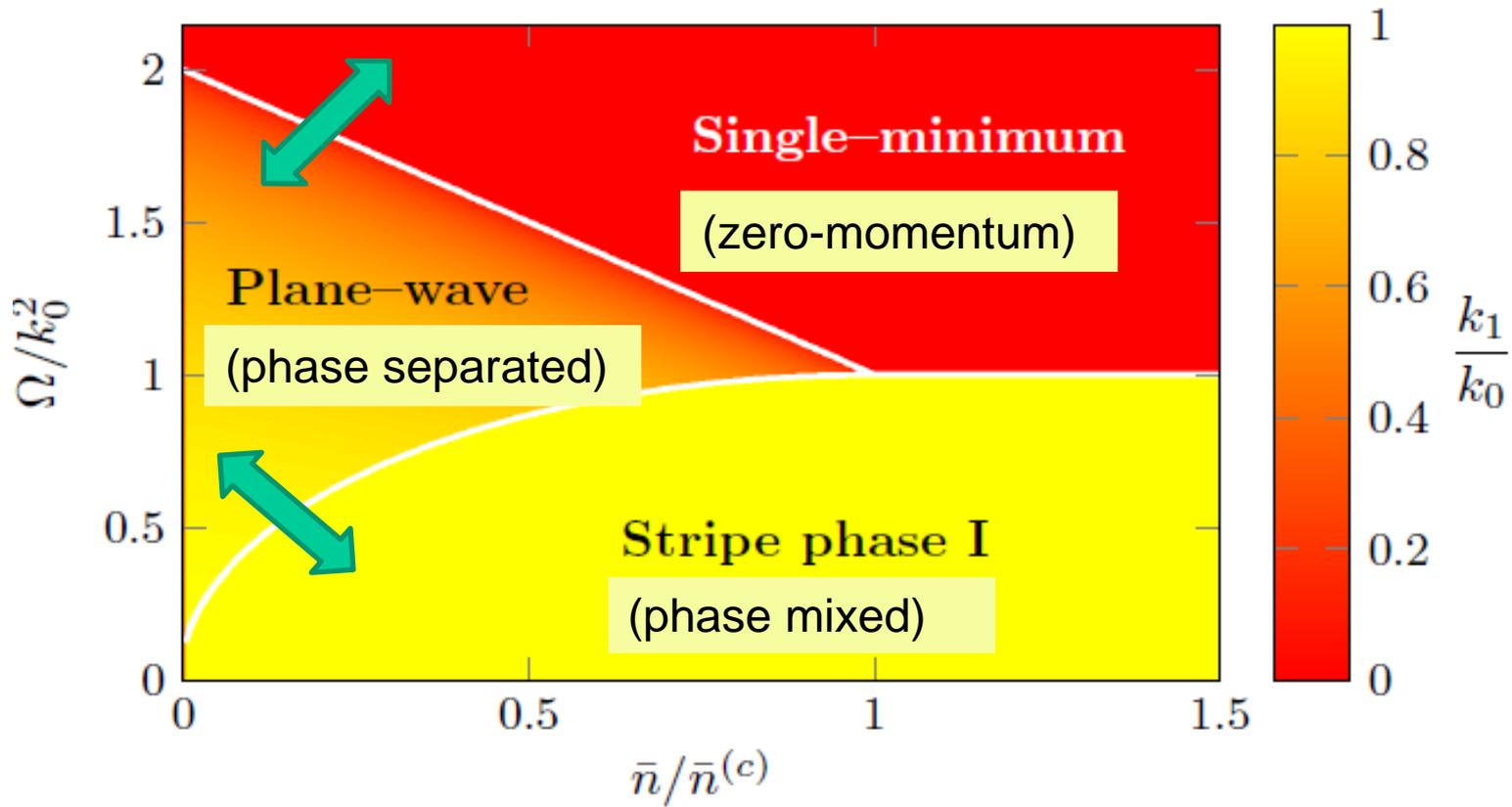
$$\Psi = \sqrt{\frac{N}{2V}} \begin{pmatrix} \sin \theta \\ -\cos \theta \end{pmatrix} e^{-ik_1 x}$$

$$\langle \sigma_z \rangle = \frac{k_1}{k_0}$$

III) Zero momentum phase

$$\Psi = \sqrt{\frac{N}{V}} \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

