

Nucleon-Transfer Reactions with Radioactive Ion Beams

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International School of Physics
"Enrico Fermi"

14-19 July 2017

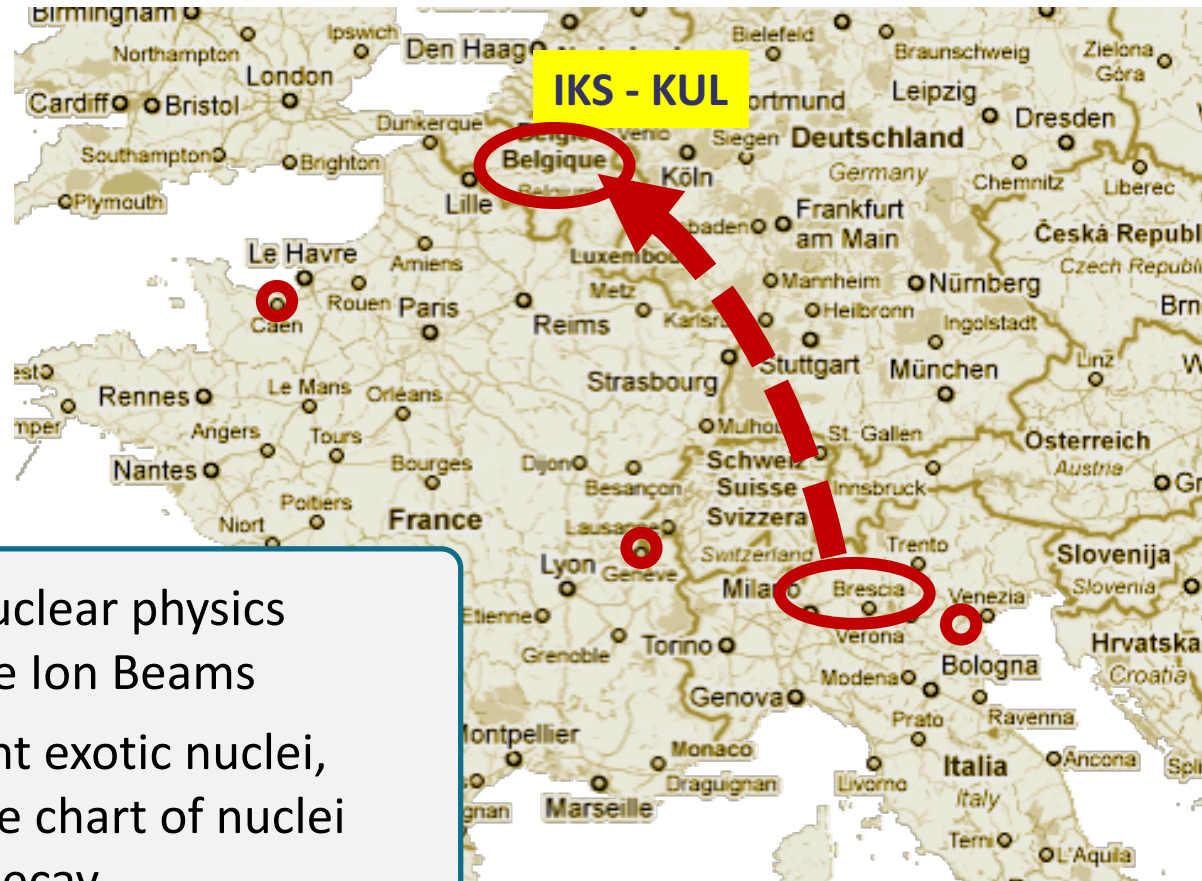
Nuclear Physics with Stable
and Radioactive Ion Beams

Lecture 1/3

About myself



About myself



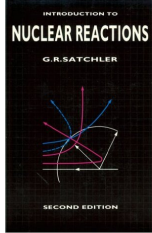
- Experimental nuclear physics with Radioactive Ion Beams
- Started with light exotic nuclei, moving up in the chart of nuclei
Reactions and decay
- Development of new instruments

Contents

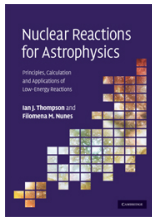
- Nuclear reactions
 - Types of reactions
 - Characteristics of direct reactions
- Why use transfer reactions
 - Information from reactions
 - Q-value, angular momentum, spectroscopic factors
- Reactions and RIBs
 - Motivations
 - Challenges: inverse kinematics
- Case studies
 - Light nuclei
 - Transfer and gammas Ne-Na
 - Mg and Ni, the 0^+ s
 - Ni region
 - Sn region
 - ...

References

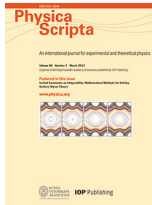
Nuclear reactions



- GR Satchler
Introduction to Nuclear Reactions
MacMillan
- IJ Thompson and FM Nunes
Nuclear Reactions for Astrophysics
Cambridge University Press



Physics with RIBs



- Nobel Symposium 152:
Physics with Radioactive Beams
Physica Scripta T152

Survey of shell evolution far from stability

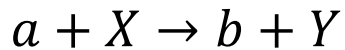
- O Sorlin and M-G Porquet
Progress in Particle and Nuclear Physics 61 (2008) 602

Contents

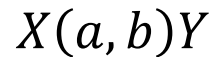
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Nuclear reactions

- A nucleus X collides with a probe a (particle, γ -ray).
In the collision they exchange energy, momentum and possibly mass
As a result we obtain a product nucleus Y and some outgoing radiation b (particle, γ -ray)

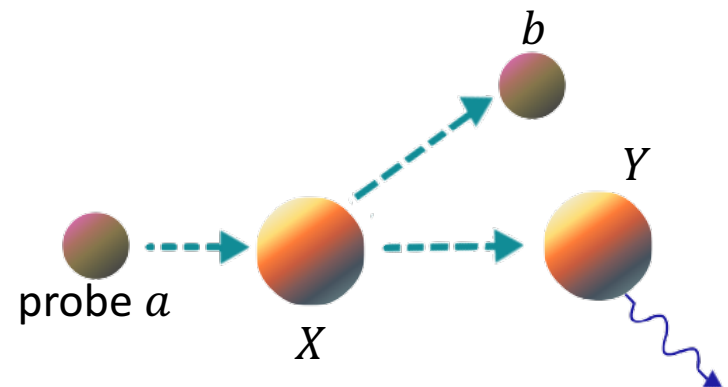


- Alternative notation:



Puts the accent on the process (a, b)

- Two aspects:
 - study the reaction mechanism
 - use reactions to investigate the structure of nuclei (\rightarrow use simple probes)



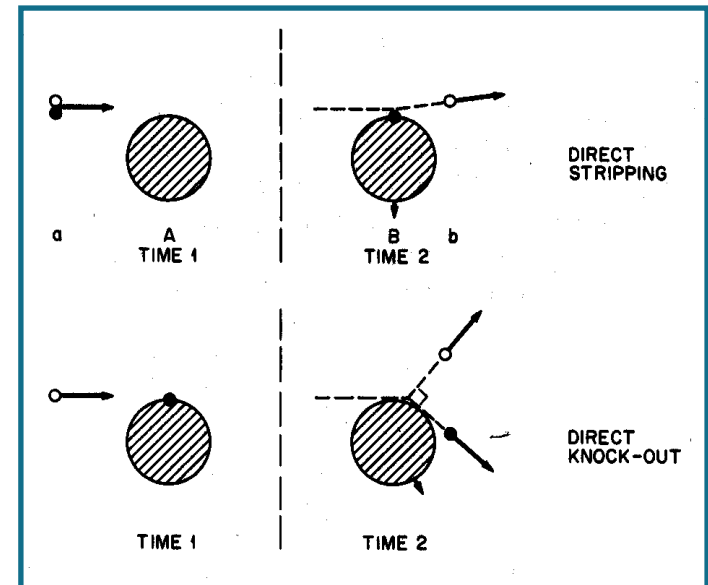
Types of reactions (list not exhaustive)

- Elastic scattering: $X(a, a)X$ $^{12}\text{C}(p, p)^{12}\text{C}$ $^{208}\text{Pb}(n, n)^{208}\text{Pb}$
Always present!
- Inelastic scattering: $X(a, a')X^*$ $^{12}\text{C}(p, p')^{12}\text{C}^*$ $^{40}\text{Ca}(\alpha, \alpha')^{40}\text{Ca}^*$
- Rearrangement reactions: (ex)change of mass
 - Transfer reactions:
 - stripping $X((a + c), a)(X + c)$ $^{12}\text{C}(d, p)^{13}\text{C}$
 - pick-up $(X + c)(a, (a + c))X$ $^{12}\text{C}(p, d)^{11}\text{C}$
 - Knock-out reactions: $X(a, ac)Y$ $^{12}\text{C}(p, 2p)^{11}\text{B}$
- Photo-disintegration: $X(\gamma, a)Y$ $^{16}\text{O}(\gamma, \alpha)^{12}\text{C}$
- Capture reactions: $X(a, \gamma)Y$ $^{14}\text{N}(\alpha, \gamma)^{18}\text{F}$

- Combination of particles: **partition**
- Partition with specified excited states: **channel**
- Different exit channels may be present (**open**) at the same time depending on conservation principles

Characteristics of direct reactions

- Direct reactions: inelastic scattering, transfer, breakup
 - Fast, only few nucleons involved
 - Likely to occur at small exit angles (peripheral)
 - Time scale $\tau \ll 10^{-22}$ s
 - Modelled as one-step processes
- Tend to probe the “valence” nucleons (depends on the energy)
- Very selective
Provide information about the similarity between initial and final states



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Information provided by reactions

- (all reactions)
The Q -value (difference in kinetic energies) identifies the excitation energy of the populated state
- (direct reactions)
The initial and final spins are connected through the transferred angular momentum, which can be measured
- (transfer reactions)
The cross section is a measure of the weight of a given configuration within the populated state

Transfer reactions are an excellent spectroscopic probe: they measure how much the wave function of a particular state may be described by a single-particle motion within the nucleus

Conservation of energy

- $E_{k,i} + M_i c^2 = E_{k,f} + M_f c^2$

where the masses include the excitation energy

- In the centre-of-mass system:

$$E'_{k,i} + \underbrace{(M_i c^2 - M_f c^2)}_{Q\text{-value for the } (i, f) \text{ channel}} = E'_{k,f} > 0 \rightarrow E'_{k,i} > -Q$$

Threshold
for the (i, f) channel

- Q is usually calculated through the mass excess $\Delta = (M - A)c^2$

- In the laboratory system:

$$Q = E_{k,f} - E_{k,i}$$

→ we can measure Q and thus
identify the channel

Example: $^{40}\text{Ca}(d,p)^{41}\text{Ca}$:

$$\Delta(^{40}\text{Ca}) = -34846 \text{ keV}$$

$$\Delta(^{41}\text{Ca}) = -35138 \text{ keV}$$

$$\Delta(d) = 13136 \text{ keV}$$

$$\Delta(p) = 7289 \text{ keV}$$

$$\rightarrow Q = 6139 \text{ keV} = 6.139 \text{ MeV}$$

Conservation of angular momentum (and parity)

- $\mathbf{J}_a + \mathbf{J}_A + \vec{\ell}_\alpha = \mathbf{J}_b + \mathbf{J}_B + \vec{\ell}_\beta$

The transferred angular momentum in $a + A \rightarrow b + B$

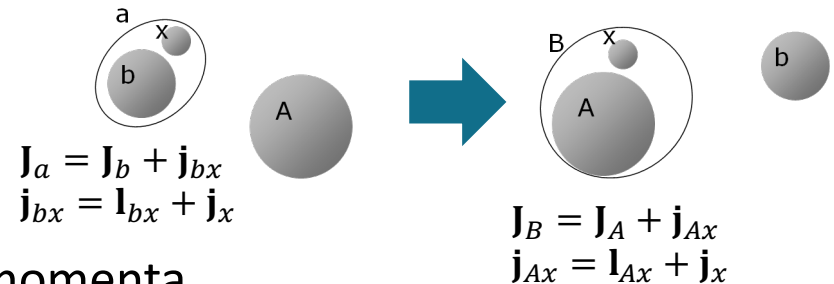
is defined as $\mathbf{l} = \vec{\ell}_\alpha - \vec{\ell}_\beta$

- Transfer reactions: $(b + x) + A \rightarrow b + (A + x)$ with $b + x = a$, $A + x = B$

$$\mathbf{l} = (\mathbf{J}_B - \mathbf{J}_A) + (\mathbf{J}_b - \mathbf{J}_a)$$

$$\mathbf{l} = \mathbf{j}_{Ax} - \mathbf{j}_{bx}$$

$$\rightarrow \mathbf{l} = \mathbf{l}_{Ax} - \mathbf{l}_{bx}$$



\rightarrow l is constrained by the binding angular momenta

\rightarrow only few l participate for a given channel

For one-nucleon transfers, these binding angular momenta are directly given by the shell-model orbitals (s,p,d,g...)

- Also, for a given channel parity must be conserved:

$$\pi_a \pi_A \pi_b \pi_B = (-1)^l = (-1)^{l_{bx} + l_{Ax}}$$

\rightarrow either only odd l (change of parity) or only even l participate

How to measure the transferred angular momentum

Semi-classical argument

- Reaction takes place on the surface of the target nucleus
- Transferred angular momentum: $\mathbf{l} = \mathbf{q} \times \mathbf{R}$
where $\mathbf{q} = \mathbf{k}_\alpha - \mathbf{k}_\beta$ is the transferred momentum
- For a given populated state \mathbf{q} is fixed in magnitude
For a given observation angle \mathbf{k}_β is fixed in direction
→ l/q is fixed (angle β between \mathbf{q} and \mathbf{R} is fixed)
→ events originate on two rings with radius l/q
- Conditions on the observation angle θ

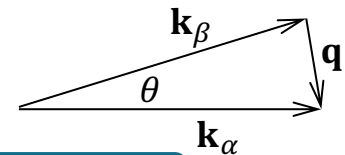
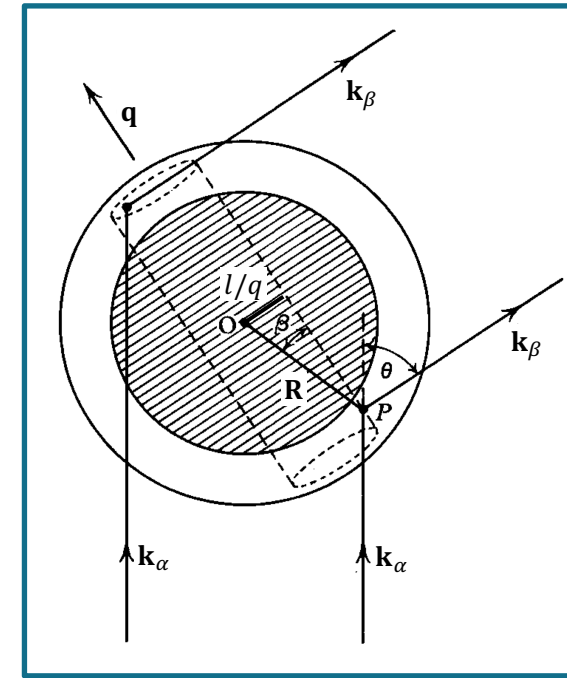
For $\mathbf{q} \ll \mathbf{k}_\alpha \approx \mathbf{k}_\beta$:

- $q \approx \bar{k}\theta$ (with $\bar{k} = (k_\alpha + k_\beta)/2$ or $\bar{k} = \sqrt{k_\alpha k_\beta}$)
- $l/q \leq R$ (reaction on the surface)

we find

$$\theta \geq l/\bar{k}R$$

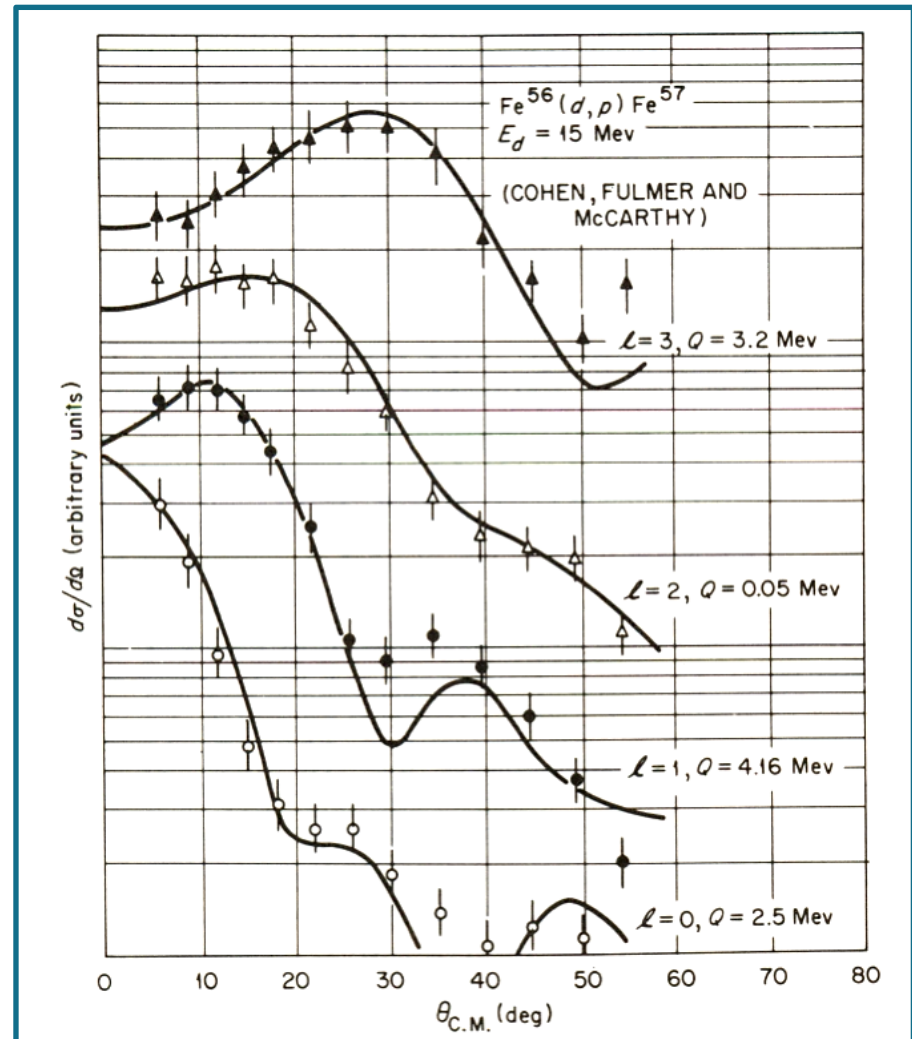
Relation between the transferred angular momentum and the scattering angle



- Also: constructive interference for $2R\theta = n\lambda \rightarrow \theta \approx n\pi/\bar{k}R$

How to measure the transferred angular momentum

- First maximum for $\theta \approx l/\bar{k}R$
- Maxima separated by $\Delta\theta \approx \pi/\bar{k}R$



BL Cohen et al, Phys Rev 126 (1962) 698

Cross sections

- Solution of the scattering problem
plane wave + modulated spherical wave

$$\psi(\mathbf{r}) \xrightarrow{r \rightarrow \infty} e^{i\mathbf{k} \cdot \mathbf{r}} + f(\theta, \varphi) \frac{e^{ikr}}{r}$$

scattering amplitude

- Cross section $d\sigma/d\Omega \propto |f(\theta, \varphi)|^2$

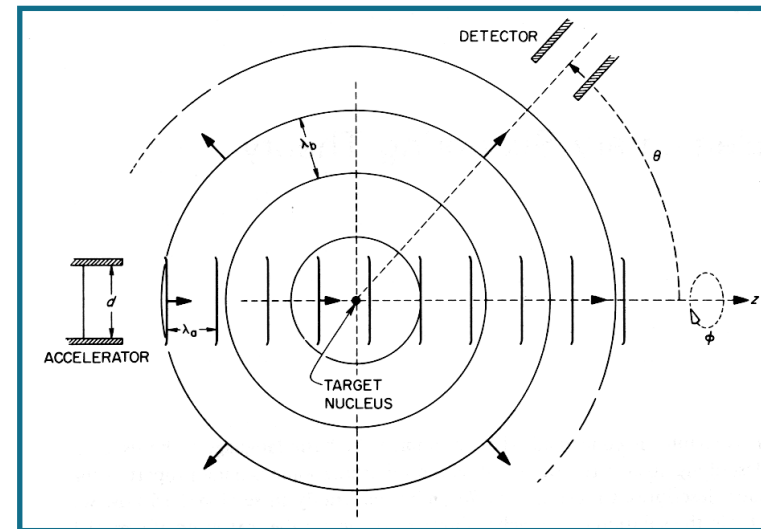
- Schrödinger equation:
 $(\nabla^2 + k^2)\psi(\mathbf{r}) = U(\mathbf{r})\psi(\mathbf{r})$
has the (formal) solution

$$\psi(\mathbf{r}) \xrightarrow{r \rightarrow \infty} e^{i\mathbf{k} \cdot \mathbf{r}} - \frac{e^{ikr}}{4\pi r} \int e^{-i\mathbf{k}' \cdot \mathbf{r}'} U(\mathbf{r}') \psi(\mathbf{r}') d\mathbf{r}'$$

(various ways to solve)

- For a transfer, $U(\mathbf{r})$ connects the initial and final states:

$$U \approx \int \phi_a^* \phi_A^* V \phi_b \phi_B d\tau$$



Spectroscopic factors

$U \approx \int \phi_a^* \phi_A^* V \phi_b \phi_B d\tau$ integral on the internal states

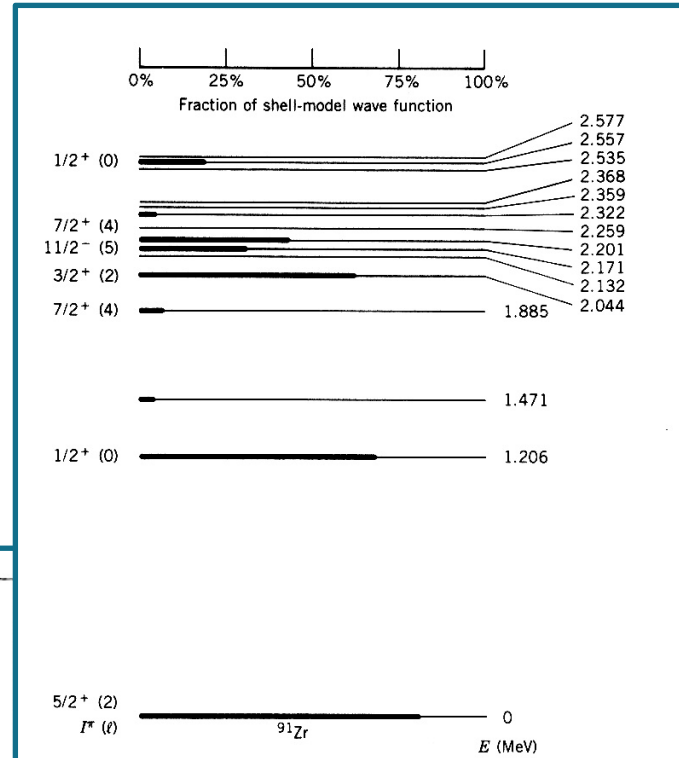
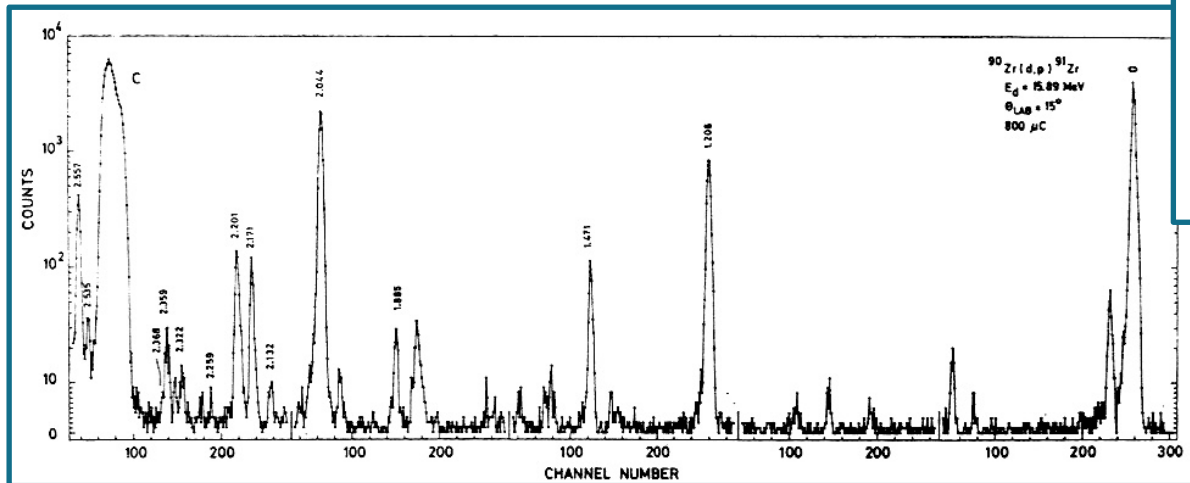
- The important part is the overlap between ϕ_A and ϕ_B which is expressed by the spectroscopic factor (various definitions)
- For the transfer of a cluster x one assumes: $\phi_B = (\phi_A \phi_x)_{l_{Ax} j_{Ax}}$ and calculates the cross section accordingly
- “Experimental” spectroscopic factors can then be obtained as ratio of the measured cross section to the calculated one:

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = S_{(l_{Ax} j_{Ax}) J_B} \left(\frac{d\sigma}{d\Omega}\right)_{\text{cal}}$$

The spectroscopic factor is a measure of how much the populated state contains the “pure” cluster (single-particle) configuration

Spectroscopic factors

- Spectroscopic factors are obtained from cross sections (integral of the peaks)
- Angular distributions are fitted to extract l and normalised to the calculated ones to obtain S



HP Block et al, Nucl Phys A 273 (1976) 142

Spectroscopic factors - caution

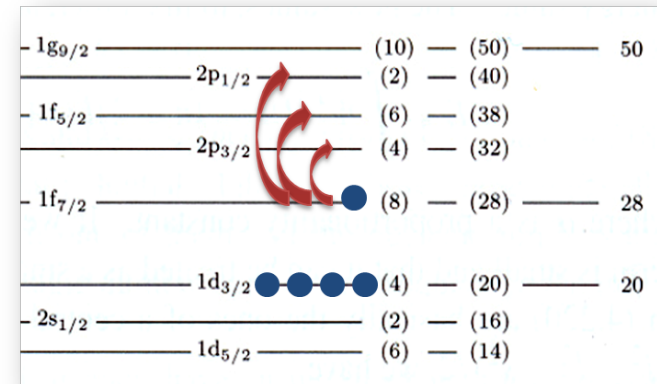
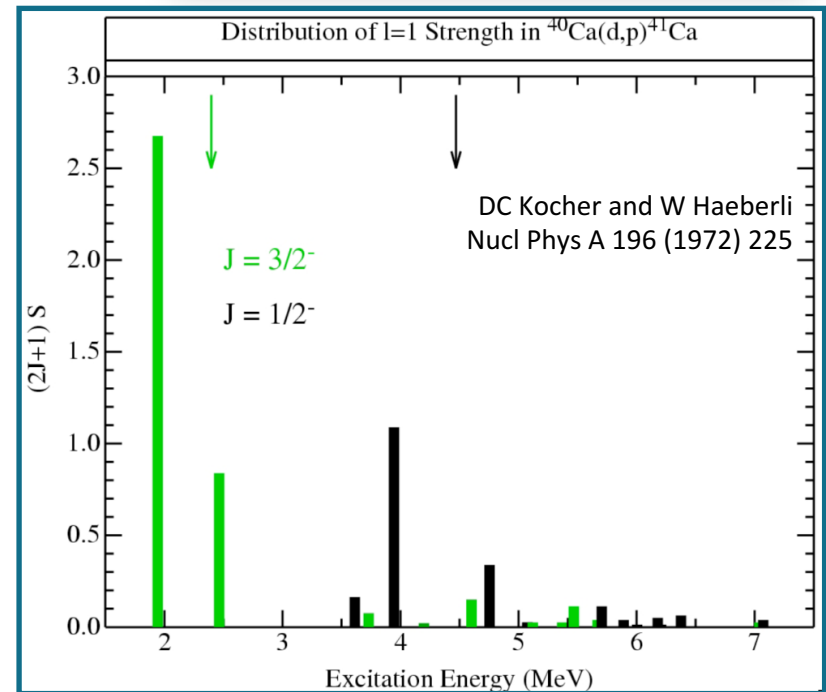
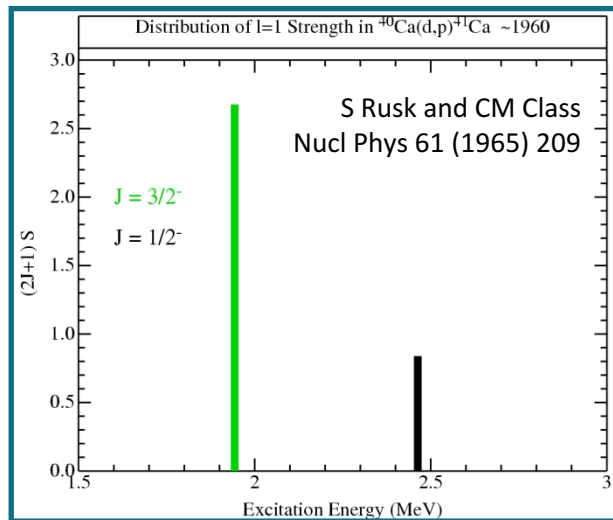
1. Absolute spectroscopic factors depend upon
 - the approximation used for the calculation (DWBA, ADWA, CRC...)
 - the potentials (interaction and binding)

→ usually, relative spectroscopic factors are used to derive structure information
2. For pure “single-particle” states the spectroscopic factors satisfy sum rules
However, a given configuration could be present in several excited states (fragmentation)
and it is usually difficult to measure all the strength

Strength fragmentation

- If the strength is fragmented:
the single-particle energy is taken to be the **centroid** (mean energy, weighted by the spectroscopic factor)
- Need to detect as much strength as possible!

$$E_{s.p.} = \sum S_i E_i$$



Example: $p_{3/2}-p_{1/2}$ spin-orbit splitting in ^{41}Ca

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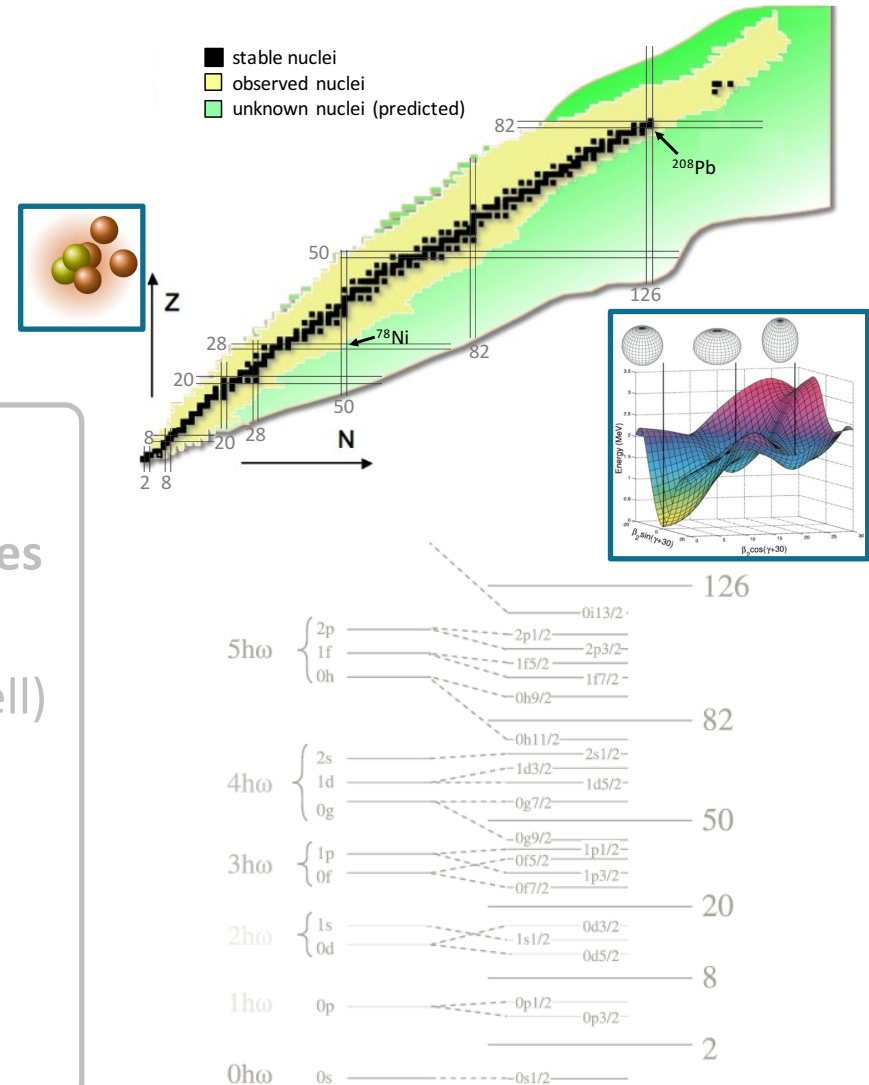
New physics far from stability

- Halos, cluster structures
- Shape transitions and coexistence (macroscopic picture)
- Changes in the shell structure

Why these changes?

An excess of neutrons or protons enhances particular aspects of the N-N interaction

- Matter distribution (shape potential well)
- Spin-orbit force
- Three-body forces
- Tensor interaction
- ...



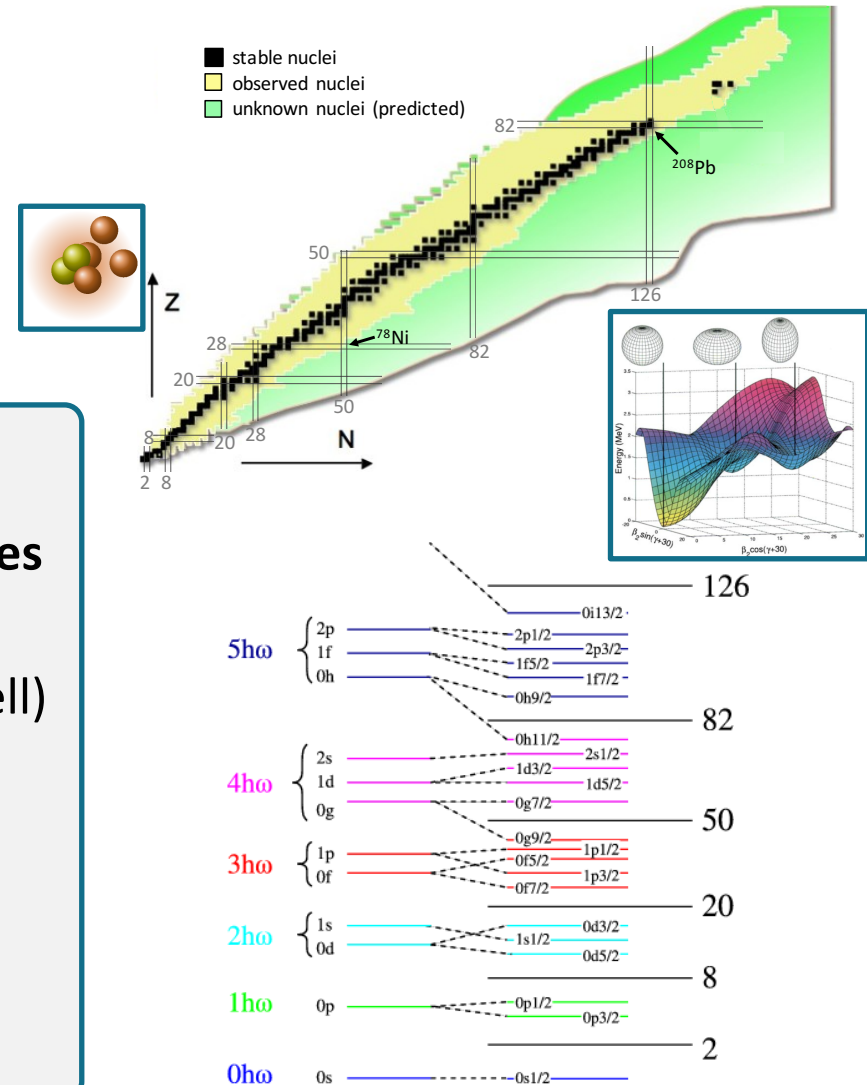
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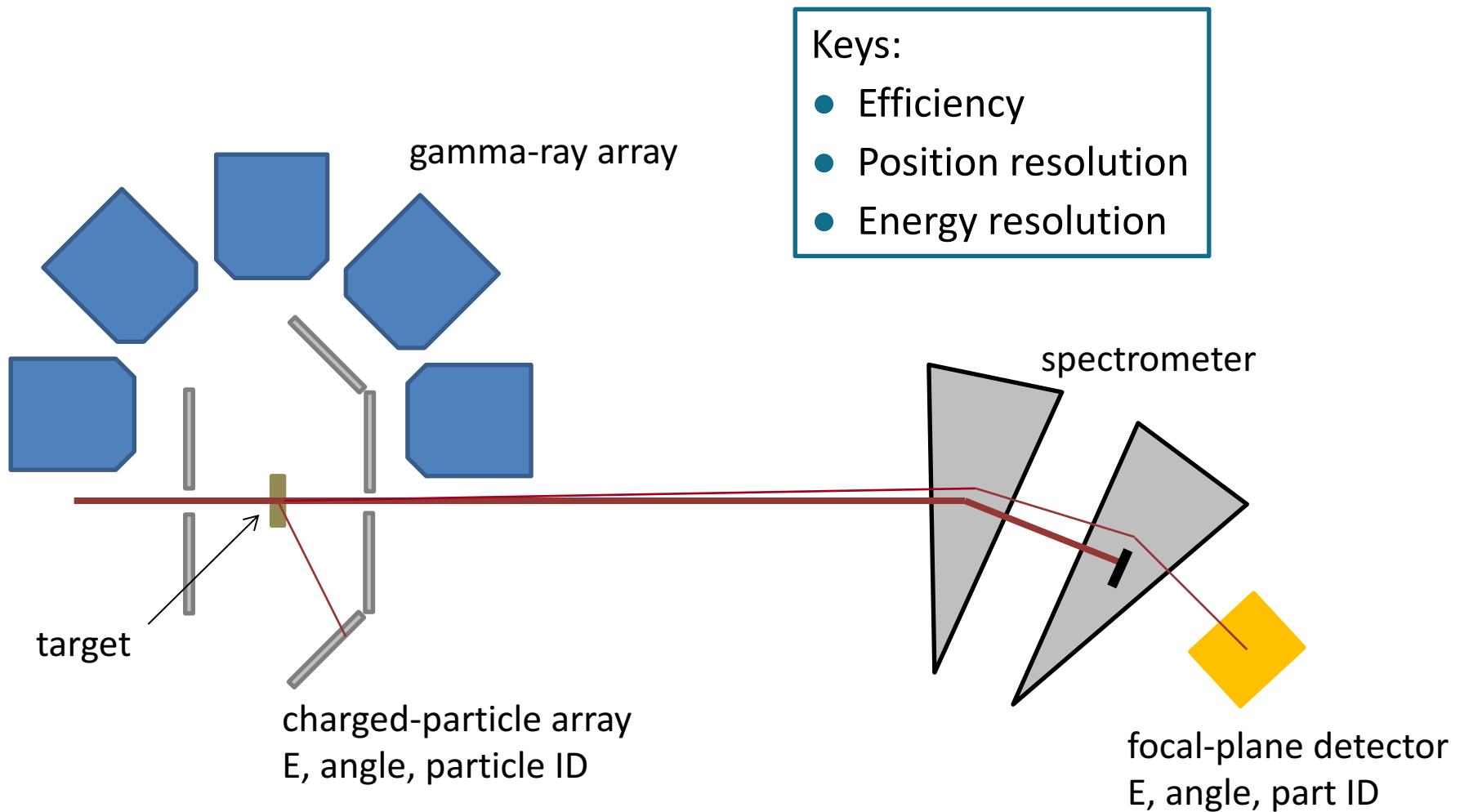
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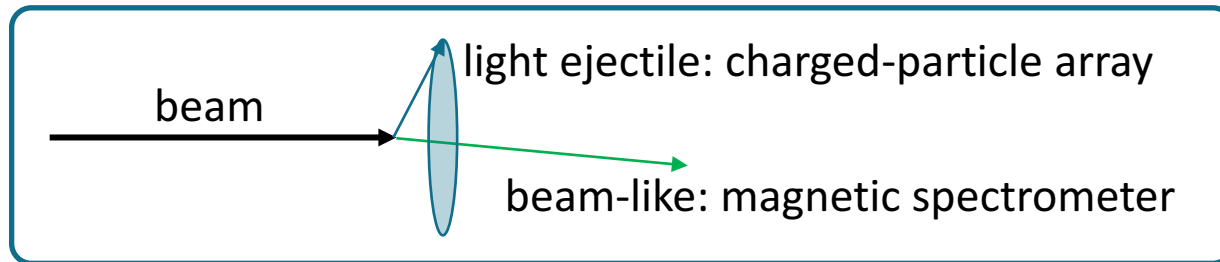
- Matter distribution (shape potential well)
- Spin-orbit force
- Three-body forces
- Tensor interaction
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General setup



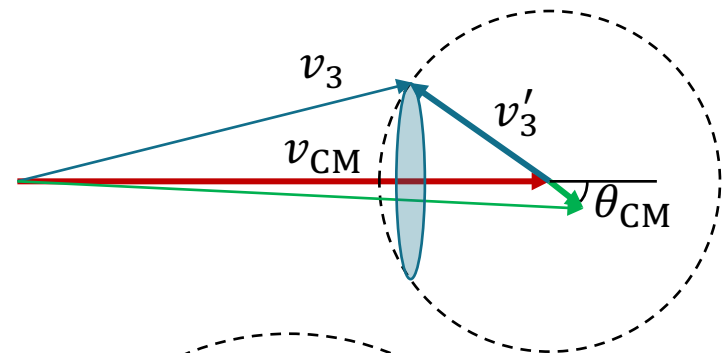
Inverse kinematics



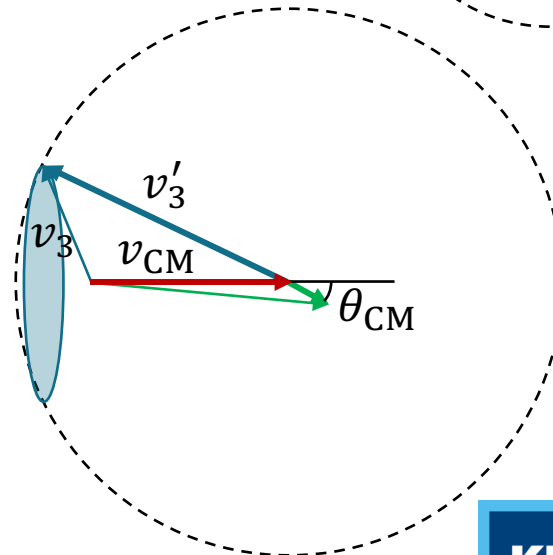
$$\frac{v'_3}{v_{\text{CM}}} \xrightarrow{Q \ll E} \approx \sqrt{\frac{m_2 m_4}{m_1 m_3}} \approx \sqrt{\frac{m_2}{m_3}}$$

inverse
kinematics

$m_2 < m_3$
pick-up (p,d)



$m_2 > m_3$
stripping (d,p)



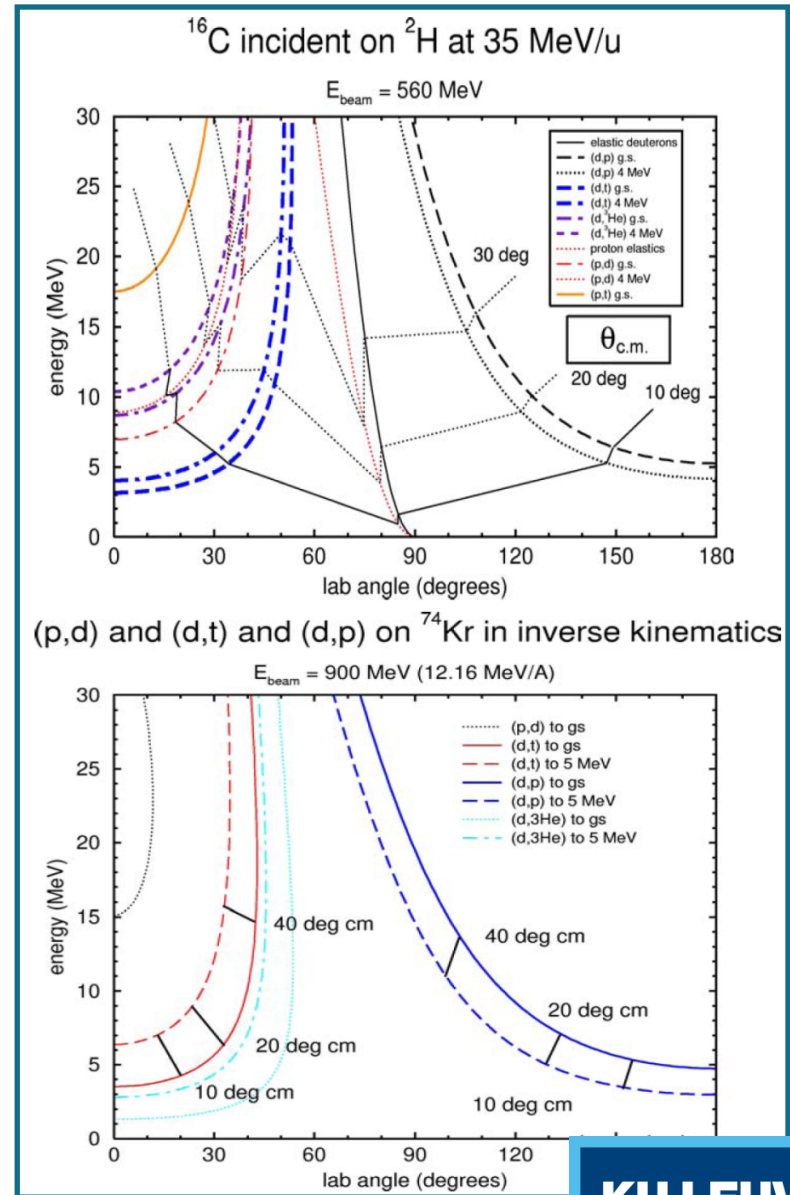
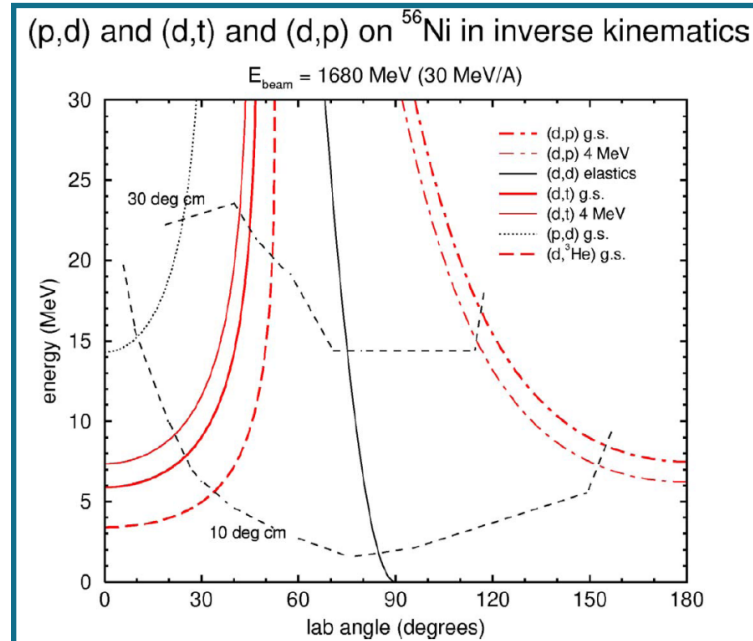
Exotic nuclei: inverse kinematics

source: Wilton Catford

Light particles

Kinematics depends:

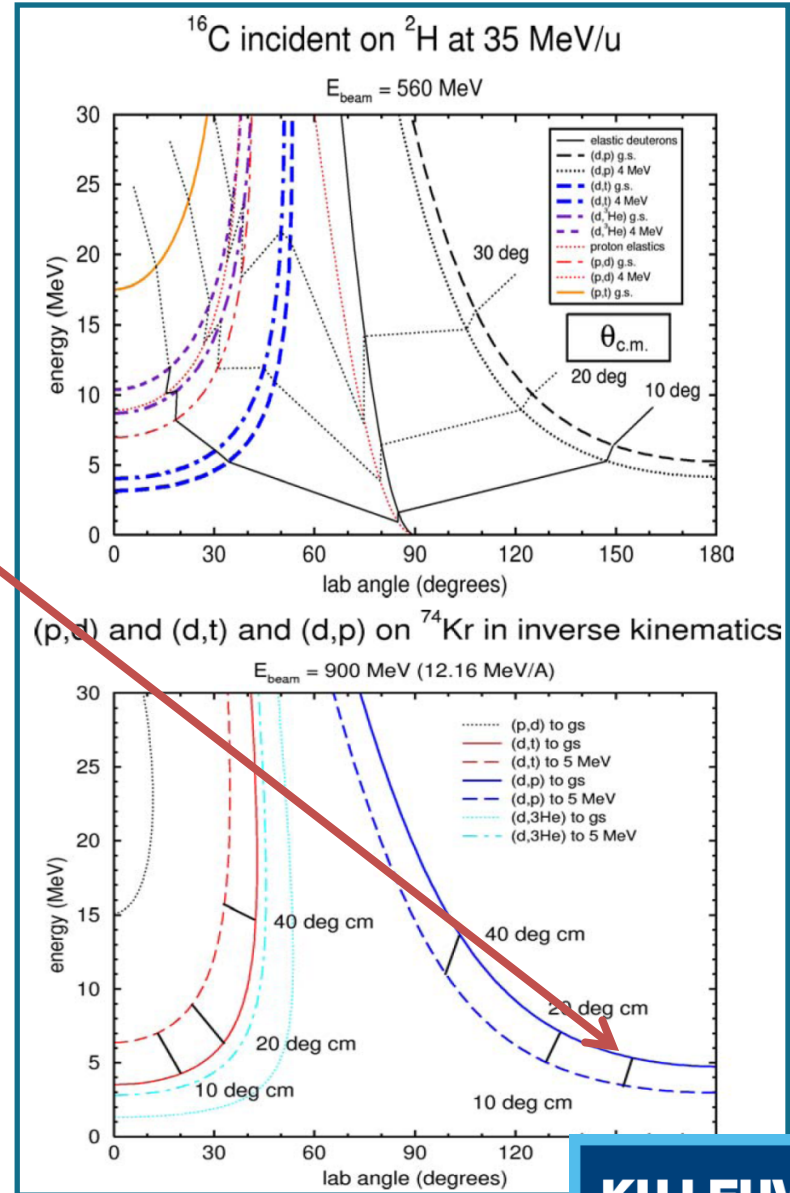
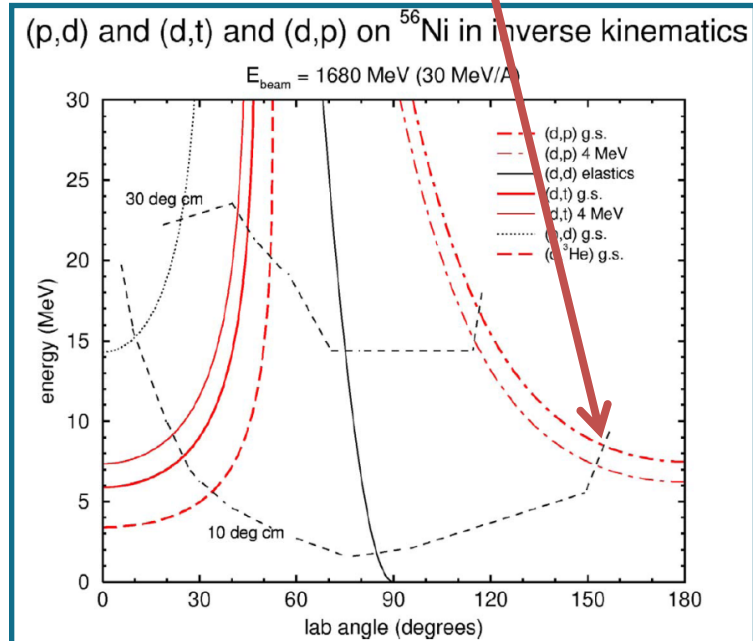
- mainly on the masses of the light particles
- not so much on beam mass or velocity