New quantum phases ($T=0$)



Plane wave-Single minimum phase transition

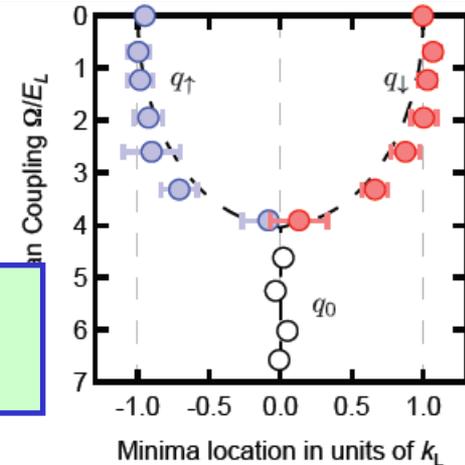
Transition is **second order**.

It has been observed at the predicted value

$$\Omega = \Omega_c \approx 2k_0^2$$

of the Raman coupling

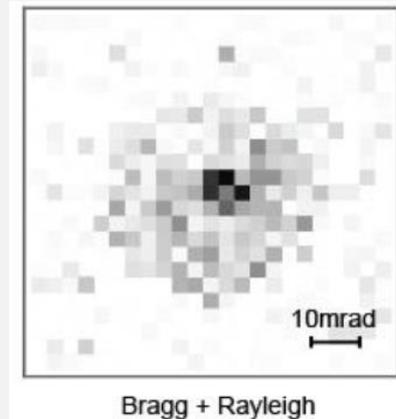
Lin et al.,
Nature 2011



Plane wave-Stripe phase transition

Transition is **first order**.

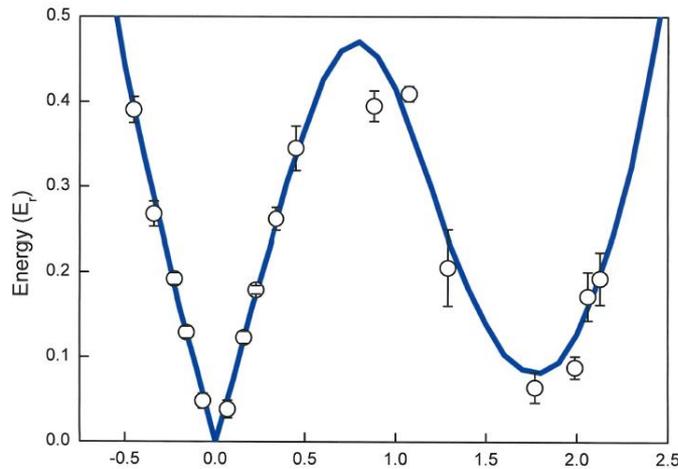
First experimental evidence of stripe phase has become recently available via Bragg scattering (MIT 2017)



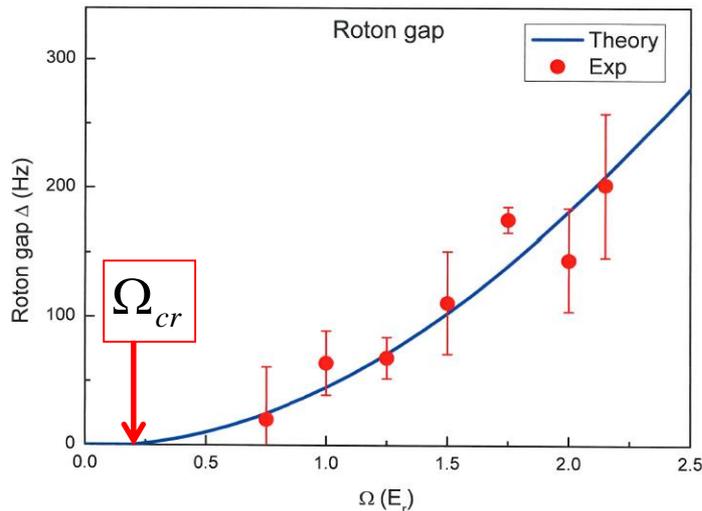
Spin-orbit coupling has **important** consequences
on the **dynamic** and **superfluid behavior**
of a Bose-Einstein condensate

At small Raman coupling, near the transition to the stripe phase a **roton** structure emerges in the excitation spectrum

Exp: Si-Cong Ji et al., PRL 114, 105301 (2015)
Theory: Martone et al., PRA 86, 063621 (2012)



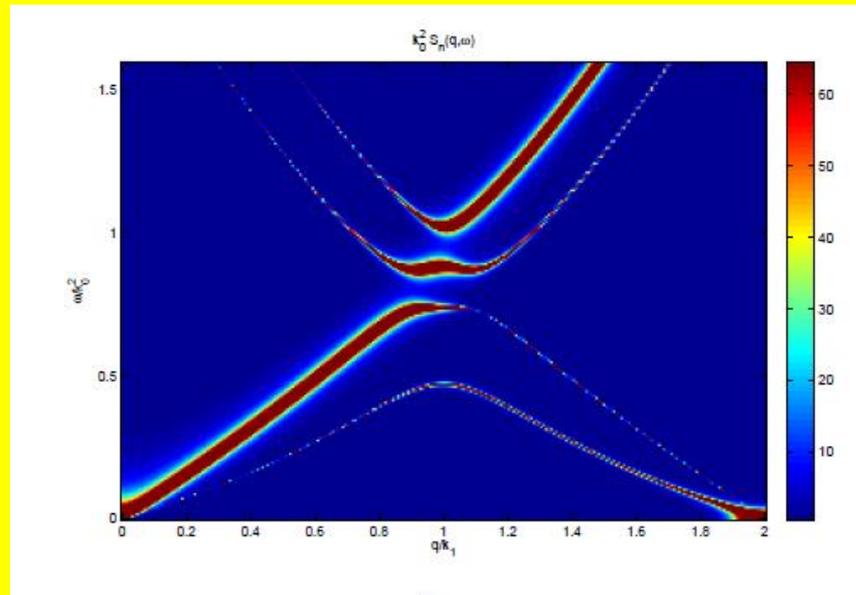
$\omega(q) \neq \omega(-q)$ consequence of violation of **parity** and **time reversal** symmetry



Roton gap decreases as Raman coupling is lowered:
onset of crystallization
(**striped** phase)

Striped phase (supersolid phase) results from **spontaneous** breaking of two continuous symmetries: **gauge** and **translational** symmetries

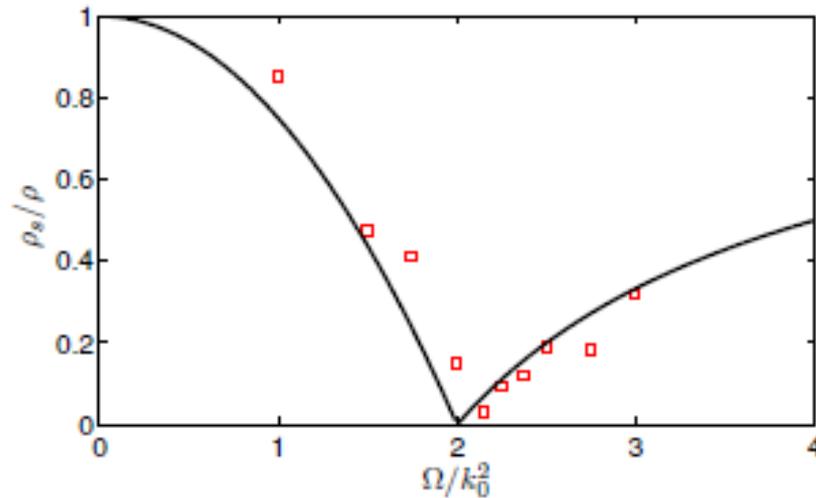
Two Goldstone modes:



- Double band structure in the striped phase of a SO coupled Bose-Einstein condensate (Yun Li et al. PRL 2013)
- No experiments available so far !!