Exotic nuclei: inverse kinematics

source: Wilton Catford

- Most particles at 90 deg but maximum of cross sections at forward and backward angles
- Kinematic compression: very small differences in energy of the light particle for different E^*

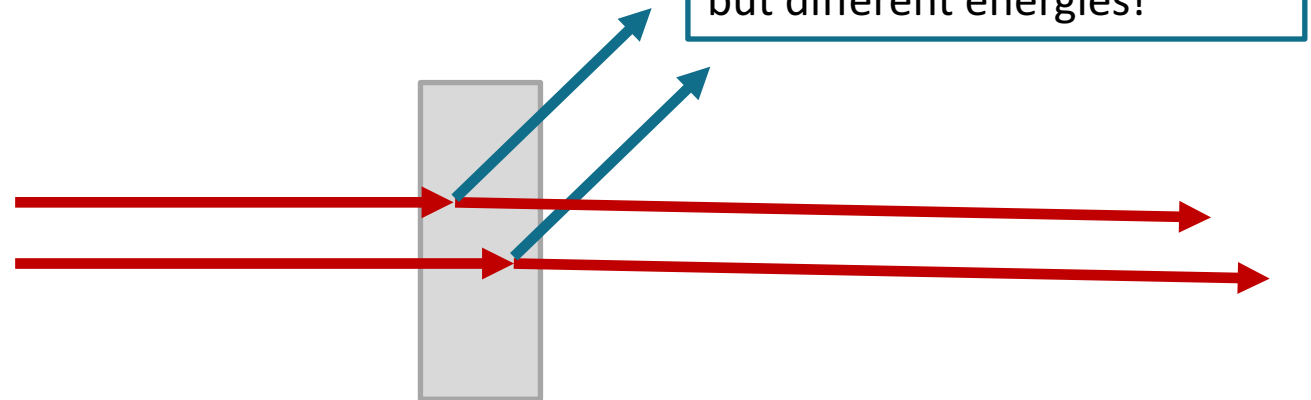


The luminosity dilemma

- We have weak beams
→ we could increase the target thickness

but

- We do not know the energy of the beam at the interaction point



- Limit for (d,p):
resolution in $E^* \approx 300$ keV
for $\approx 200 \mu\text{g}/\text{cm}^2$ target
(depends on many factors!!)

Limits in resolution

Resolution in E^*

- Light beam:
better detect
beam-like particle
(limit on angular
resolution)
- Heavier beam:
better detect light
recoil (limit on
E resolution from
energy loss in the
target)
- In general:
much worse than
direct kinematics

152

J.S. Winfield et al. / Nucl. Instr. and Meth. in Phys. Res. A 396 (1997) 147–164

Table 2

Major contributions in keV to the resolution of the excitation energy spectra of single neutron stripping and pickup reactions in inverse kinematics, where the heavy ion is detected in a spectrometer. The detection angle corresponds to 10°_{cm} . The last column is an approximate estimate as a sum in quadrature of the net effect of five non-Gaussian contributions. Other symbols are explained in the text

Reaction	E_i/A (MeV)	θ_{lab}	Origin of contribution					Σ_{quad}
			$\Delta\theta$	Δp	E_{stragg}	$\Theta_{1/2}$	dE/dx	
$p(^{12}\text{Be}, ^{11}\text{Be})d$	30	1.07°	172	147	101	74	23	259
$p(^{12}\text{Be}, ^{11}\text{Be})d$	15	1.06°	84	71	99	74	37	169
$p(^{77}\text{Kr}, ^{76}\text{Kr})d$	30	0.16°	1404	811	808	723	56	1952
$p(^{77}\text{Kr}, ^{76}\text{Kr})d$	10	0.10°	334	143	502	570	268	883
$d(^{76}\text{Kr}, ^{77}\text{Kr})p$	10	0.21°	1140	614	2177	1859	1321	3408

Table 3

Major contributions in keV to the resolution of the excitation energy spectra of single neutron pickup and stripping reactions in inverse kinematics, where the light particle is detected in a silicon detector. Symbols as described in text and Table 2

Reaction	E_i/A (MeV)	θ_{lab}	Origin of contribution				Σ_{quad}
			$\Delta\theta$	ΔE_f	ΔE_i	dE/dx	
$p(^{12}\text{Be}, d)^{11}\text{Be}$	30	19.0°	136	74	114	649	685
$p(^{12}\text{Be}, d)^{11}\text{Be}$	15	17.8°	66	72	55	984	995
$p(^{77}\text{Kr}, d)^{76}\text{Kr}$	30	15.0°	124	55	64	186	249
$p(^{77}\text{Kr}, d)^{76}\text{Kr}$	10	6.0°	26	24	23	775	777
$d(^{76}\text{Kr}, p)^{77}\text{Kr}$	10	155.3°	52	93	37	1309	1316

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Lecture 2/3

Contents

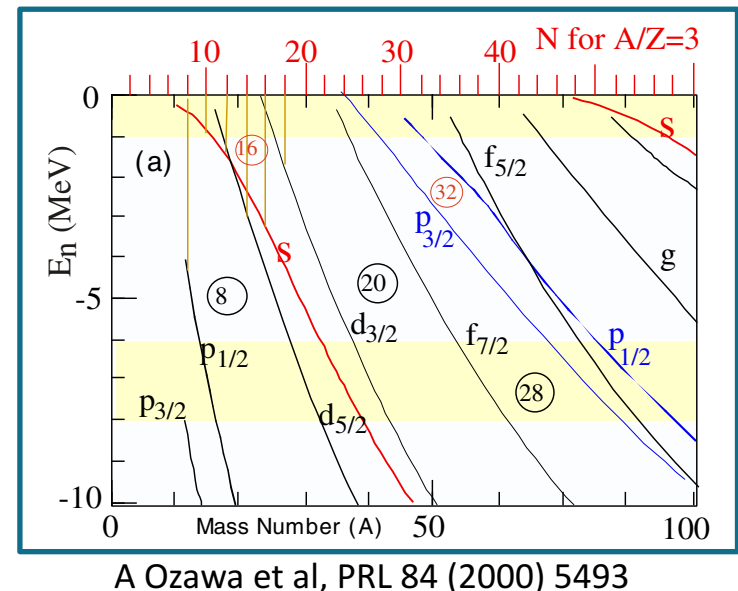
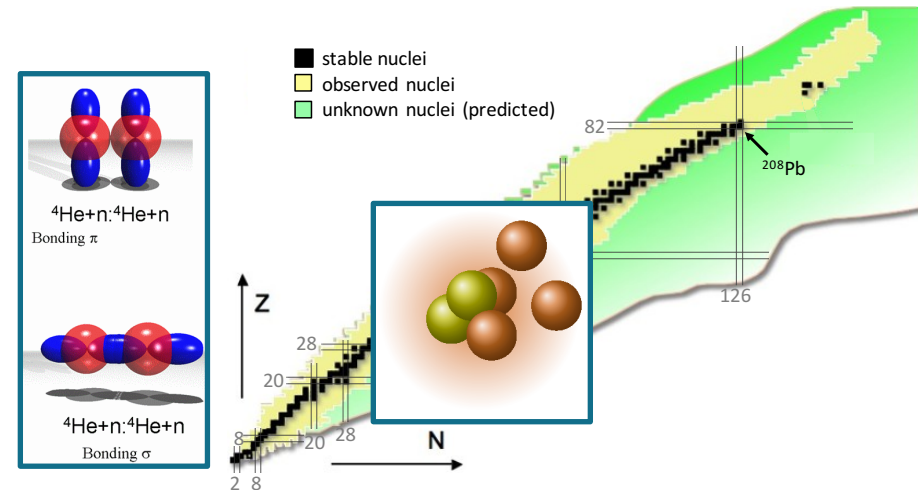
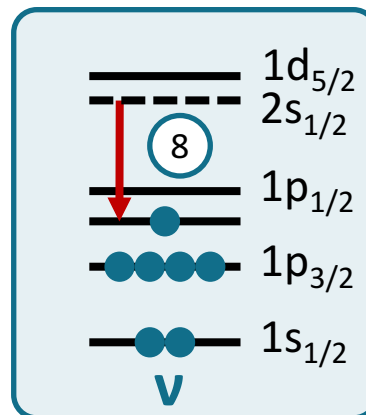
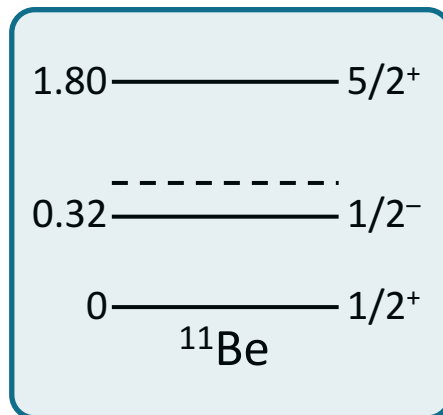
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 - **Light nuclei, $N=8$**
 - The emergence of $N=16$
 - The spin-orbit term
 - Mg and Ni, the 0^+ s
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Light nuclei

- Halo structures
- Clustering and deformation

Disappearance of N=8

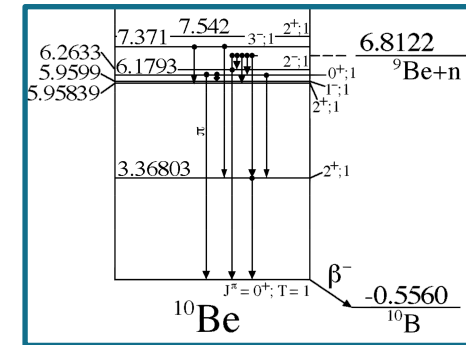
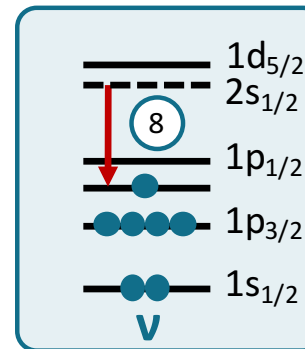
- Ground state in ^{15}C
Inversion of levels in ^{11}Be
- Due to proton-neutron interaction and the removal of protons
I. Talmi and I. Unna PRL 4 (1960) 469
- Cause of the halo in ^{11}Li , ^{11}Be , ^{14}Be



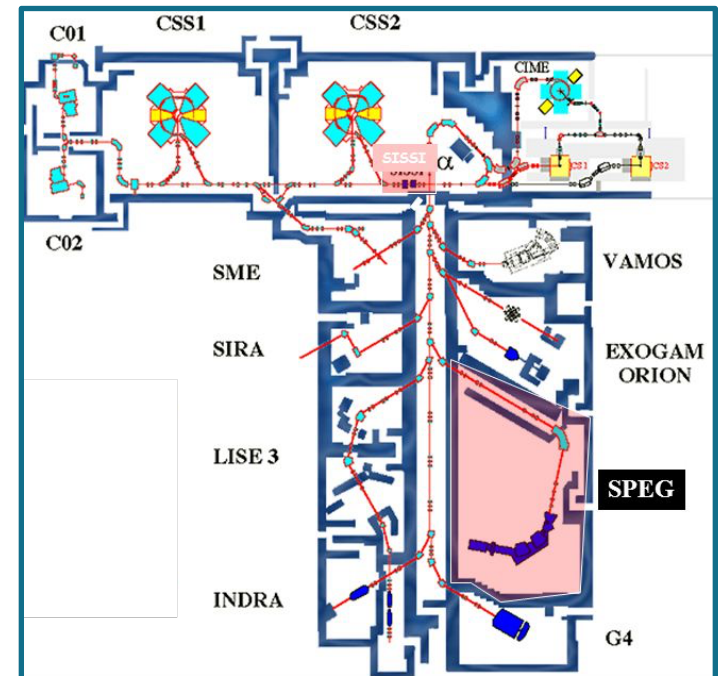
Light nuclei – I

Ground state of ^{11}Be

- $[0^+ \otimes 2s]_{1/2+}$ or $[2^+ \otimes 1d]_{1/2+}$?
“ ^{10}Be core” configuration in ^{11}Be ?
 - 2^+ in ^{10}Be at 3.34 MeV
- Probe overlap between ^{11}Be gs and ^{10}Be $0^+/2^+$ states



- **Experiment:** $^{11}\text{Be}(p,d)^{10}\text{Be}$ at GANIL
 - Primary beam ^{15}N 65 MeV/nucleon
 - In-flight fragment separation in SISSI/alpha
→ ^{11}Be at 35.3 MeV/nucleon
 - Detection in SPEG

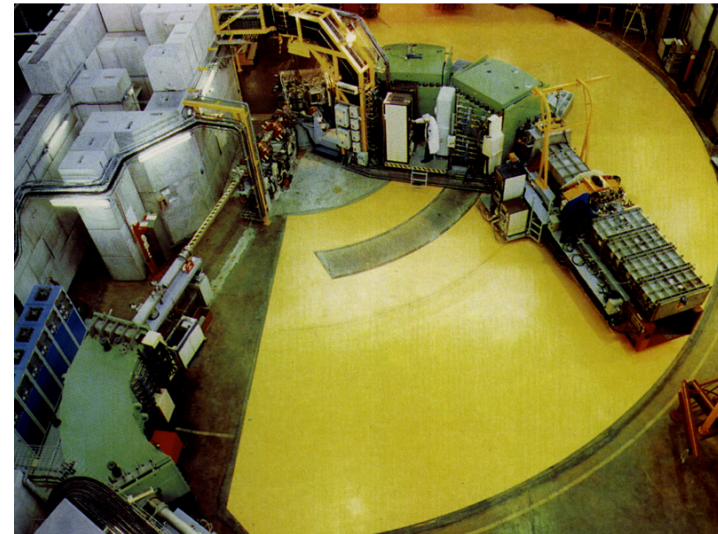
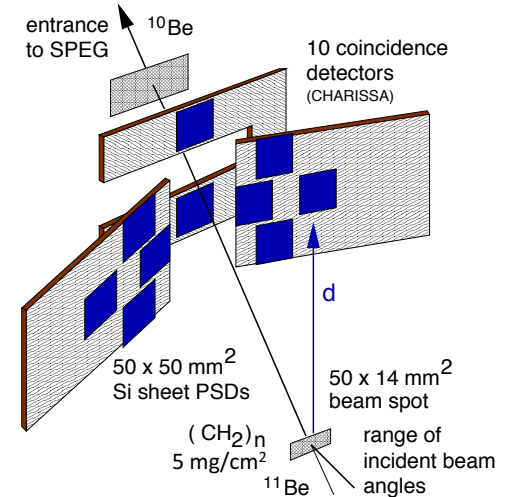
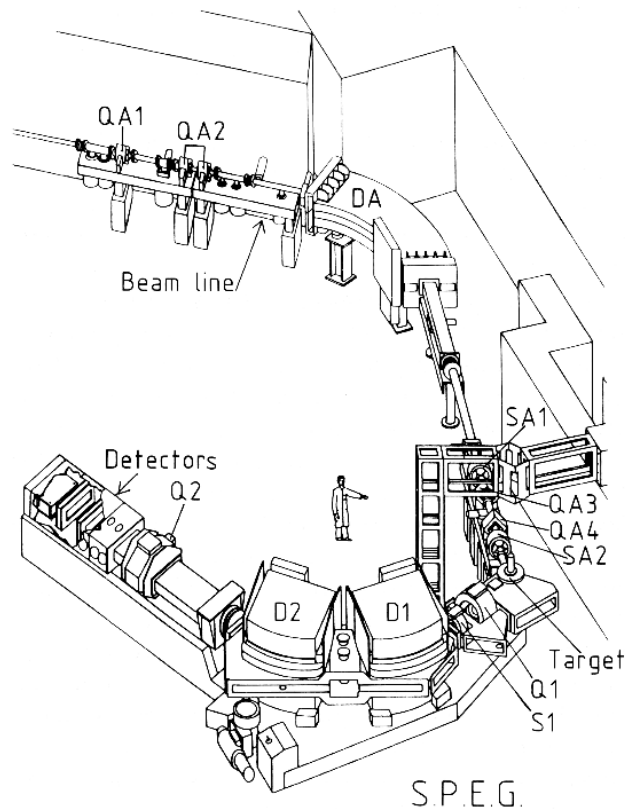


Light nuclei – I

Ground state of ^{11}Be

Experiment: $^{11}\text{Be}(p,d)^{10}\text{Be}$

- d in CHARISSA: particle detectors (resistive)
- ^{10}Be SPEG: (dispersion-matched) spectrometer

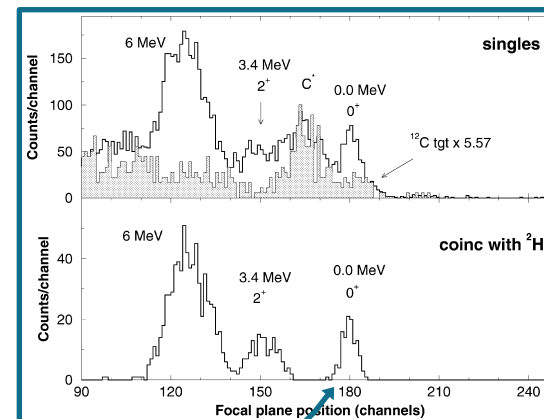
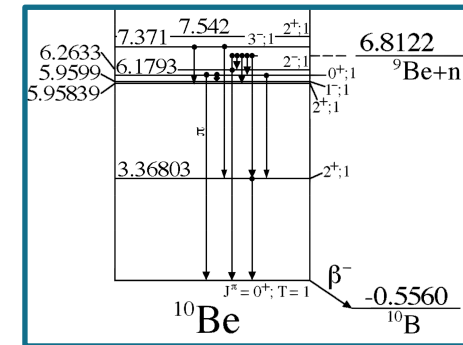
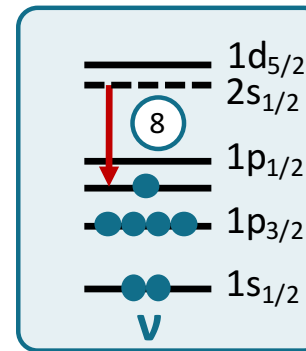


Light nuclei – I

Ground state of ^{11}Be

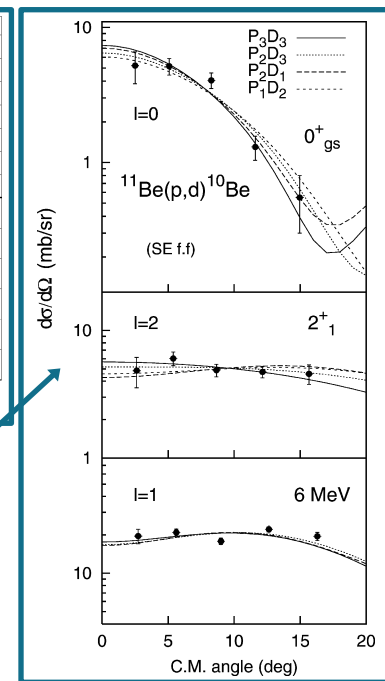
Experiment: $^{11}\text{Be}(p,d)^{10}\text{Be}$

- 0^+ state in ^{10}Be populated by removal of the $2s_{1/2}$ neutron
 \rightarrow assume pure $[0^+ \otimes 2s]_{1/2+}$ configuration, calculate $d\sigma/d\Omega$ for 0^+ and normalize \rightarrow SF for $[0^+ \otimes 2s]_{1/2+}$
- 2^+ state populated by removal of a $d_{5/2}$ neutron only possible if ^{11}Be gs contains the $[2^+ \otimes 1d]_{1/2+}$ configuration
 \rightarrow assume pure $[2^+ \otimes 1d]_{1/2+}$ configuration, calculate $d\sigma/d\Omega$ for 2^+ and normalize \rightarrow SF for $[2^+ \otimes 1d]_{1/2+}$



resolution ≈ 700 keV

different optical model potentials



Light nuclei – I

Ground state of ^{11}Be

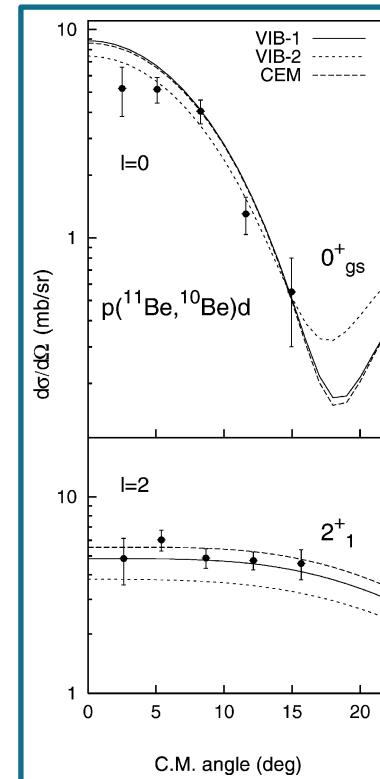
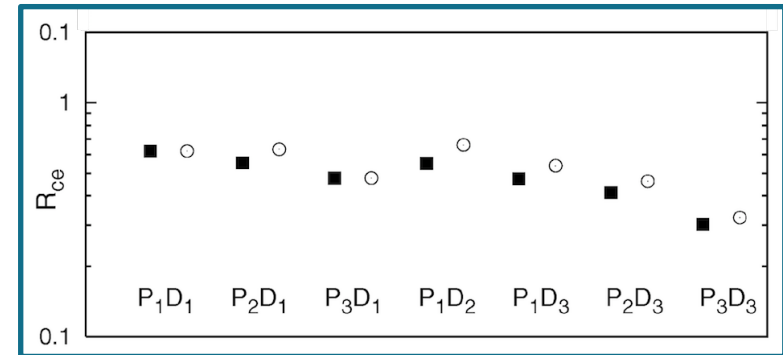
Experiment: $^{11}\text{Be}(p,d)^{10}\text{Be}$

- Caution: how to build the $[0^+ \otimes 2s]_{1/2+}$ and $[2^+ \otimes 1d]_{1/2+}$ configurations?
- Assume ^{10}Be inert and bind the neutron with a Woods-Saxon potential

Result: $SF(0^+) \leq 70\%$, $SF(2^+) \geq 30\%$

- Take into account the large deformation of ^{10}Be in the 2^+ state (solve coupled-channel problem)

Result: $SF(0^+) = 84\%$, $SF(2^+) = 16\%$



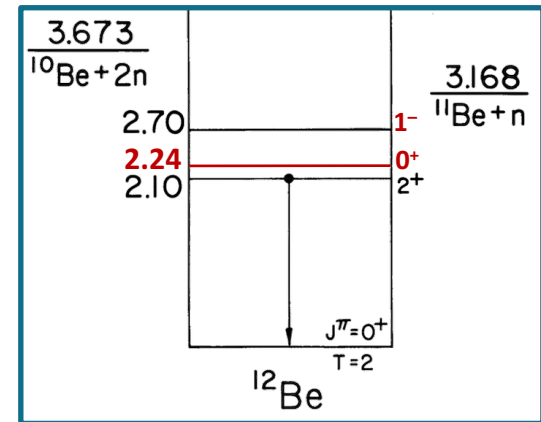
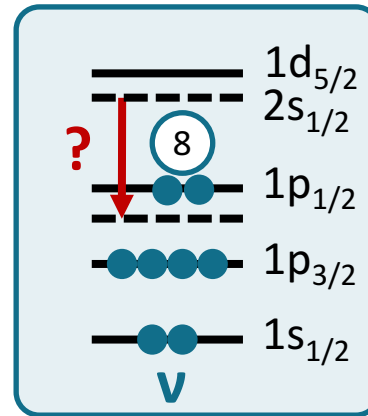
no normalisation