Breaking of **Galilean** invariance caused by spin-orbit coupling has major consequences on the **superfluid behavior**

Superfluid density as a function of Raman coupling



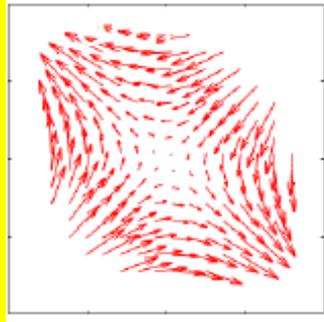
$$\rho_s = \rho m c^2 \kappa$$

- Superfluidity disappears at the transition between plane wave-and single minimum phases
- Full line is prediction of theory (Hong Kong- Trento 2016)
- Exp points are obtained using measured values of sound velocity (Shanghai 2015)

Moment of inertia of a spin-orbit coupled BEC

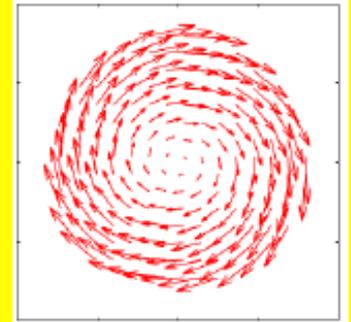
Can a **BEC rotate** like a **rigid body** ?

$$\vec{v} \propto \nabla(xy)$$



**Superfluid
(irrotational)
flow**

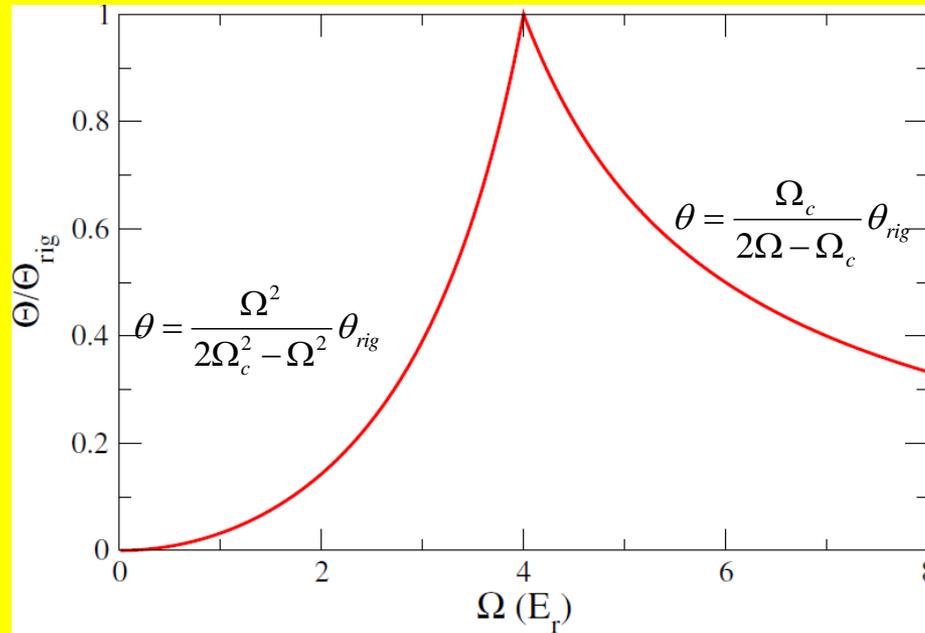
$$\vec{v} = \vec{\omega}_{rot} \times \vec{r}$$