Light nuclei – II

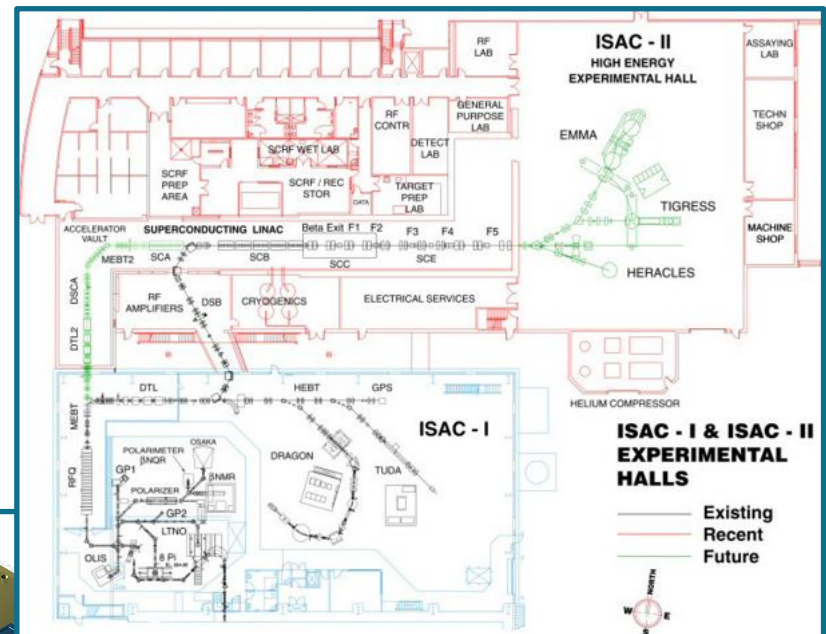
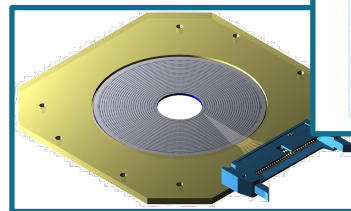
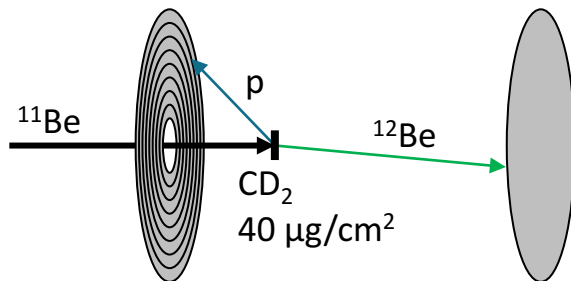
R Kanungo et al, PLB 682 (2010) 391

Structure of states in ^{12}Be

- What is the content of $v(s_{1/2})^2$ in the 0^+ states of ^{12}Be ?
- Also measured in knock-out reactions – but those cannot separate 0^+_1 and 0^+_2



- **Experiment:** $^{11}\text{Be}(d,p)^{12}\text{Be}$ at TRIUMF
 - ISOL production
 - Post-acceleration to 5 MeV/nucleon



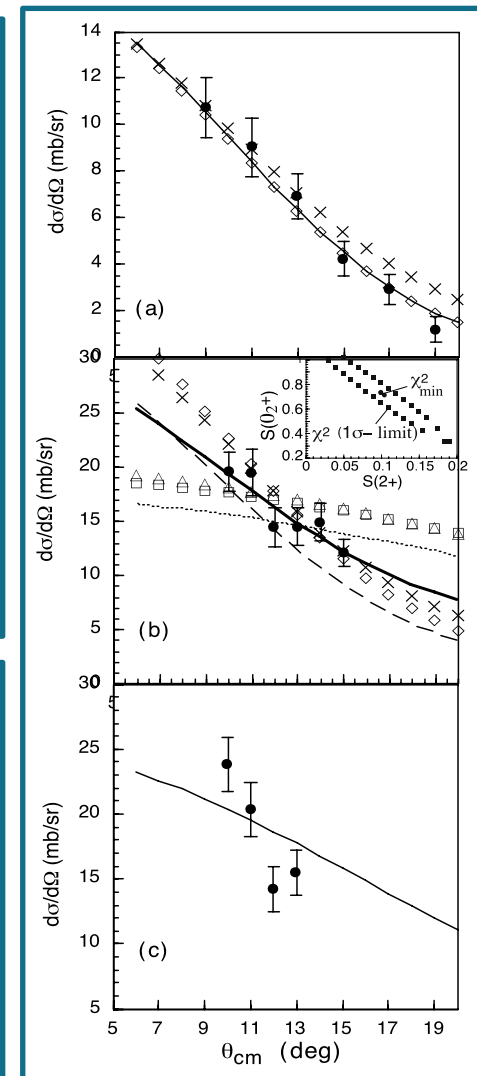
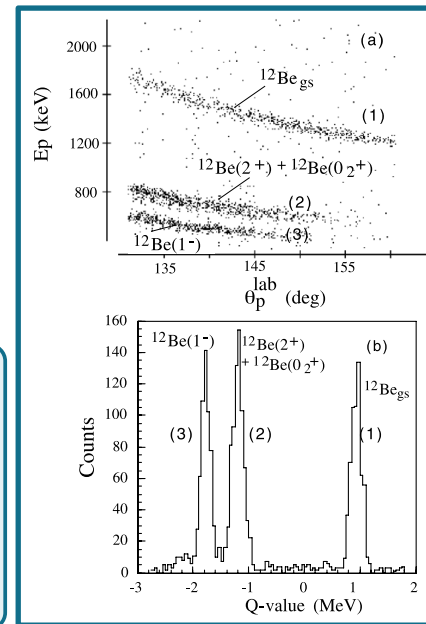
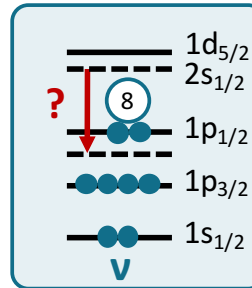
Light nuclei – II

R Kanungo et al, PLB 682 (2010) 391

Structure of states in ^{12}Be

Experiment: $^{11}\text{Be}(d,p)^{12}\text{Be}$

- Transfer to all bound states is observed
 0^+_1 and $0^+_2 \rightarrow$ neutron to $2s_{1/2}$
 $2^+ \rightarrow$ neutron to $1d_{5/2}$
 $1^- \rightarrow$ neutron to $1p_{1/2}$
- Doublet fitted with a sum of the two configurations

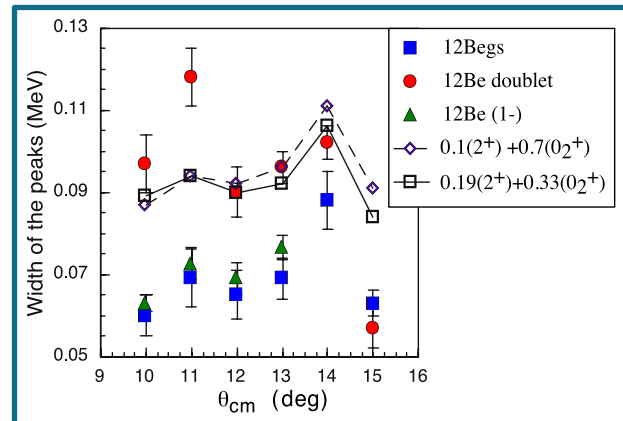


Content of s-wave neutron:

$$0^+_1 : 0.28^{+0.03}_{-0.07}$$

$$0^+_2 : 0.73^{+0.27}_{-0.40}$$

The 0^+_2 is probably a halo state



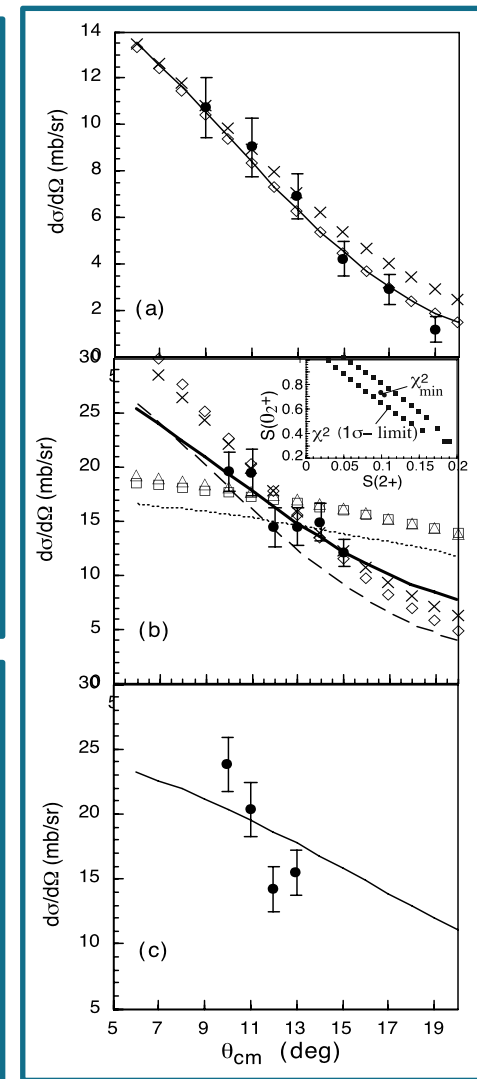
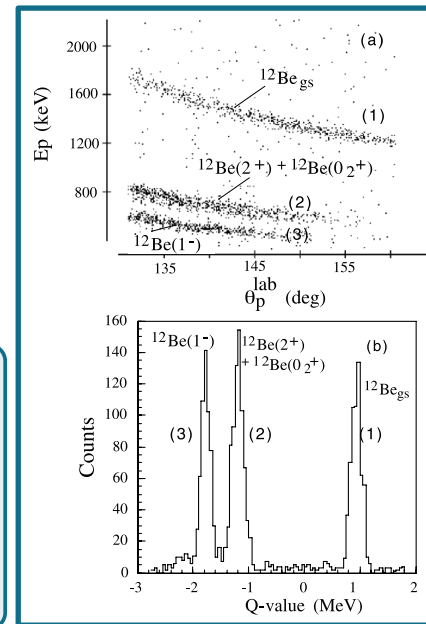
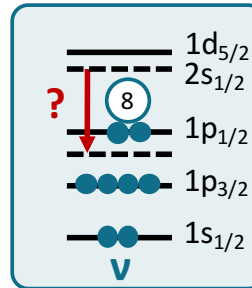
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R Kanungo et al, PLB 682 (2010) 391

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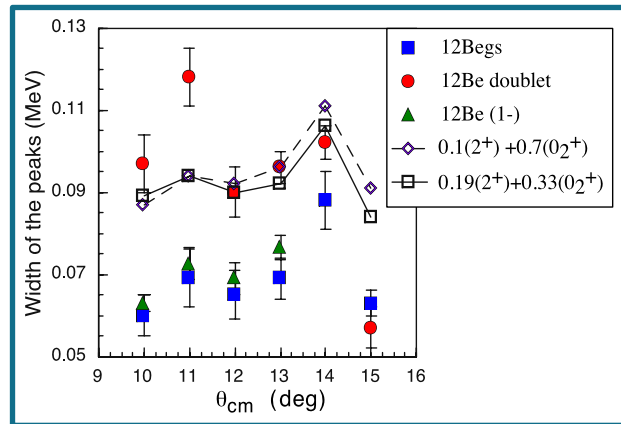


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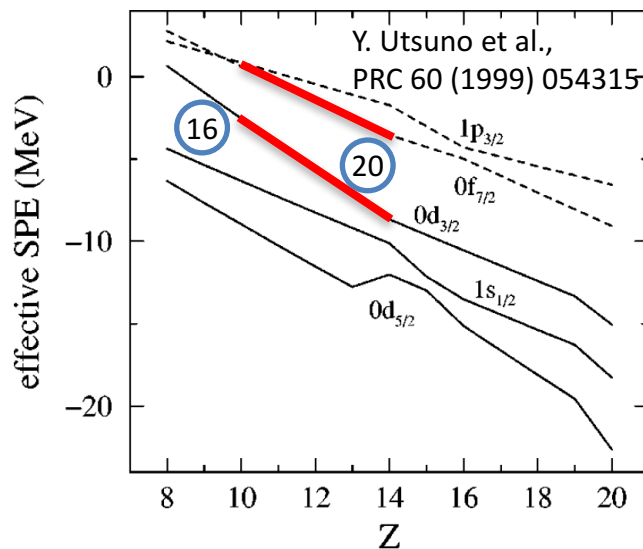
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 - **The emergence of $N=16$**
 - The spin-orbit term
 - Mg and Ni, the 0^+ s
 - Ni region
 - ...

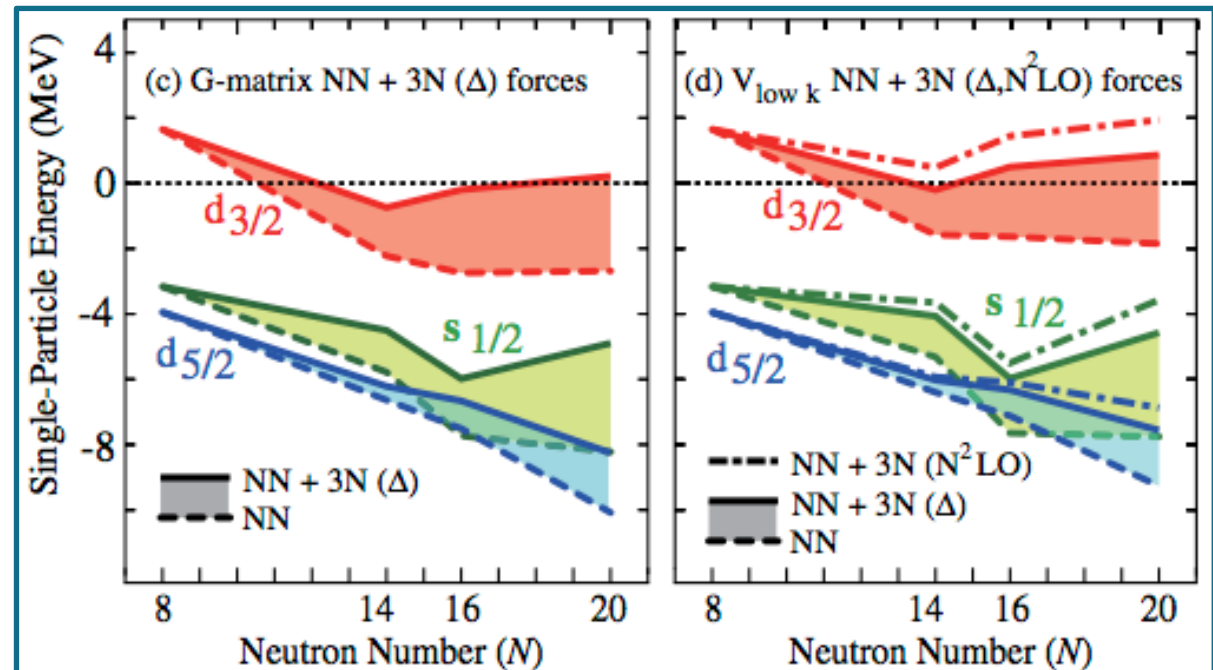
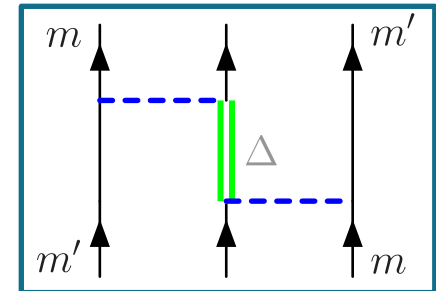
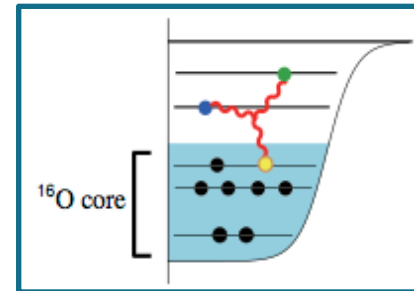
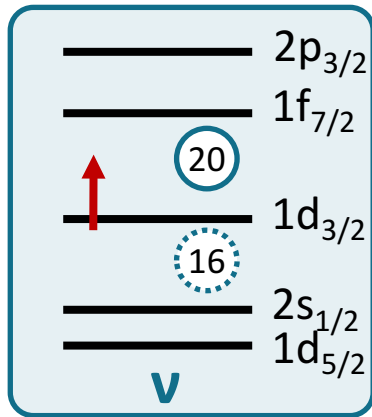
- Historically this was the first identification of shell evolution far from stability (mid-'70)

[illegible]

The emergence of N=16

- 3-body forces in O isotopes

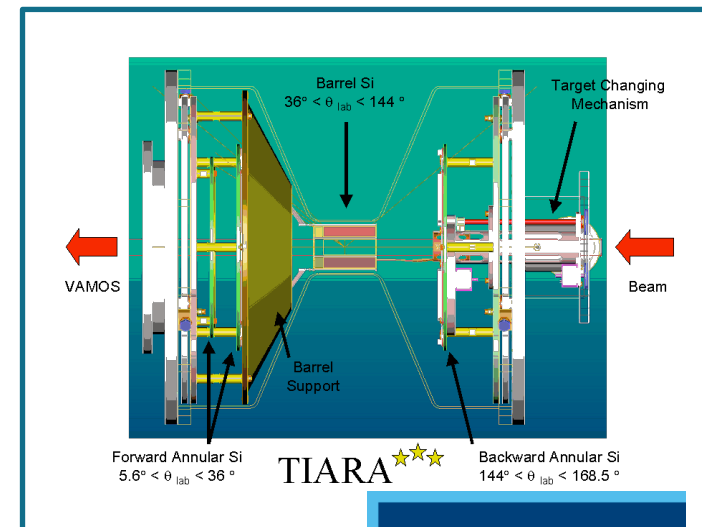
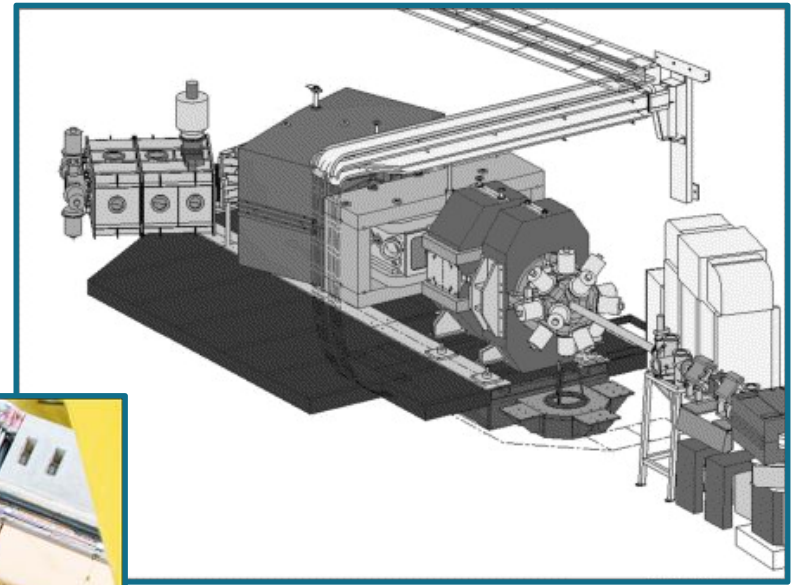
T Otsuka et al, PRL 105 (2010) 032501



(d,p) on Ne and Na isotopes

At GANIL (SPIRAL)

- TIARA charged-particle detectors
- EXOGAM γ -ray array
- VAMOS spectrometer

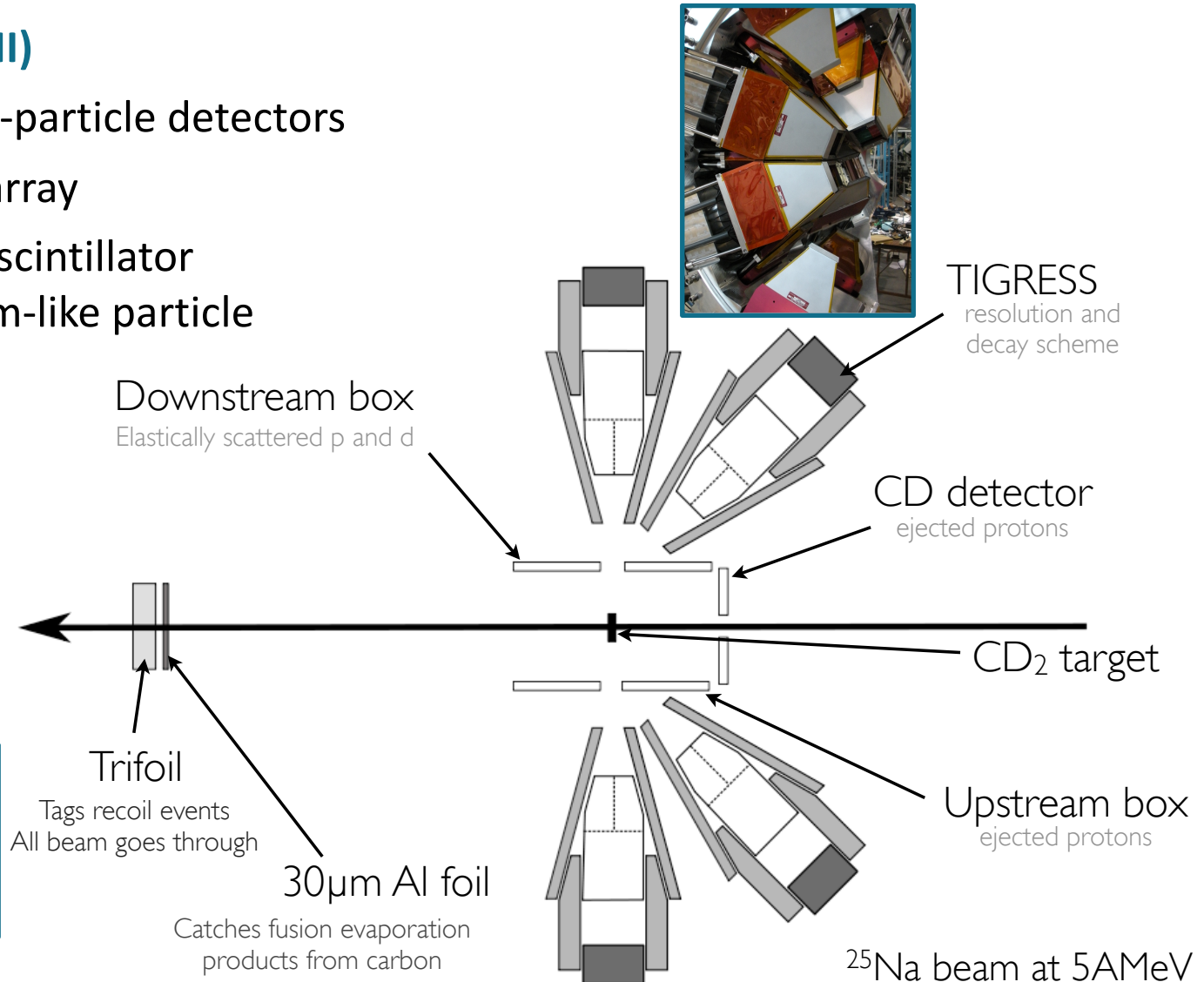


(d,p) on Ne and Na isotopes

GL Wilson et al, PLB 759 (2016) 417

At TRIUMF (ISAC-II)

- SHARC charged-particle detectors
- TIGRESS γ -ray array
- TRIFOIL plastic scintillator to identify beam-like particle

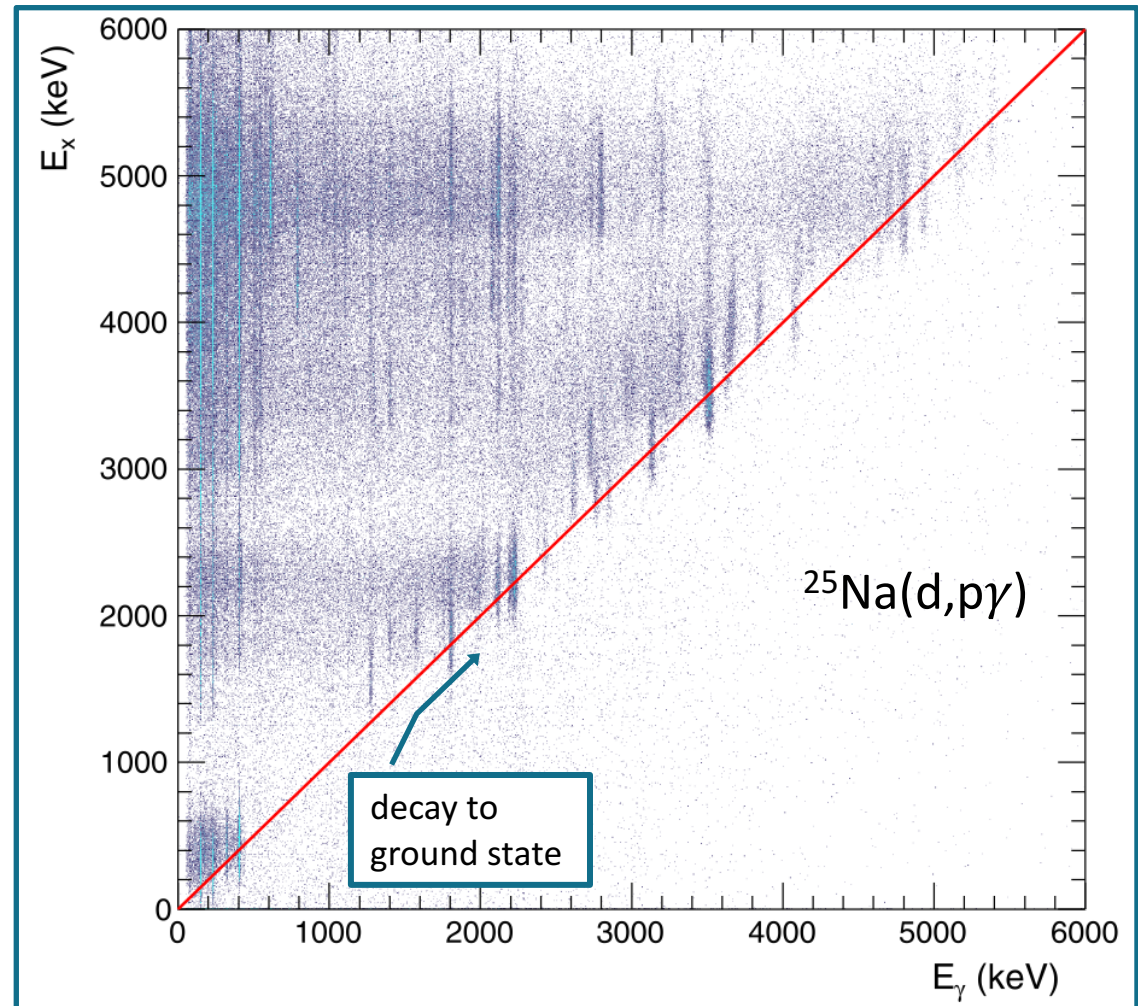


(d,p) on Ne and Na isotopes

GL Wilson et al, PLB 759 (2016) 417

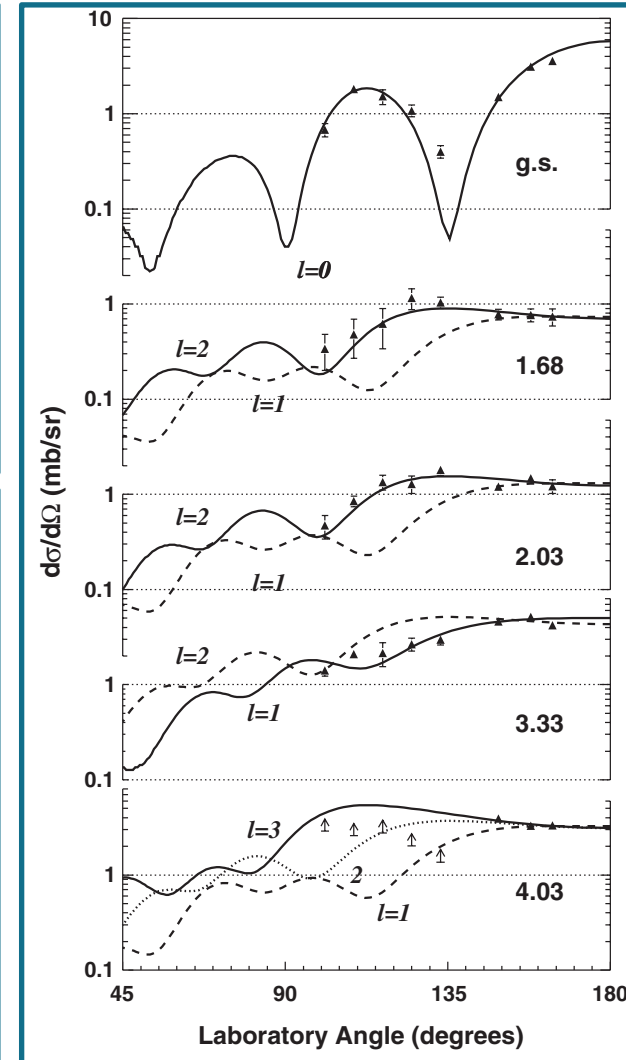
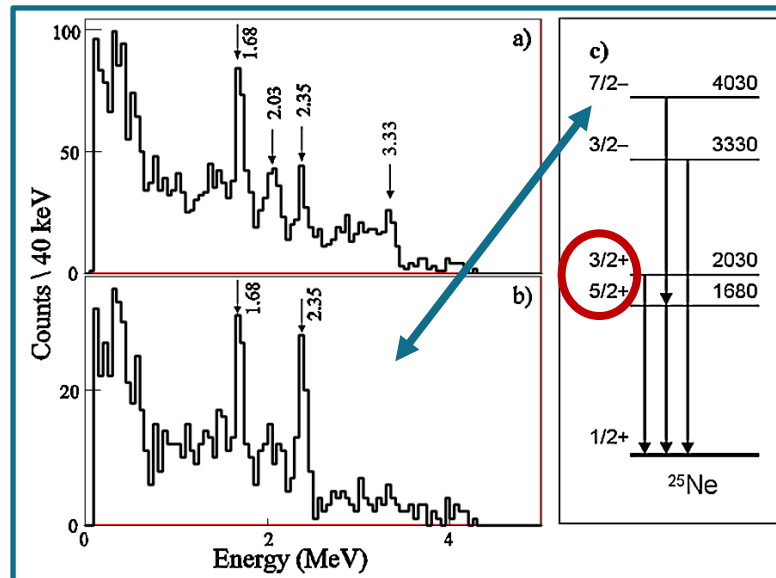
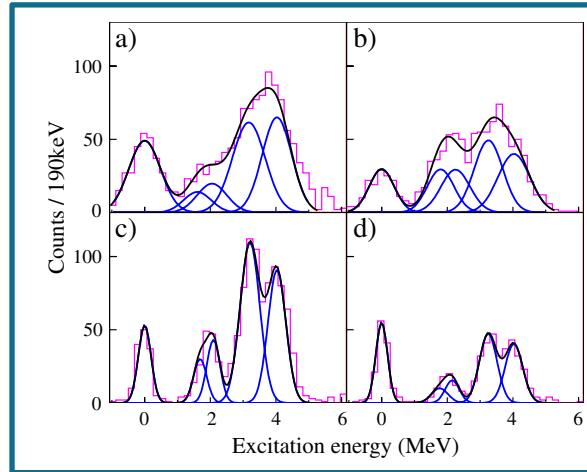
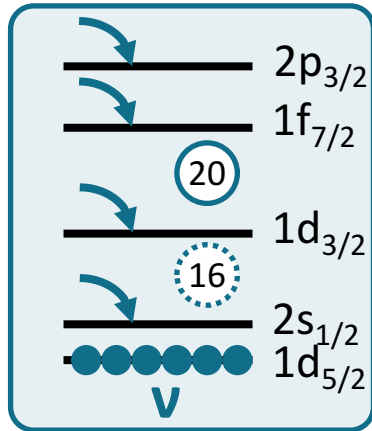
Conditions

- Populated state decays promptly
- Angular resolution for Doppler correction



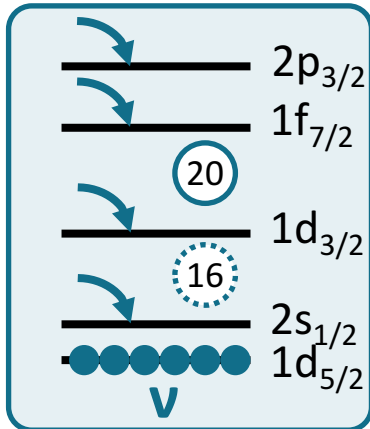
(d,p) on Ne and Na isotopes

W Catford et al, PRL 104 (2010) 192501

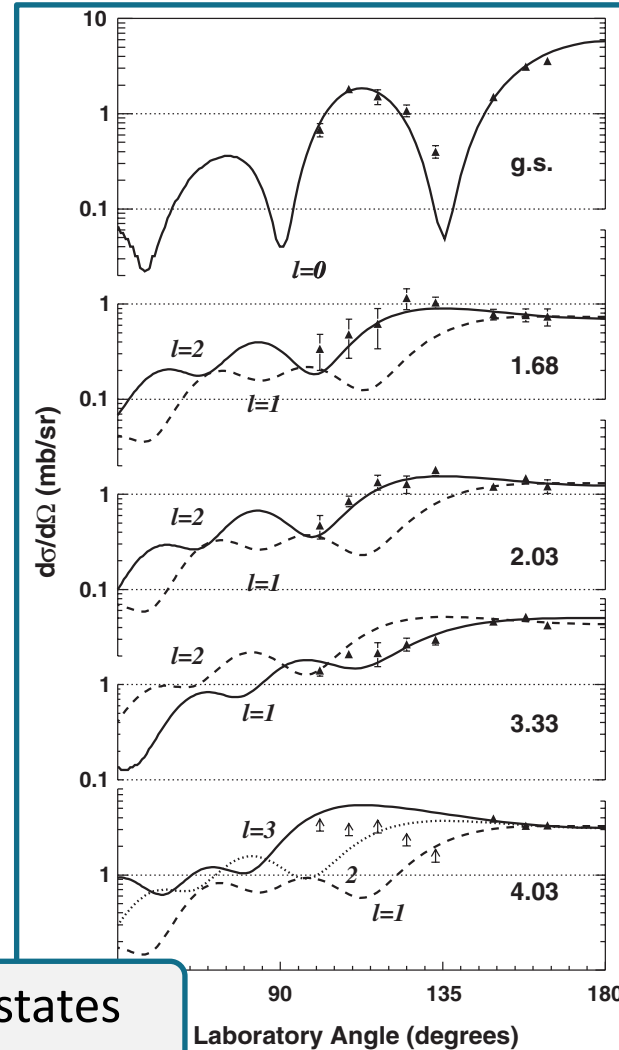
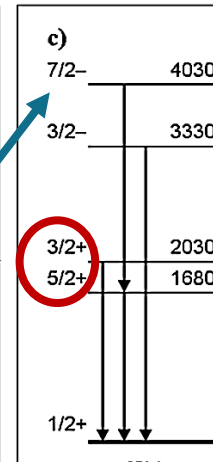
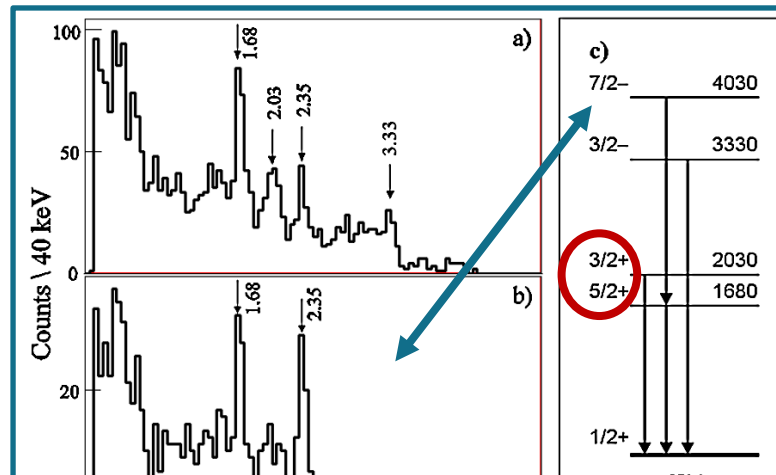
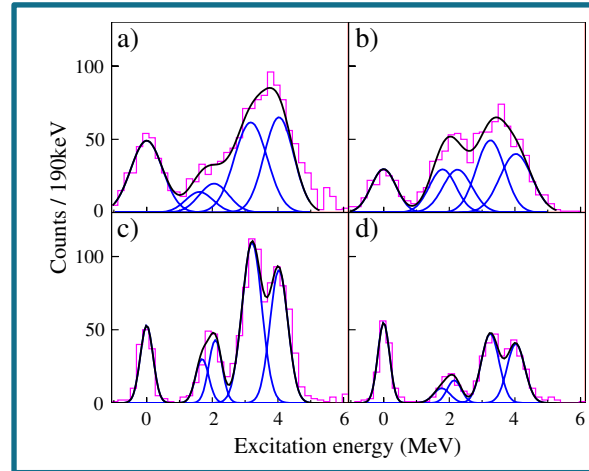
 $^{24}\text{Ne}(d,p)$


(d,p) on Ne and Na isotopes

W Catford et al, PRL 104 (2010) 192501

 $^{24}\text{Ne}(d,p)$ 

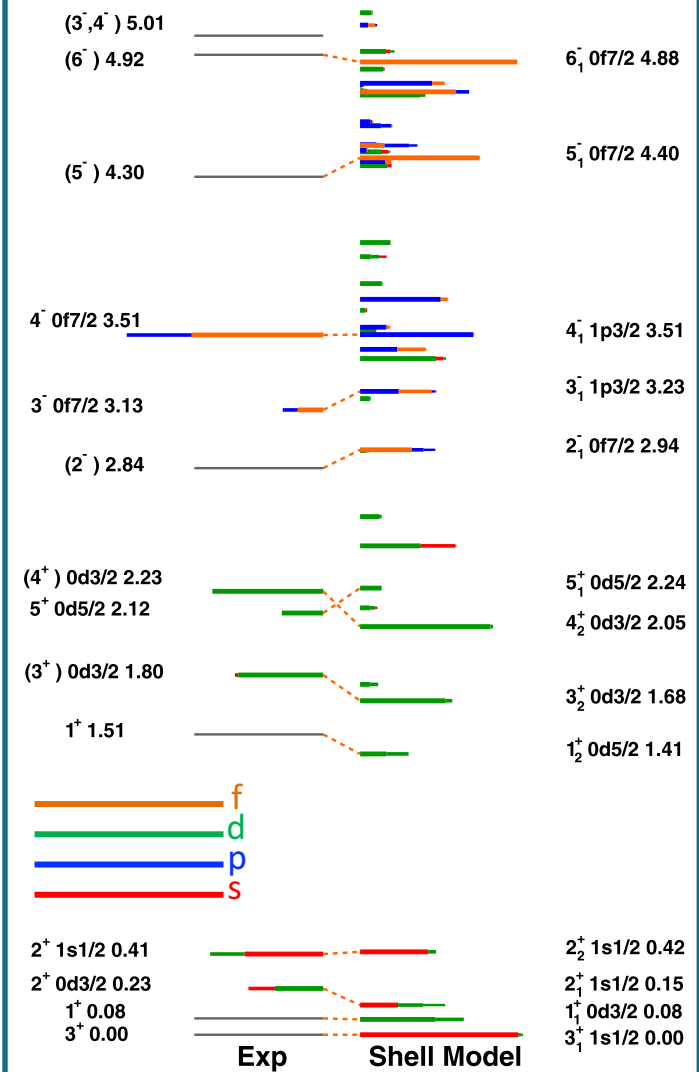
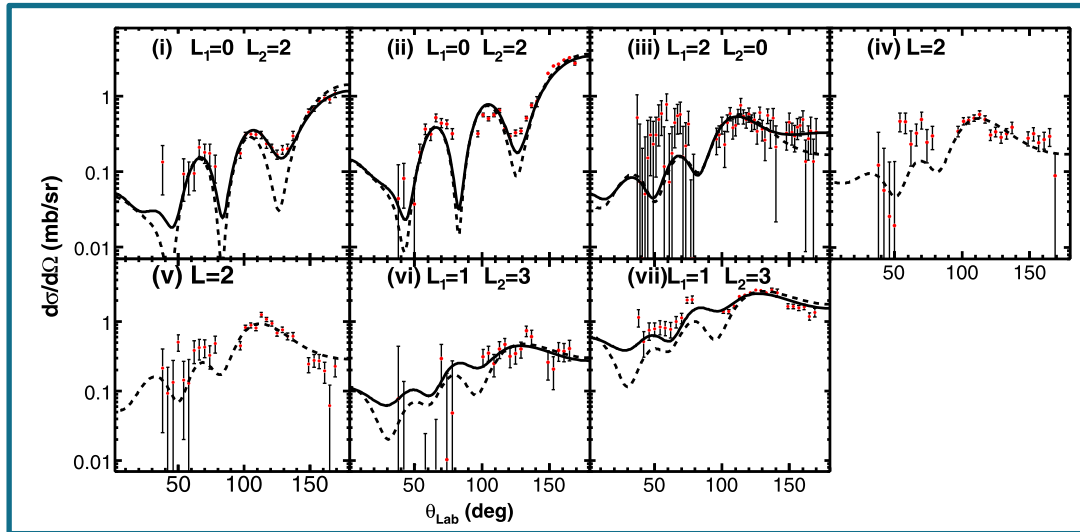
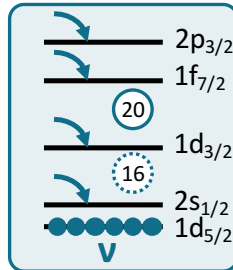
$$\begin{aligned} \text{SF}(1/2^+) &= 0.80 \\ \text{SF}(5/2^+) &= 0.15 \\ \text{SF}(3/2^+) &= 0.44 \\ \text{SF}(3/2^-) &= 0.75 \\ \text{SF}(7/2^-) &= 0.80 \end{aligned}$$



- Firm assignment of the spin of the first two excited states
- Raise of the $3/2^+$ (≈ 1 MeV) with respect to the $5/2^+$ compared to ^{27}Mg

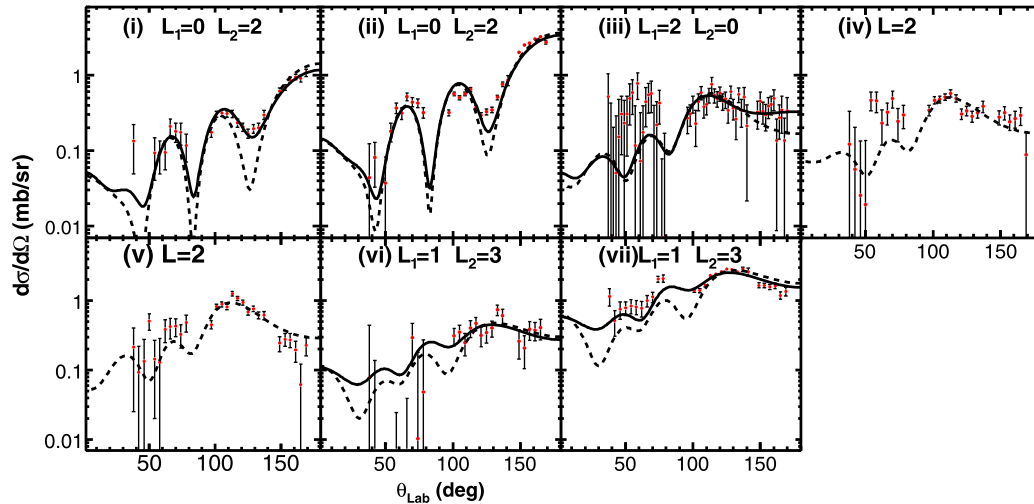
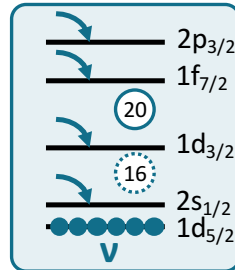
(d,p) on Ne and Na isotopes

GL Wilson et al, PLB 759 (2016) 417

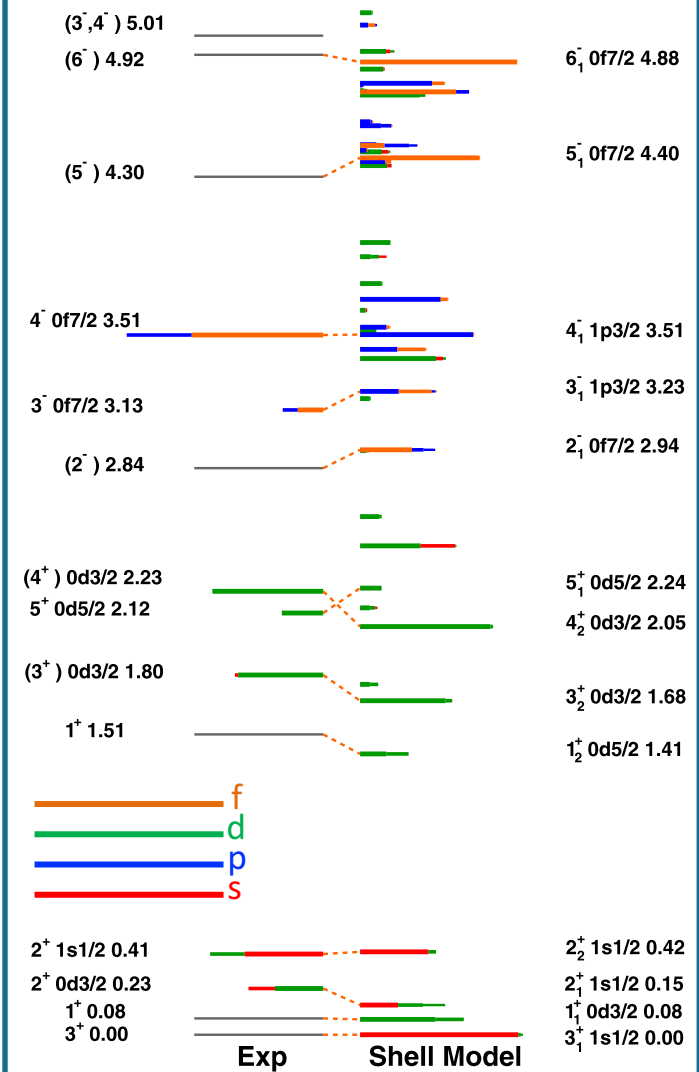
 $^{25}\text{Na}(d,p)$ 

(d,p) on Ne and Na isotopes

GL Wilson et al, PLB 759 (2016) 417

 $^{25}\text{Na}(d,p)$ 

- Important role of intruder configuration (negative parity states)
- Results reproduced by calculations with N=20 gap reduced by 700 keV

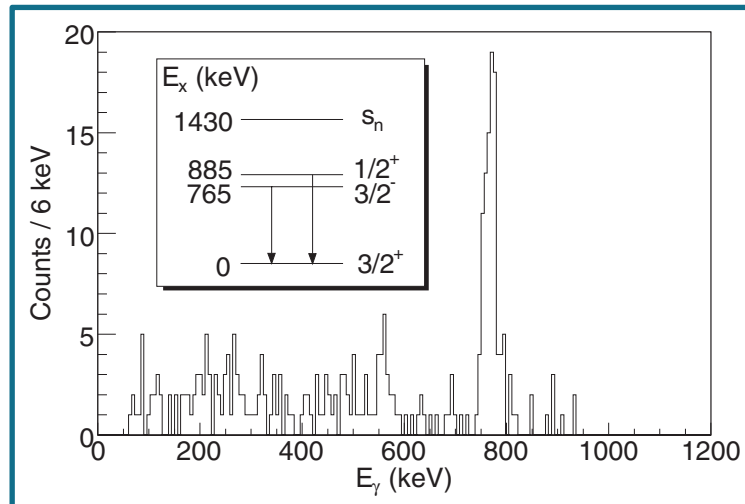
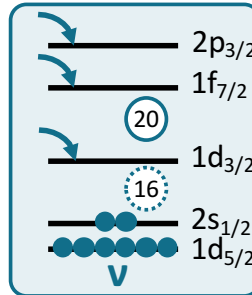
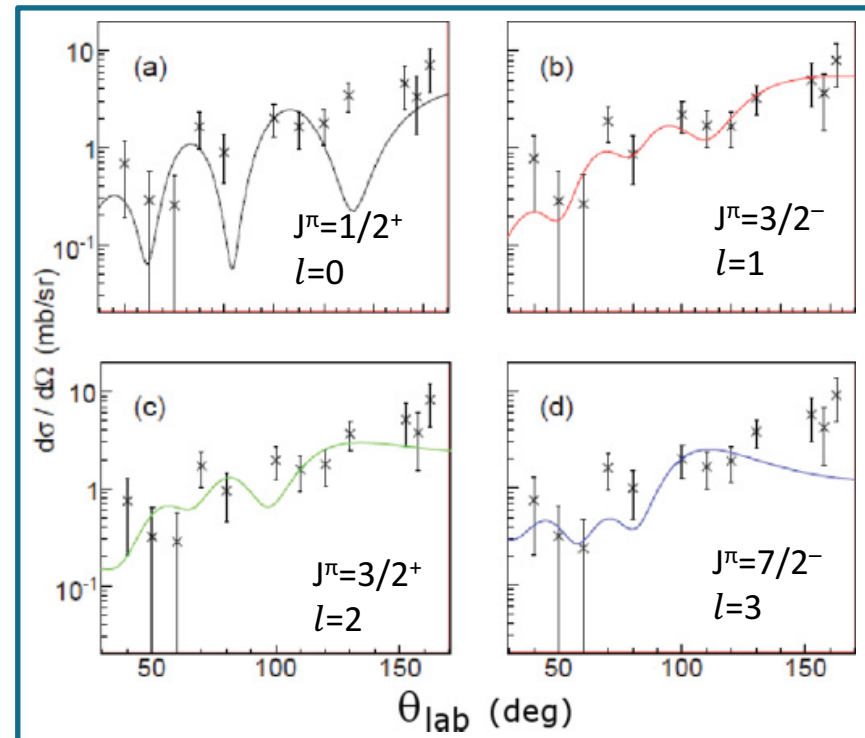
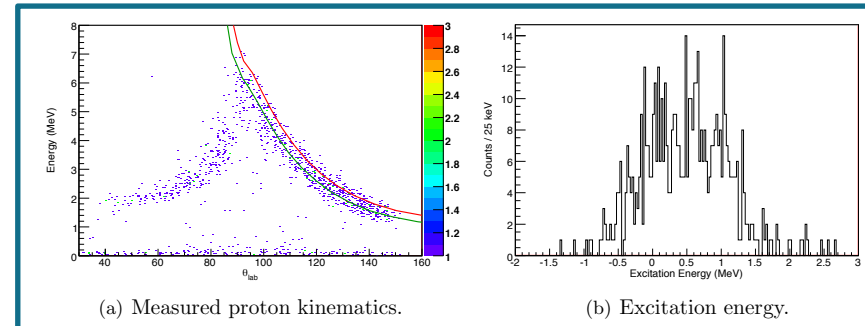


(d,p) on Ne and Na isotopes

M Brown et al, PRC 85 (2012) 011302(R)

$^{26}\text{Ne}(d,p)$

- Angular distributions: efficiency correction for coincidences as function of the spin
- Ground-state selection: $E^* < 200$ keV