**Non superfluid
(rigid body)
flow**

Behavior of moment of inertia

(S.S. PRL 18, 145302 2017)



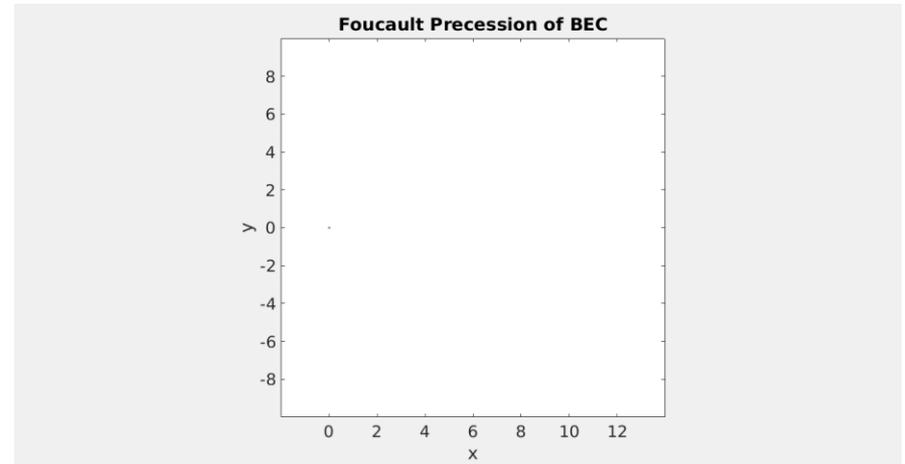
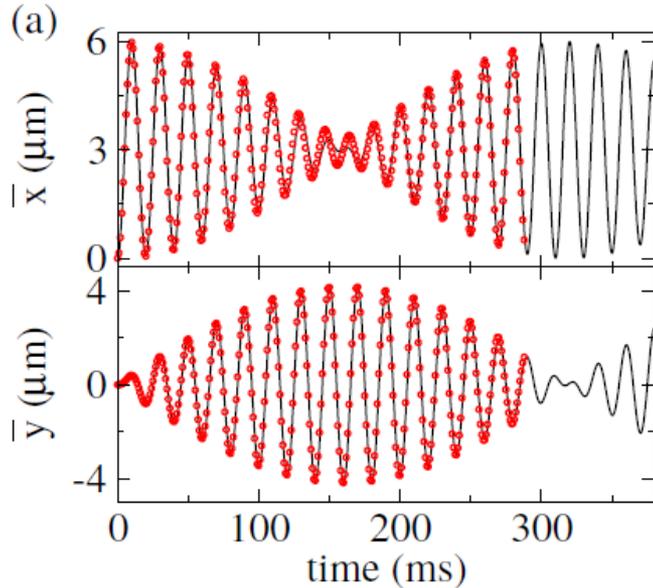
Rigid value $\theta = \theta_{rig}$ at the transition
between plane wave and single momentum phase.
Dramatic consequence of spin-orbit coupling

The presence of the artificial gauge field caused by spin-orbit coupling brings effectively the quantum system into a **non inertial frame**

Foucault pendulum in a spin-orbit coupled gas

(Chunlei Qu and S.S., PRL 2018)

Precession following the excitation
of the dipole mode along x



MAIN CONCLUSION AND PERSPECTIVES

- The investigation of synthetic (artificial) gauge fields is opening **rapidly evolving frontiers** of experimental and theoretical research in cold atomic physics.
- Many other important issues (not addressed in this talk):
 - realization of **2D and 3D** spin orbit coupling
 - Gauge fields in the presence of **optical lattices**
 - **Synthetic dimensions**
 - Superfluidity of **supersolid** matter
 - Synthetic gauge fields in Fermi superfluids
 - **Non Abelian** gauge fields (Rashba Hamiltonian)
 - **Berry's phase**
 - novel **topological properties** of quantum matter
 - etc..

The Trento BEC team



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