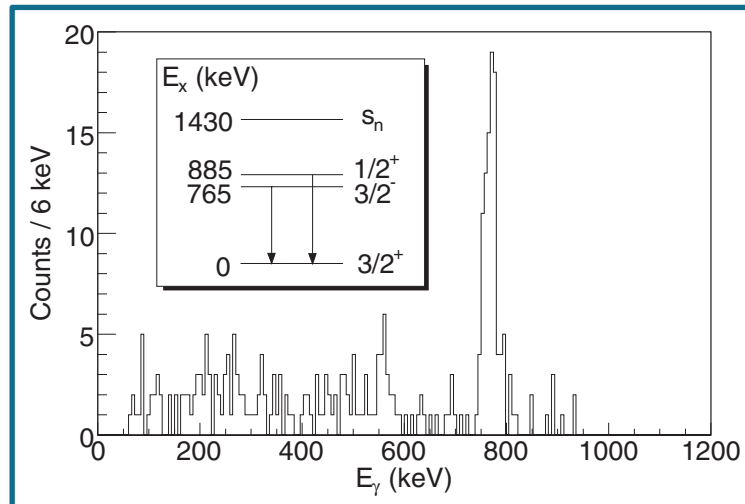
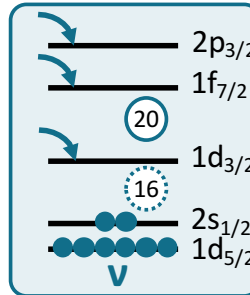
Very low $3/2^-$ intruder state

(d,p) on Ne and Na isotopes

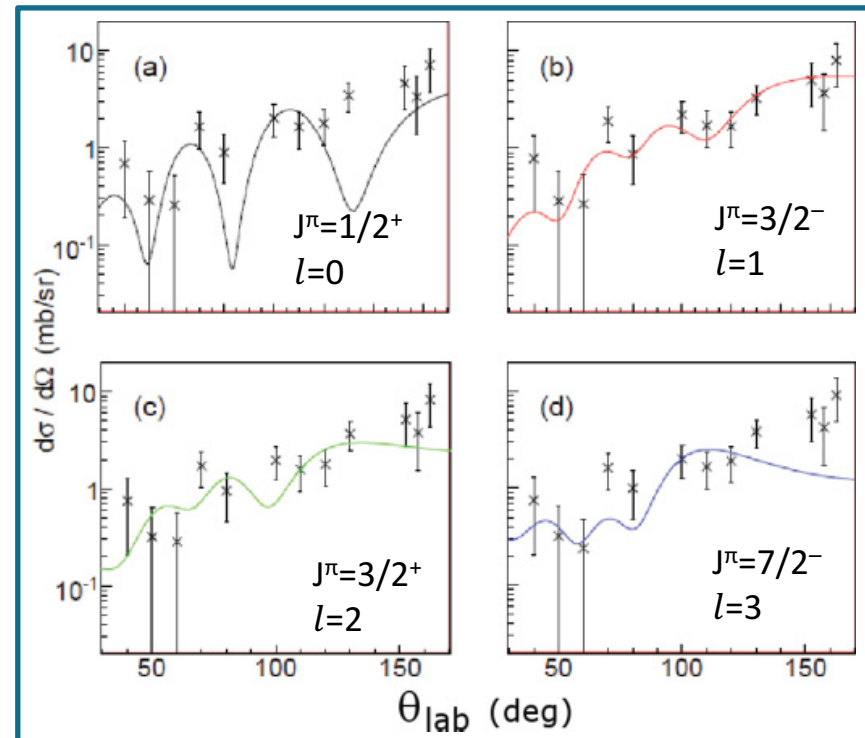
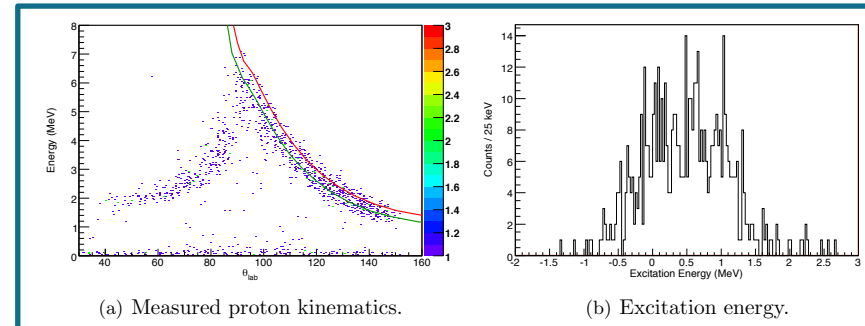
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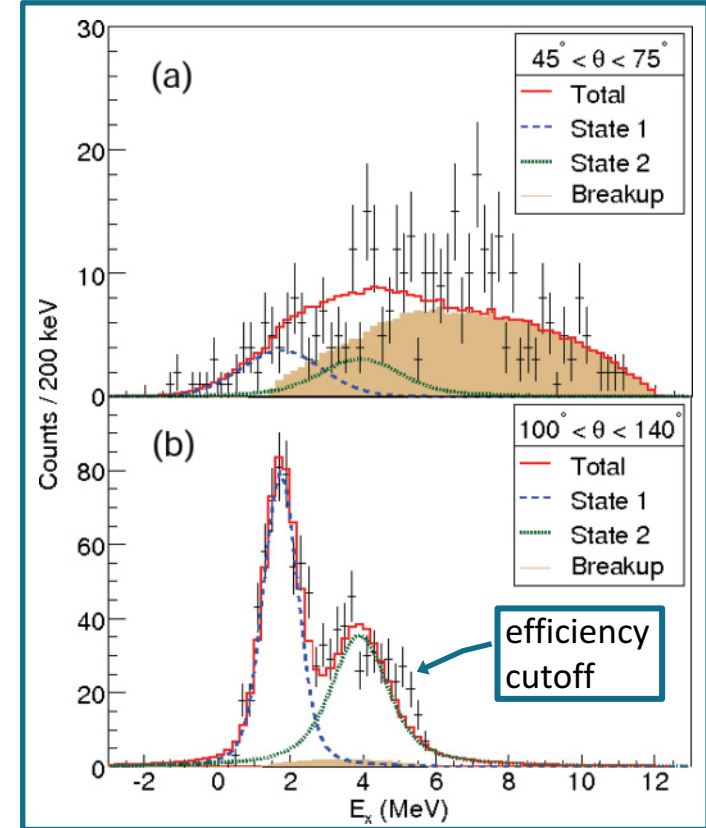
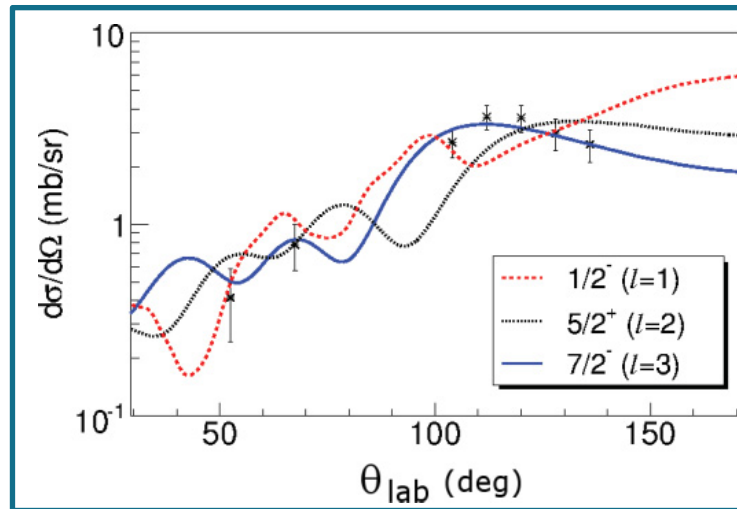
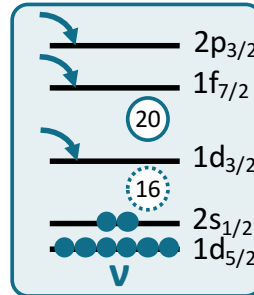


(d,p) on Ne and Na isotopes

M Brown et al, PRC 85 (2012) 011302(R)

$^{26}\text{Ne}(d,p)$

- Proton coincidences with ^{26}Na : transfer to unbound states

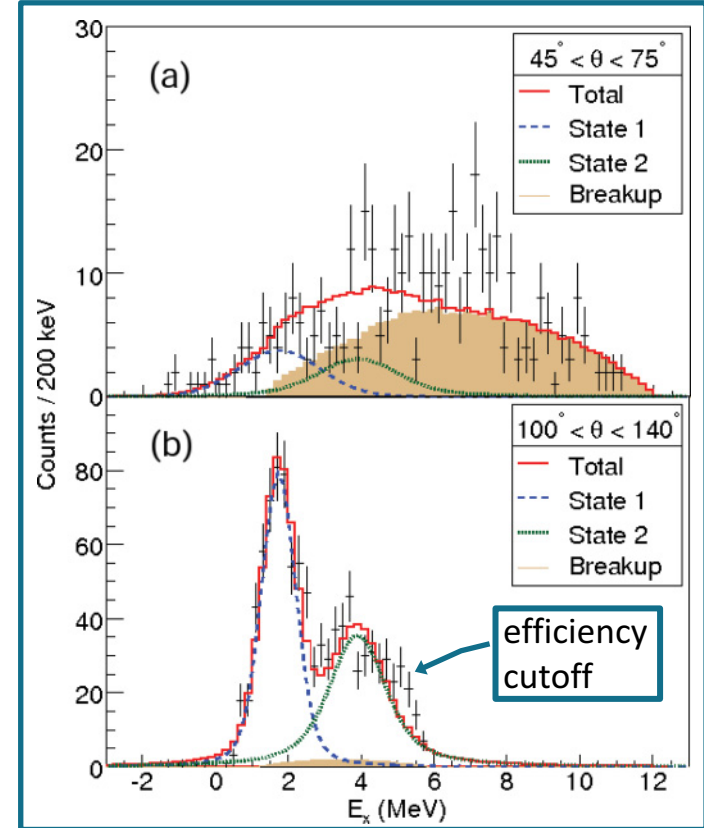
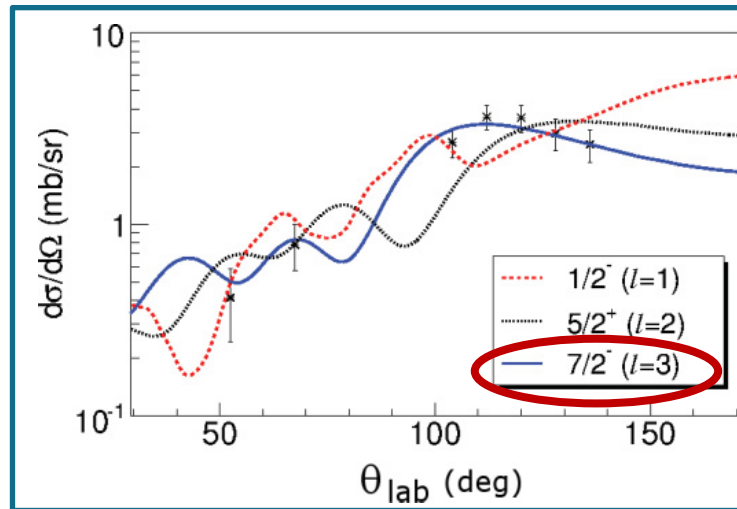
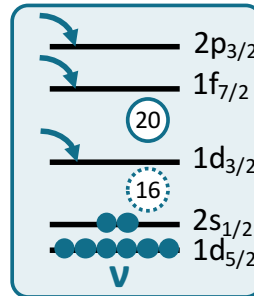


(d,p) on Ne and Na isotopes

M Brown et al, PRC 85 (2012) 011302(R)

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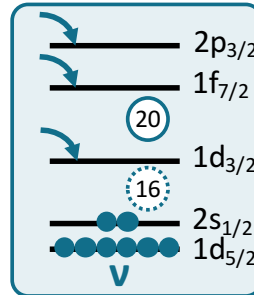


(d,p) on Ne and Na isotopes

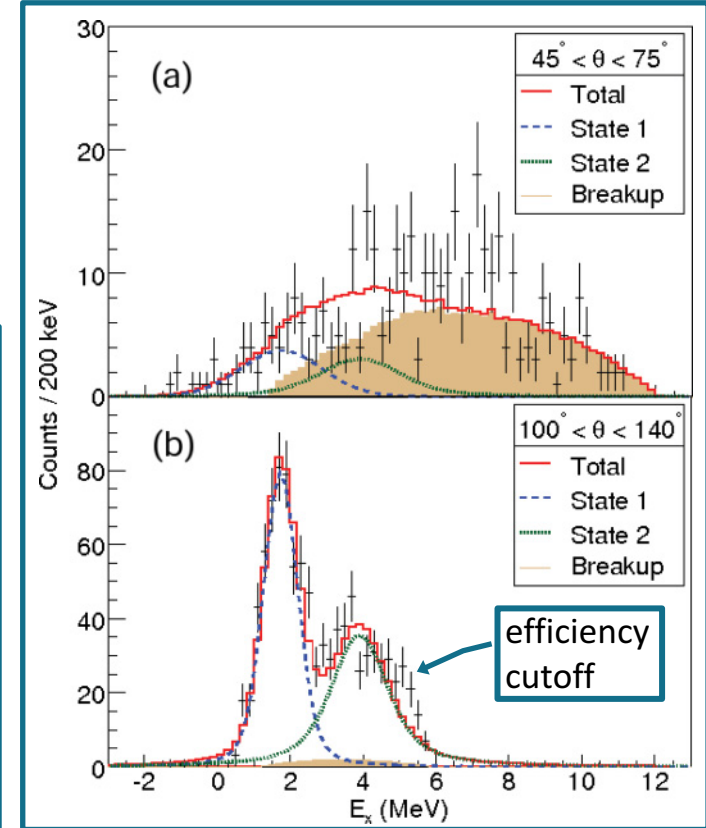
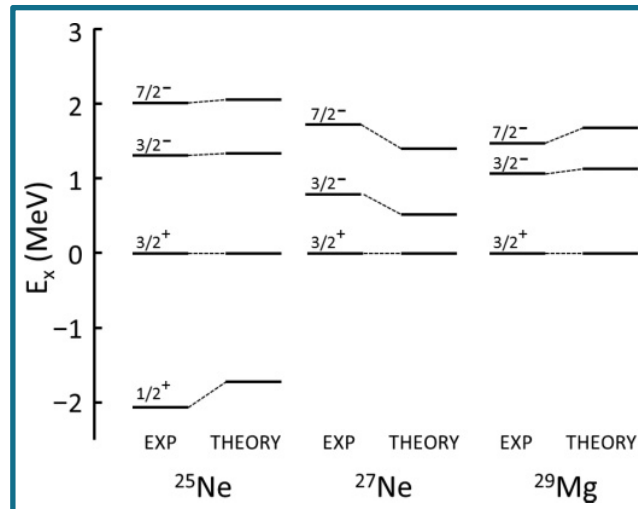
M Brown et al, PRC 85 (2012) 011302(R)

$^{26}\text{Ne}(d,p)$

- Proton coincidences with ^{26}Na : transfer to unbound states



$$\begin{aligned} \text{SF}(3/2^+) &= 0.42 \\ \text{SF}(3/2^-) &= 0.64 \\ \text{SF}(1/2^+) &= 0.17 \\ \text{SF}(7/2^-) &= 0.35 \end{aligned}$$



- Identification of intruder states $3/2^-$, $7/2^-$
- Results reproduced by calculations with N=20 gap reduced by 700 keV

Nucleon-Transfer Reactions with Radioactive Ion Beams

Riccardo Raabe
KU Leuven, Instituut voor Kern- en Stralingsfysica



International School of Physics
"Enrico Fermi"

14-19 July 2017

Nuclear Physics with Stable
and Radioactive Ion Beams

Lecture 3/3

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- Nuclear reactions
 - Types of reactions
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- Why use transfer reactions
 - Information from reactions
 - Q-value, angular momentum, spectroscopic factors
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 - Challenges: inverse kinematics
- **Case studies**
 - Light nuclei, $N=8$
 - The emergence of $N=16$
 - **The spin-orbit term**
 - Mg and Ni, the 0^+ s
 - ...

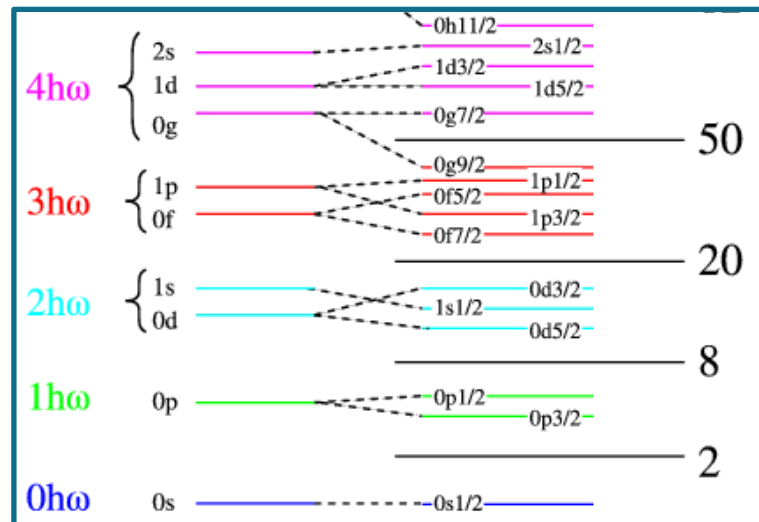
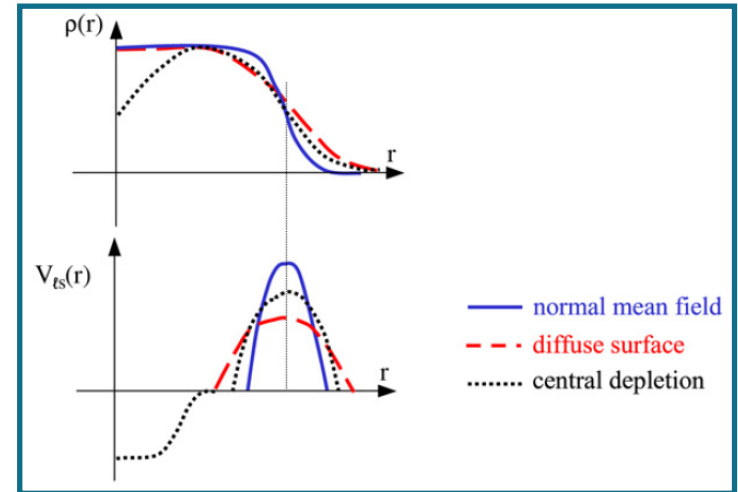
The spin-orbit term

O. Sorlin, M.-G. Porquet, PPNP 61 (2008) 602

- One-body spin-orbit potential:

$$V_{\ell s}(r) = \frac{1}{r} \frac{d\rho}{dr} \vec{\ell} \cdot \vec{s}$$

- a diffuse matter distribution should decrease the SO term
- a depletion of density at the center should induce a decrease of SO for nucleons in the region

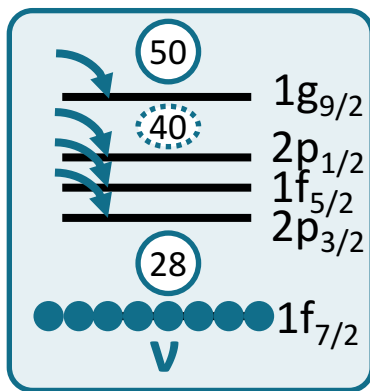


Spin orbit at the surface?

L Gaudefroy et al, PRL 97 (2006) 092501

“Reduction of the Spin-Orbit Splittings
at the N=28 shell closure”

$^{46}\text{Ar}(d,p)^{47}\text{Ar}$ at GANIL (SPIRAL)



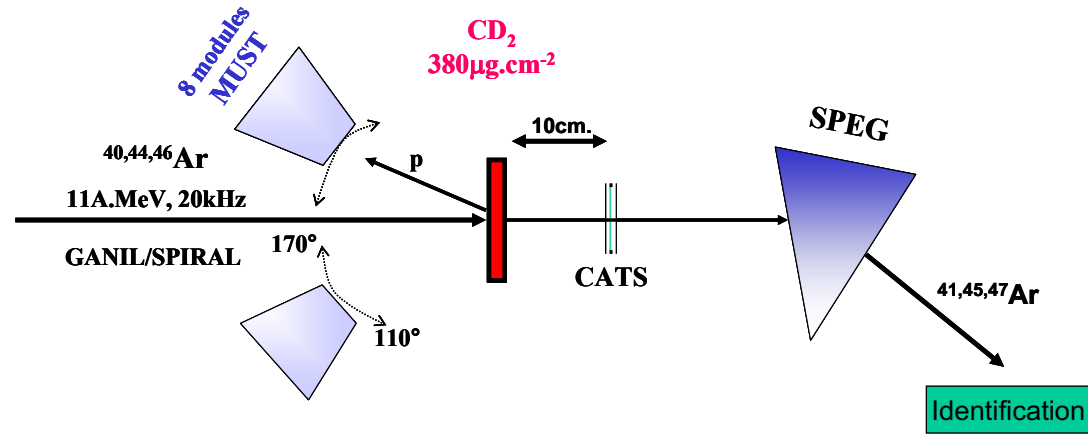
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	42Sc	43Sc	44Sc	45Sc	46Sc	47Sc	48Sc	49Sc	50Sc	51Sc	52Sc	53Sc	54Sc	55Sc	56Sc	57Sc	58Sc
20	41Ca	42Ca	43Ca	44Ca	45Ca	46Ca	47Ca	48Ca	49Ca	50Ca	51Ca	52Ca	53Ca	54Ca	55Ca	56Ca	57Ca
	40K	41K	42K	43K	44K	45K	46K	47K	48K	49K	50K	51K	52K	53K	54K	55K	56K
18	39Ar	40Ar	41Ar	42Ar	43Ar	44Ar	45Ar	46Ar	47Ar	48Ar	49Ar	50Ar	51Ar	52Ar	53Ar		
	38Cl	39Cl	40Cl	41Cl	42Cl	43Cl	44Cl	45Cl	46Cl	47Cl	48Cl	49Cl	50Cl	51Cl			
16	37S	38S	39S	40S	41S	42S	43S	44S	45S	46S	47S	48S	49S				
	36P	37P	38P	39P	40P	41P	42P	43P	44P	45P	46P						
14	35Si	36Si	37Si	38Si	39Si	40Si	41Si	42Si	43Si	44Si							
	21	23	25	27	29	31	33	35	N								

Spin orbit at the surface?

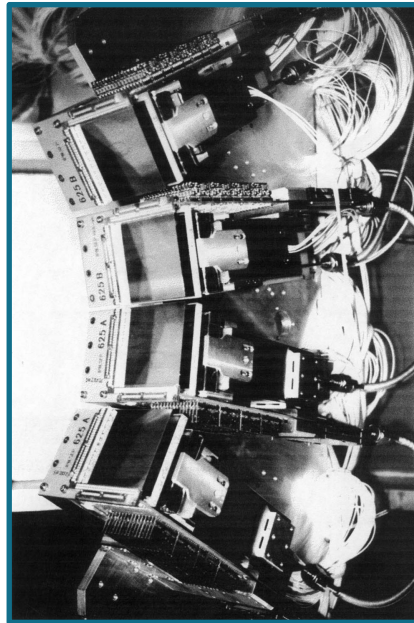
L Gaudefroy et al, PRL 97 (2006) 092501

“Reduction of the Spin-Orbit Splittings at the N=28 shell closure”

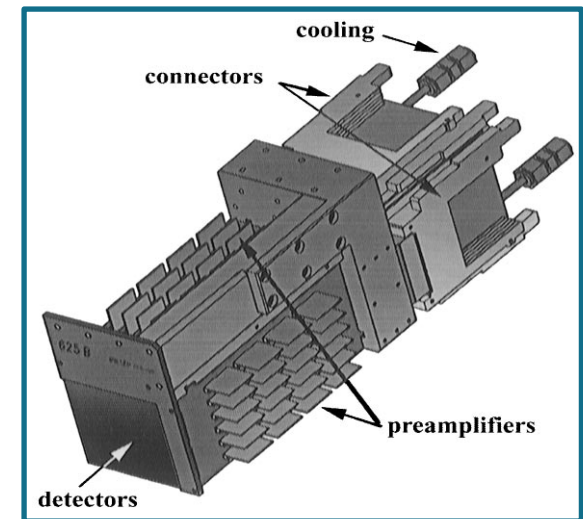
$^{46}\text{Ar}(d,p)^{47}\text{Ar}$ at GANIL (SPIRAL)



- SPEG for identification of ^{47}Ar
- MUST charged-particle telescope detectors
Si-Si(Li)-CsI



Y. Blumenfeld et al
NIMA 421 (1999) 471



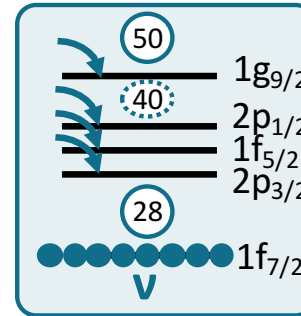
KU LEUVEN

Spin orbit at the surface?

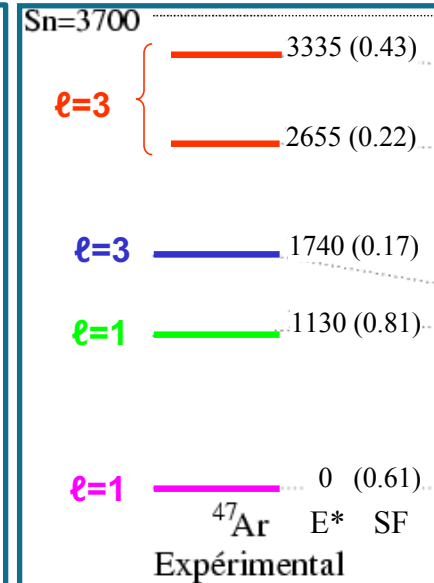
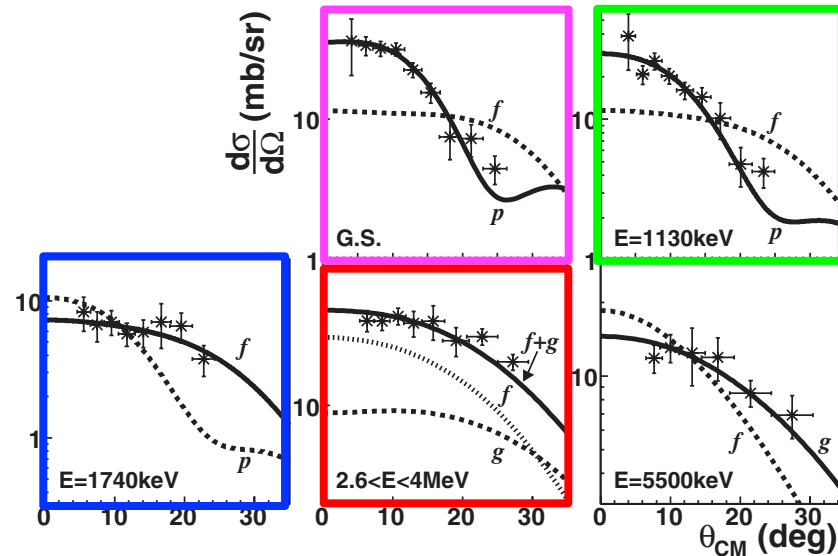
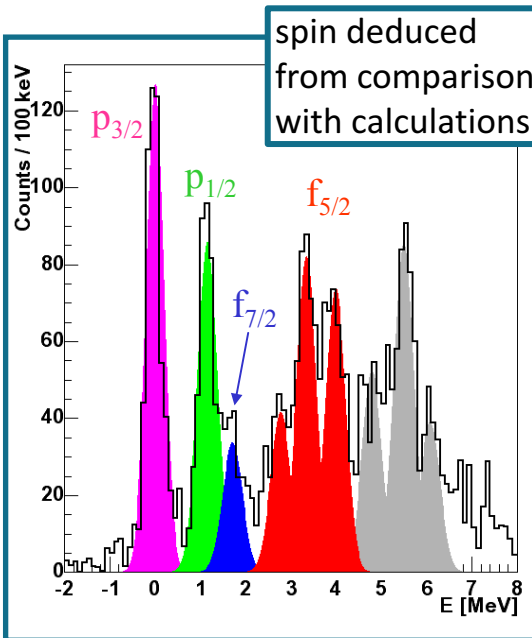
L Gaudefroy et al, PRL 97 (2006) 092501

“Reduction of the Spin-Orbit Splittings
at the N=28 shell closure”

$^{46}\text{Ar}(d,p)^{47}\text{Ar}$



p strength almost
complete
missing $f_{5/2}$ strength
from calculations



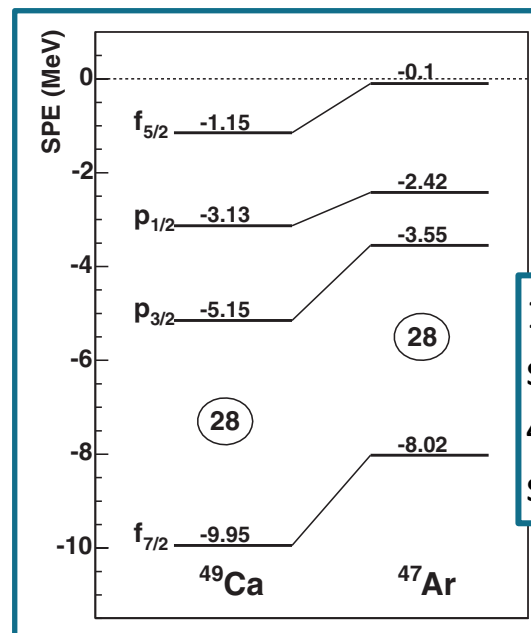
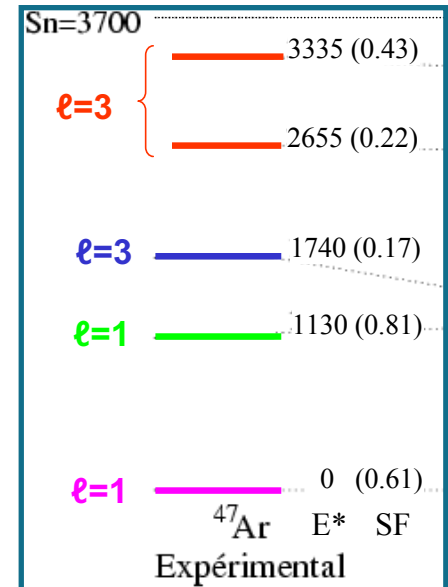
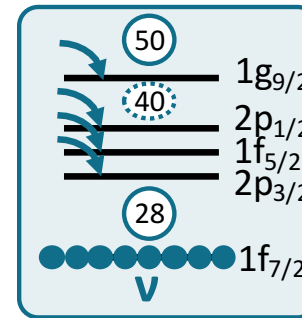
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L Gaudefroy et al, PRL 97 (2006) 092501

“Reduction of the Spin-Orbit Splittings at the N=28 shell closure”

$^{46}\text{Ar}(d,p)^{47}\text{Ar}$

- Mass excess of ground state from Q-value
→ N=28 gap deduced
Reduction of 330 keV compared to ^{49}Ca
- Centroid of $f_{5/2}$ deduced from experiment and calculations; plotted with energy of the “p states”
- Differences with ^{49}Ca (N=28 gap) ascribed to the removal of protons from $d_{3/2}$ and $s_{1/2}$



10% reduction of splitting f orbitals;
45% reduction of splitting p orbitals

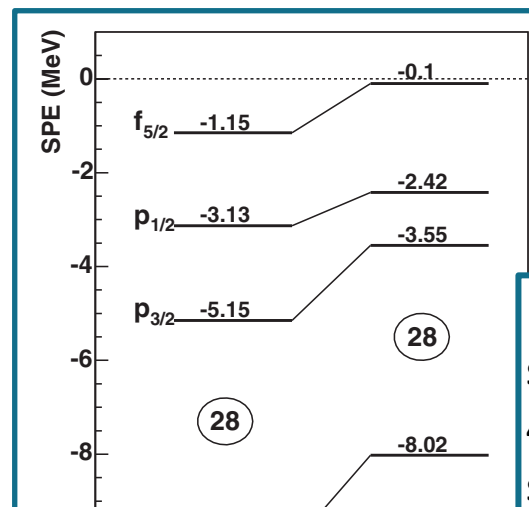
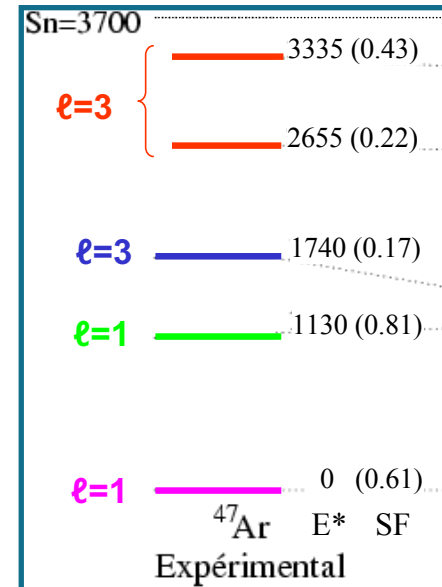
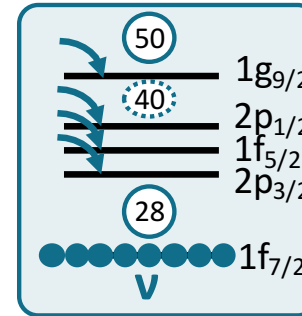
Spin orbit at the surface?

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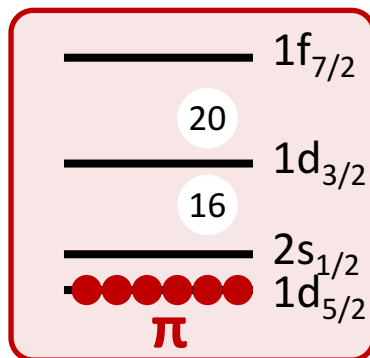
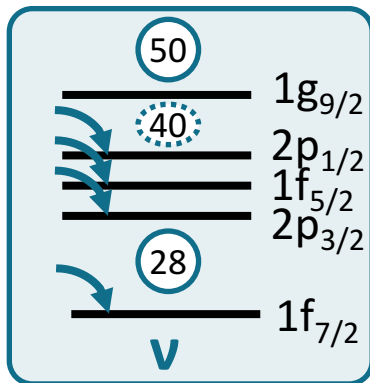
10% reduction of splitting f orbitals;
45% reduction of splitting p orbitals

- Tensor force sufficient to explain reduction of splitting of f orbitals
- Reduction of splitting p orbitals can be due to removal of $s_{1/2}$ proton

Bubble in nucleus?

G Burgunder et al, PRL 112 (2014) 042502

“Experimental Study of the Two-Body Spin-Orbit Force in Nuclei”

 $^{34}\text{Si}(d,p)^{35}\text{Si}$ at GANIL (LISE)


Z	38Ca	39Ca	40Ca	41Ca	42Ca	43Ca	44Ca	45Ca	46Ca	47Ca	48Ca	49Ca	50Ca	51Ca	52Ca	53Ca	54Ca
	37K	38K	39K	40K	41K	42K	43K	44K	45K	46K	47K	48K	49K	50K	51K	52K	53K
18	36Ar	37Ar	38Ar	39Ar	40Ar	41Ar	42Ar	43Ar	44Ar	45Ar	46Ar	47Ar	48Ar	49Ar	50Ar	51Ar	52Ar
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14	32Si	33Si	34Si	35Si	36Si	37Si	38Si	39Si	40Si	41Si	42Si	43Si	44Si				
	31Al	32Al	33Al	34Al	35Al	36Al	37Al	38Al	39Al	40Al	41Al	42Al	43Al				
12	30Mg	31Mg	32Mg	33Mg	34Mg	35Mg	36Mg	37Mg	38Mg	39Mg	40Mg						
	18	20	22	24	26	28	30	32	34	36	38	40					N

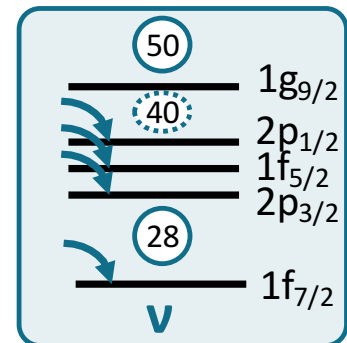
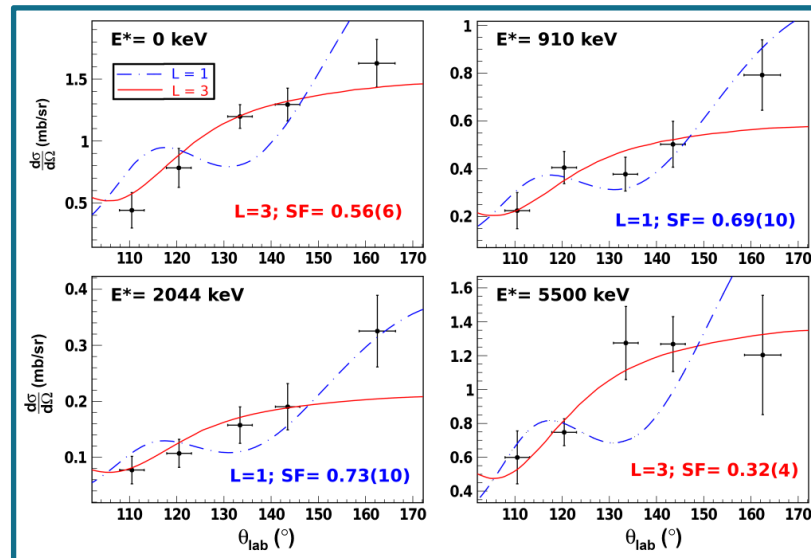
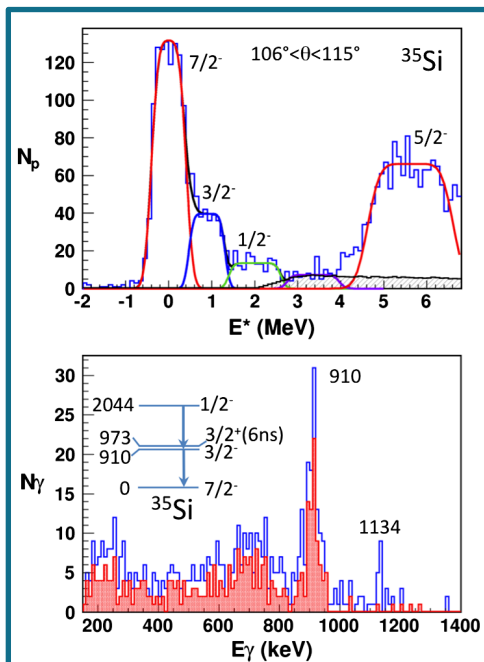
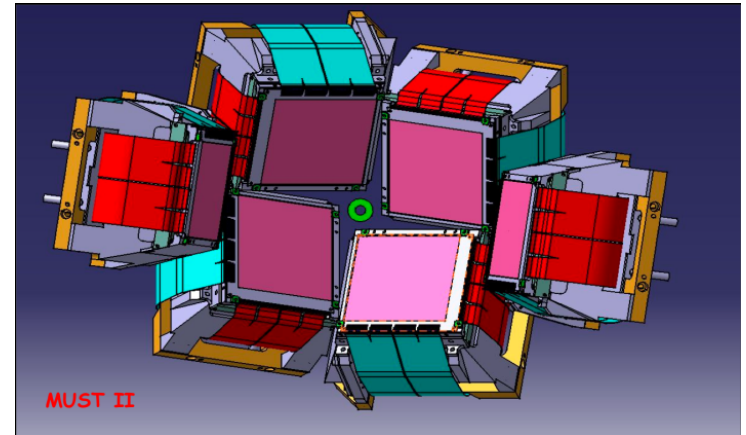
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“Experimental Study of the Two-Body Spin-Orbit Force in Nuclei”

$^{34}\text{Si}(d,p)^{35}\text{Si}$ at GANIL (LISE)

- MUST2 charged-particle detector
- Ionisation chamber + plastic detector for identification of the beam-like particle
- EXOGAM γ -ray array



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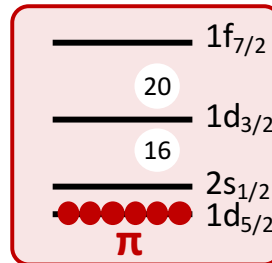
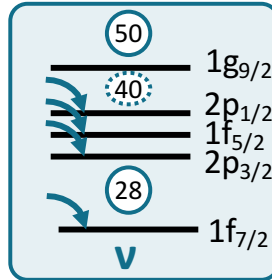
Bubble in nucleus?

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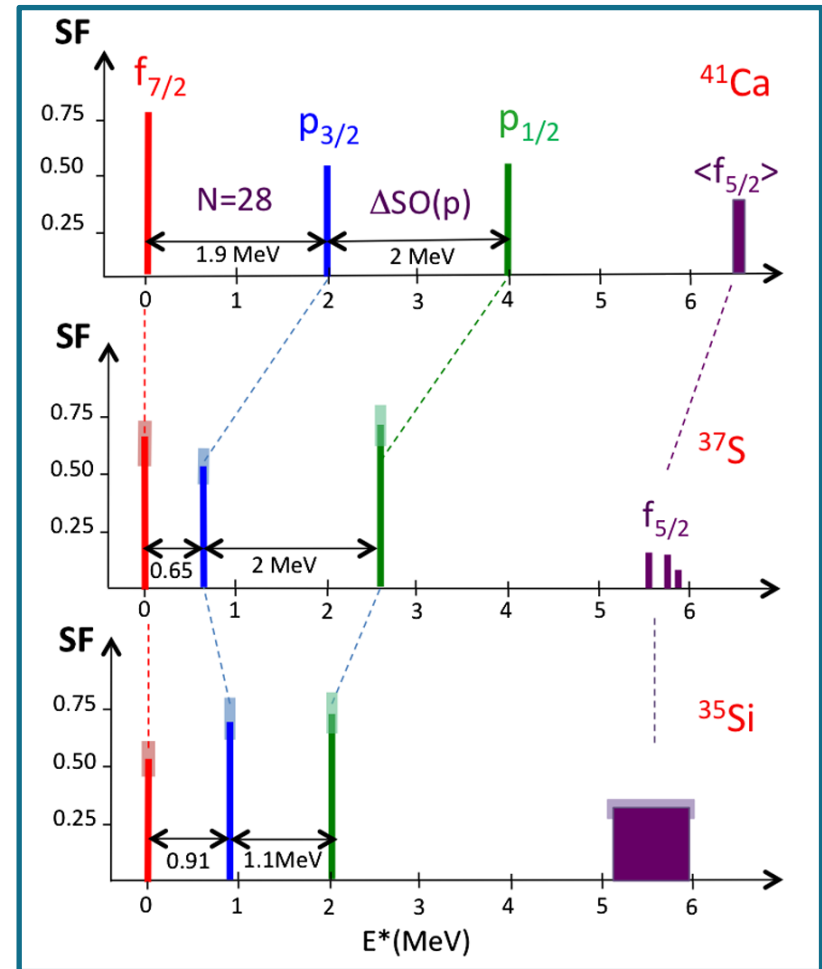
“Experimental Study of the Two-Body Spin-Orbit Force in Nuclei”

$^{34}\text{Si}(d,p)^{35}\text{Si}$ at GANIL (LISE)

- Comparison between “doubly magic nuclei”
- Difference only due to density-dependent terms in the SO-splitting



The Two-Body SO-force is constrained by the experimental values



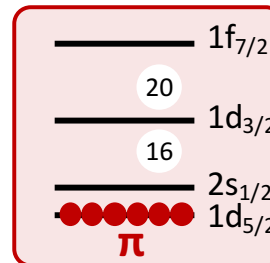
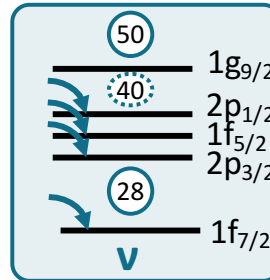
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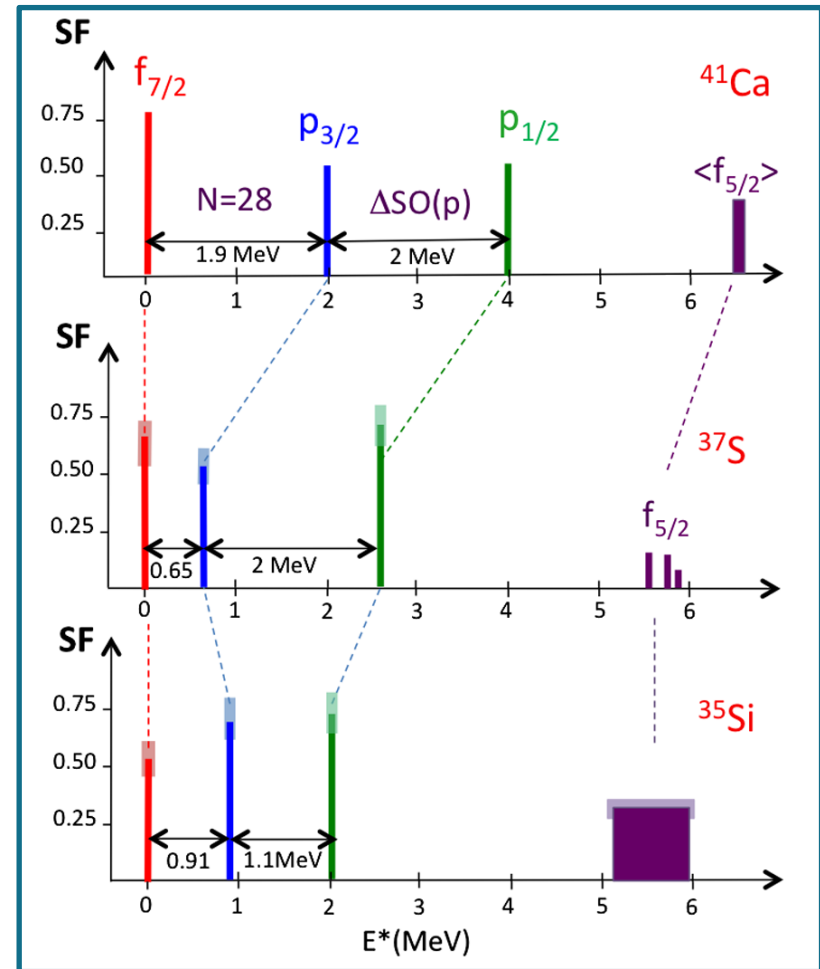
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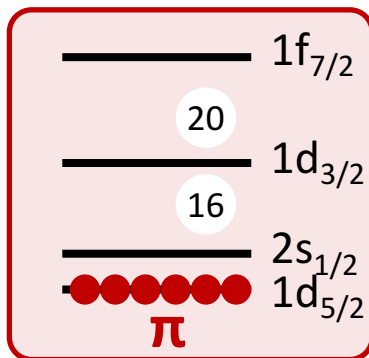


The Two-Body SO-force is constrained by the experimental values



^{34}Si proton removal

- Experiment at MSU
- ^{34}Si on ^9Be target
proton and γ detection
- l from momentum
distribution of protons
- Deduced spin and SFs
of states in ^{33}Al



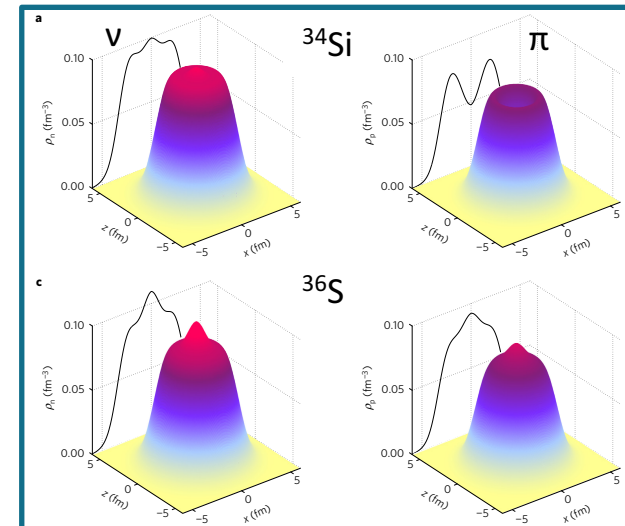
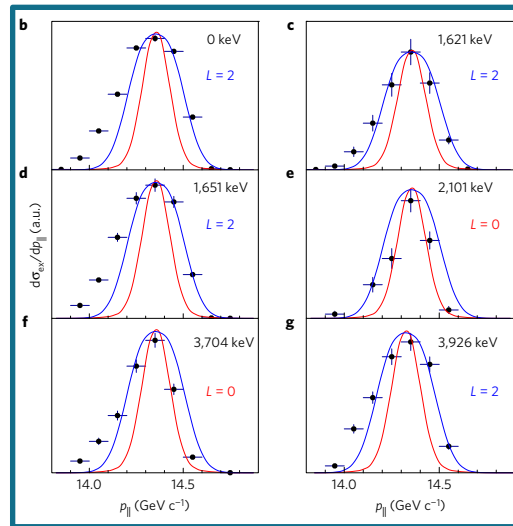
Occupation of $s_{1/2}$ in ^{34}Si is only 17%
Density is depleted inside the nucleus

PUBLISHED ONLINE: 24 OCTOBER 2016 | DOI: 10.1038/NPHYS3916

nature
physics

A proton density bubble in the doubly magic ^{34}Si nucleus

A. Mutschler^{1,2}, A. Lemasson^{2,3}, O. Sorlin^{2*}, D. Bazin⁴, C. Borcea⁵, R. Borcea⁵, Z. Dombrádi⁶, J.-P. Ebran⁷, A. Gade⁴, H. Iwasaki⁴, E. Khan¹, A. Lepailleur², F. Recchia³, T. Roger², F. Rotaru⁵, D. Sohler⁶, M. Stanoiu⁵, S. R. Stroberg^{4,8}, J. A. Tostevin⁹, M. Vandebrouck¹, D. Weisshaar³ and K. Wimmer^{3,10,11}



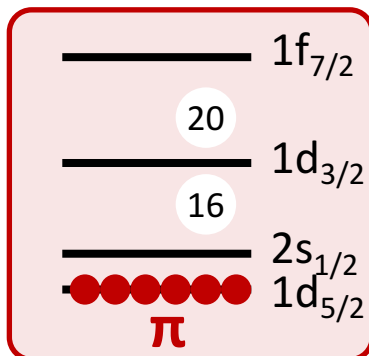
Bubble in nucleus?

A Mutschler et al, Nat Phys 13 (2017) 152

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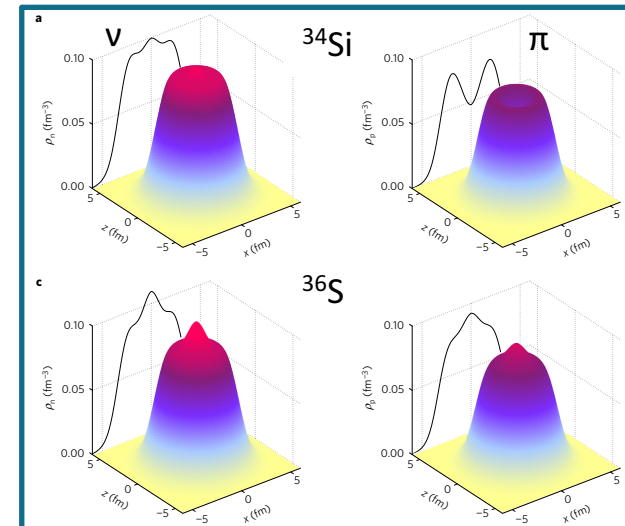
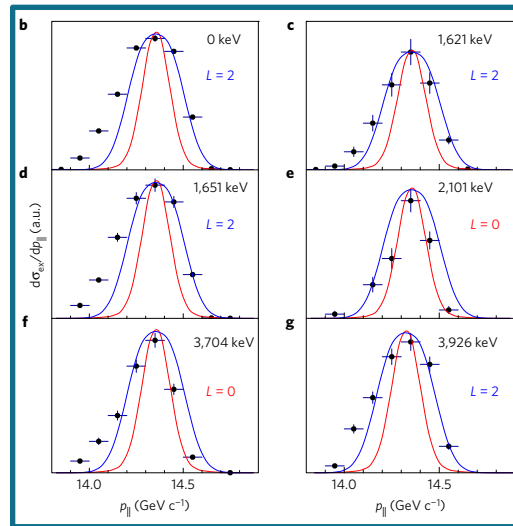
ARTICLES

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Contents

- Nuclear reactions
 - Types of reactions
 - Characteristics of direct reactions
- Why use transfer reactions
 - Information from reactions
 - Q-value, angular momentum, spectroscopic factors
- Reactions and RIBs
 - Motivations
 - Challenges: inverse kinematics
- **Case studies**
 - Light nuclei, $N=8$
 - The emergence of $N=16$
 - The spin-orbit term
 - **Mg and Ni, the 0^+ s**
 - ...

The structure of 0^+ states

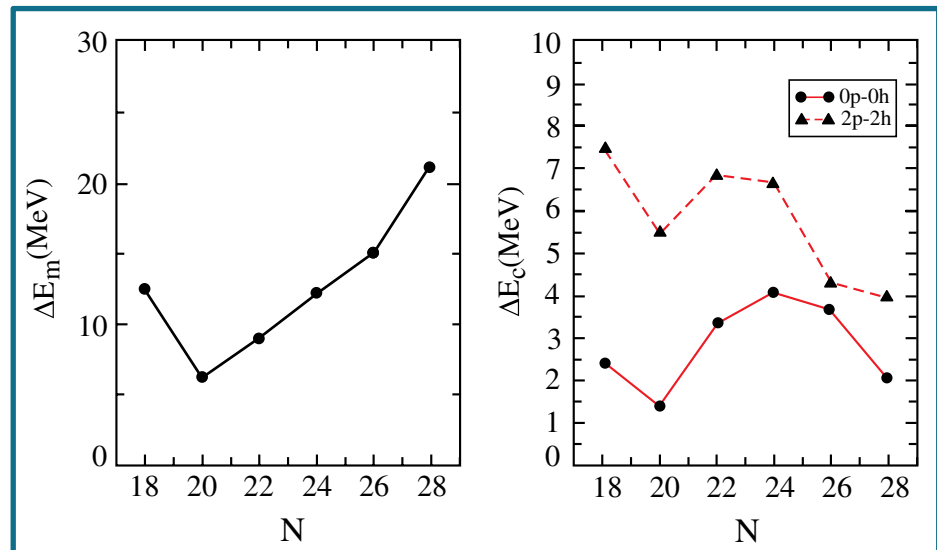
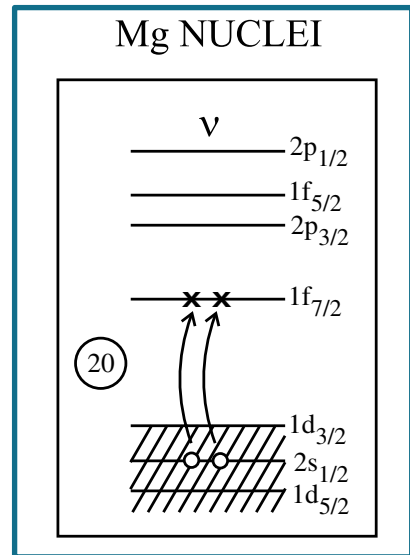
- When the monopole gap is of the same size as the correlation energy:
2p-2h configurations appear at low energy
 0^+ states with different shapes
- “Shape transitions” and
“islands of inversion”:
How can we probe the s.p.
content of the wave function?

Use two-neutron transfer to connect
 0^+ states with similar configurations

Caution

- The initial state should be known
- Reaction process:
two neutrons as a cluster?

K Heyde and JL Wood,
Rev Mod Phys 83 (2011) 1467



E Caurier et al, PRC 58 (1998) 2033

The structure of 0^+ states

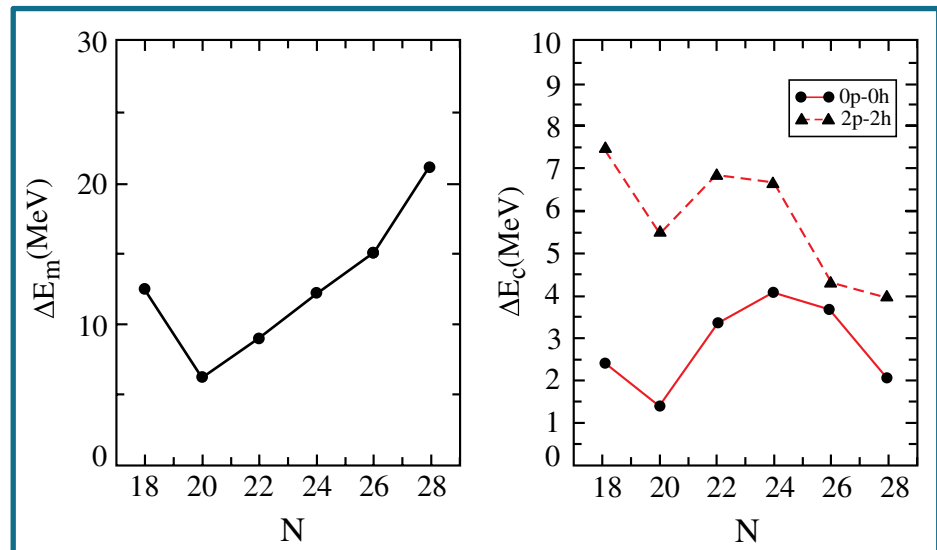
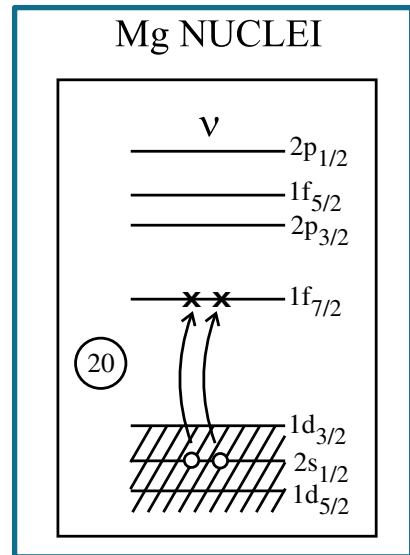
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The 0^+ states in ^{32}Mg

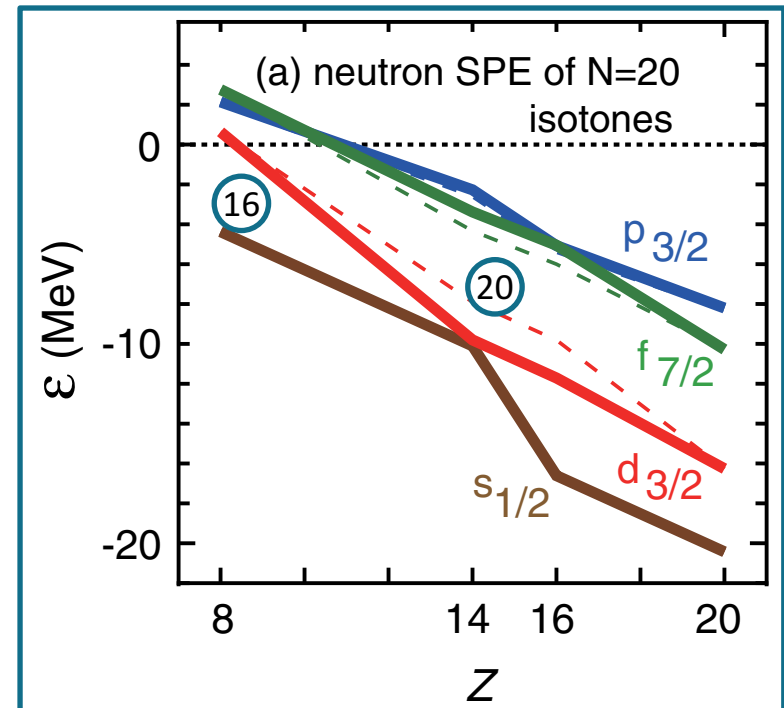
K Wimmer et al., PRL 105 (2010) 252501

Looking for the second, spherical 0^+ in ^{32}Mg

$^{30}\text{Mg}(t,p)^{32}\text{Mg}$

S 32 94.99 55 < 0.0005	S 33 0.75 σ 0.46 σ_{rel} 0.12 σ_{rel} 0.002	S 34 4.25 σ 0.25	S 35 87.37 d β^- 0.2 no γ	S 36 0.01 σ 0.24	S 37 5.0 m β^- 1.8, 4.9... γ 3103...	S 38 2.83 h β^- 1.0, 2.9... γ 1942, 1746...
P 31 100 17	P 32 14.268 d β^- 1.7 no γ	P 33 25.35 d β^- 0.2485 no γ	P 34 12.4 s β^- 5.4... γ 2127...	P 35 47.4 s β^- 2.3... γ 1572...	P 36 5.6 s β^- 3291, 903 1638, 2540...	P 37 2.31 s β^- 646, 1583 2254...
Si 30 3.092 107	Si 31 2.62 h β^- 1.5... γ (1266) σ 0.073	Si 32 153 a β^- 0.2 no γ σ < 0.5	Si 33 6.11 s β^- 3.9, 5.8... γ 1848...	Si 34 2.77 s β^- 3.1 γ 1179, 429 1608	Si 35 0.78 s β^- 4101, 2386 3860, 241...	Si 36 0.45 s β^- 175, 250, 878 425...
Al 29 6.6 m 25... 273, 2426 38...	Al 30 3.60 s β^- 5.1, 6.3... γ 2235, 1263 3498...	Al 31 644 ms β^- 5.6, 7.9... γ 2317, 1695...	Al 32 33 ms β^- 1941, 3042 4230... β n	Al 33 41.7 ms β^- 1941*, 434 1010	Al 34 56.3 ms β^- 12.8... γ 729, 3326 124, 4257 β n	Al 35 38.6 ms β^- 13.3, 14.2... γ 64, 910 3326*... β n
Mg 28 20.9 h 0.5, 0.9... 1, 1342, 401 ...	Mg 29 1.30 s β^- 4.3, 7.5... γ 2224, 1398 960...	Mg 30 335 ms β^- 6.1... γ 244, 444...	Mg 31 230 ms β^- 1626, 666... β n	Mg 32 86 ms β^- 167... β n	Mg 33 90.5 ms β^- 13.5... β n	Mg 34 20 ms β^- 1616, 4730 1638, 2096... β n
Na 27 301 ms 8.0... 35, 1698... 0.46...	Na 28 30.5 ms β^- 13.9... γ 1471, 2389... 1474*	Na 29 44.9 ms β^- 10.8, 13.4... γ 55, 2560 1474*	Na 30 48 ms β^- 12.2, 15.7... γ 1482, 1040* 1978...	Na 31 17.0 ms β^- 15.4... γ 81, 1482*, 2244 β n 0.08, 0.51... 22n	Na 32 13.2 ms β^- 885, 2152... β n, β 2n	Na 33 8.0 ms β^- 886*, 547 1243... β n
Ne 26 192 ms 4, 1279, 232 ...	Ne 27 31.5 ms β^- 12.6... γ 63, 3019 2736, 2225... β n	Ne 28 18.9 ms β^- 12.2... γ 2063, 863... β 2n	Ne 29 14.8 ms β^- 15.3... γ 72, 1516 1249, 1588... β n, β 2n	Ne 30 5.8 ms β^- 151 β n	Ne 31 3.4 ms β^- β n?	Ne 32 3.5 ms β^- β n?
F 25 50 ms 703, 1613 ...	F 26 10.2 ms β^- γ 2018, 1673 β n	F 27 5.0 ms β^- γ 2018*	F 28 <40 ns β^- γ 2018*	F 29 2.6 ms β^- γ 2018*	F 30 <260 ns β^- γ 2018*	F 31 >260 ns β^- γ 2018*

T Otsuka et al, PRL 104 (2010) 012501



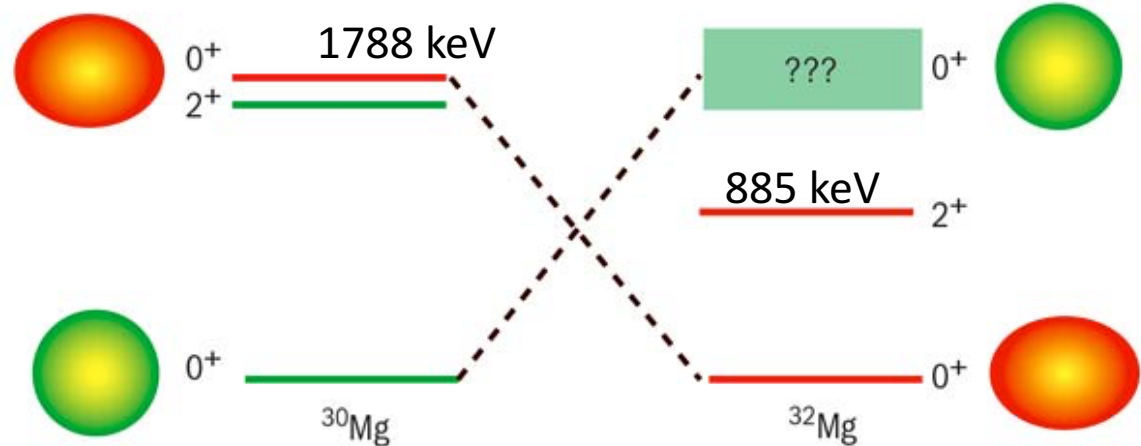
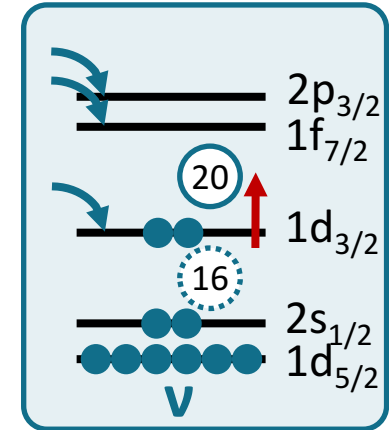
The 0^+ states in ^{32}Mg

K Wimmer et al., PRL 105 (2010) 252501

Looking for the second, spherical 0^+ in ^{32}Mg

$^{30}\text{Mg}(t,p)^{32}\text{Mg}$

- ^{30}Mg : spherical ground state, deformed (intruder) excited state; small mixing
- ^{32}Mg : only ground state 0^+ known, deformed
Predictions for 0^+_2 between 1.4 MeV and 3 MeV
- Two-neutron transfer to
 - find the second 0^+
 - determine the overlap



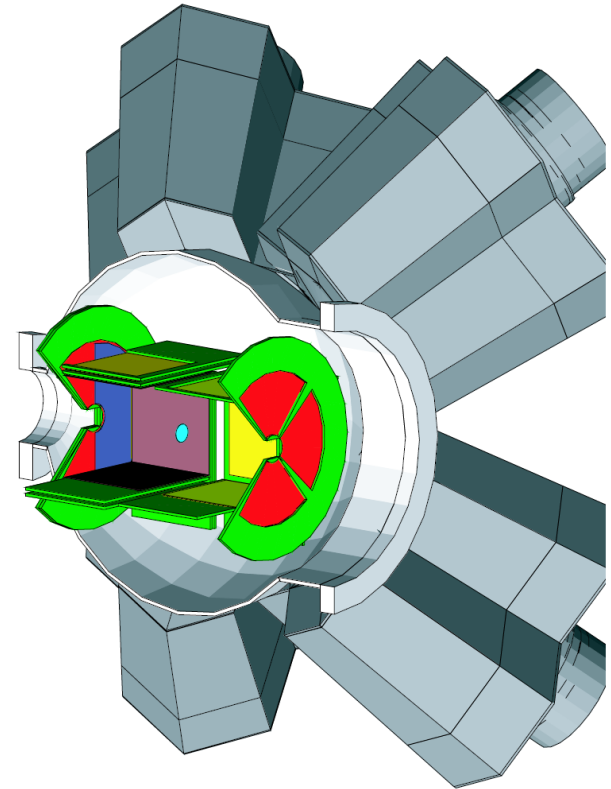
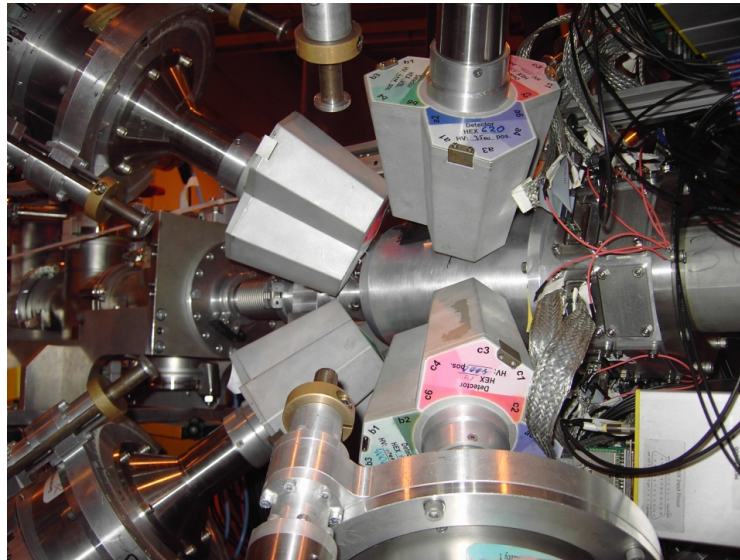
Two-neutron transfer to ^{32}Mg

K Wimmer et al., PRL 105 (2010) 252501

Looking for the second, spherical 0^+ in ^{32}Mg

$^{30}\text{Mg}(t,p)^{32}\text{Mg}$

- ^{30}Mg beam at REX-ISOLDE, 1.8 MeV/nucleon (below fusion barrier for Ti)
- Tritium-implanted Ti foil (t : $40\text{ }\mu\text{g}/\text{cm}^2$)
- T-REX charged-particle detector
- Miniball γ -ray array



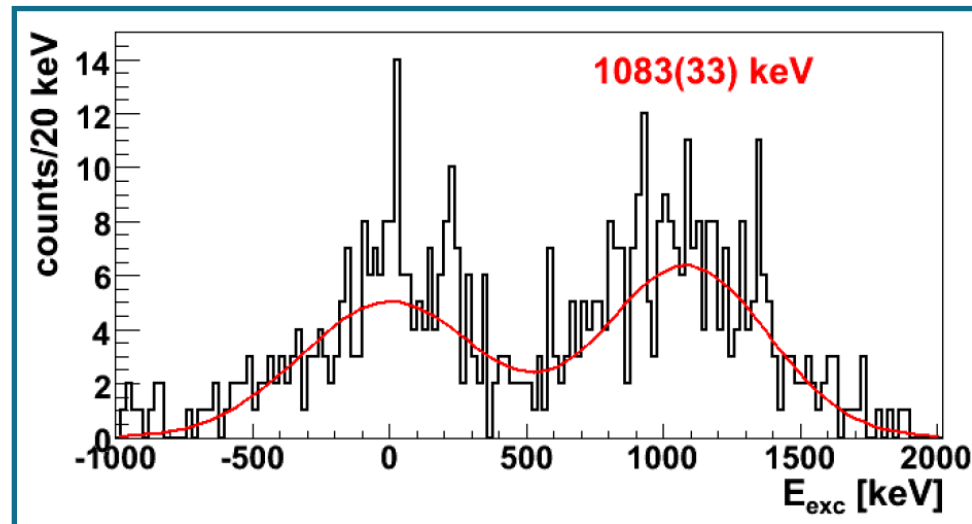
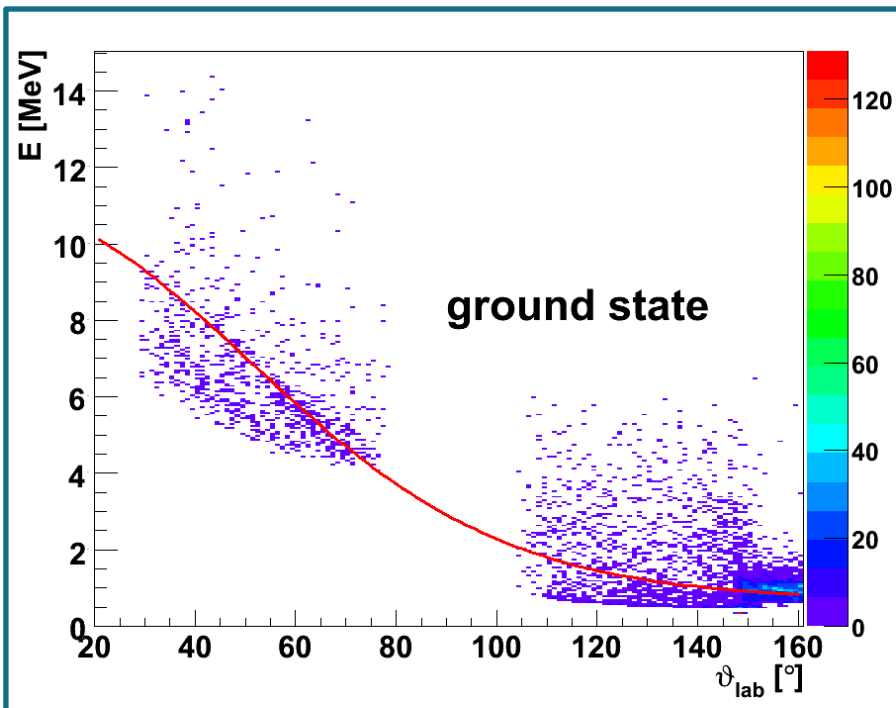
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$^{30}\text{Mg}(t,p)^{32}\text{Mg}$

- Two states identified, well separated



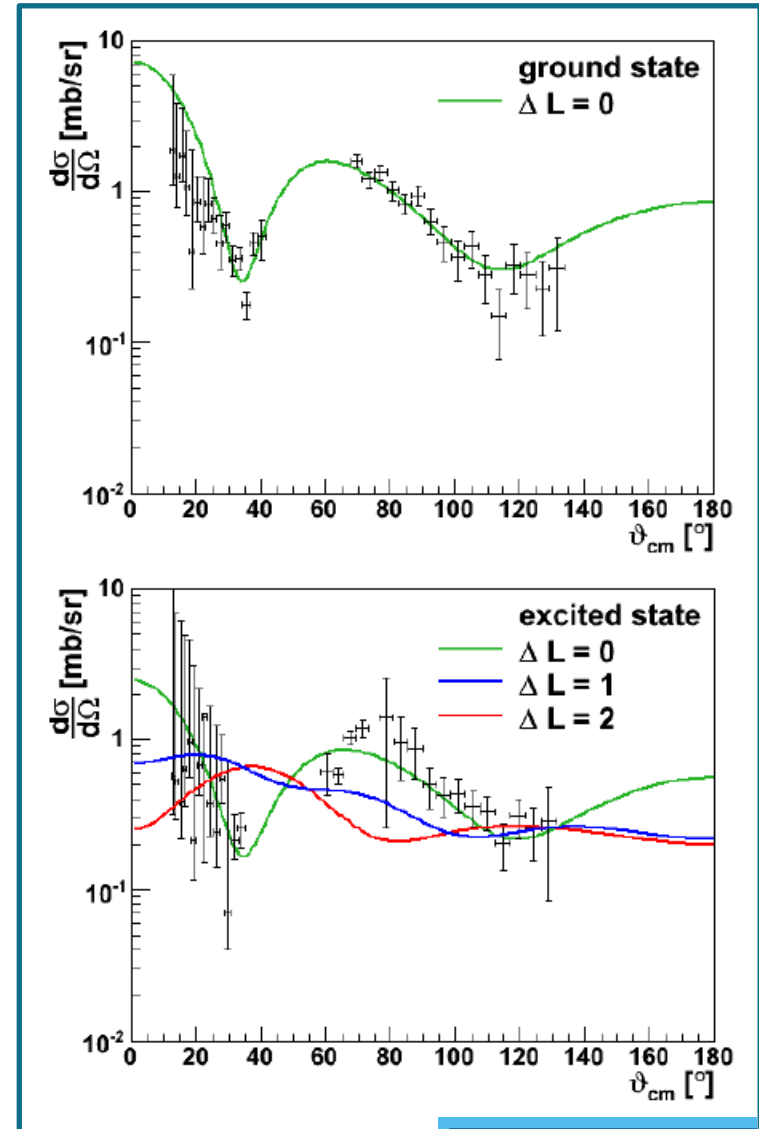
Two-neutron transfer to ^{32}Mg

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Looking for the second, spherical 0^+ in ^{32}Mg

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- Two states identified, well separated
- Angular distributions: $l=0$
- γ -ray coincidences with excited state:
no 2^+ (18 cts expected from 2^+ at 886 keV)



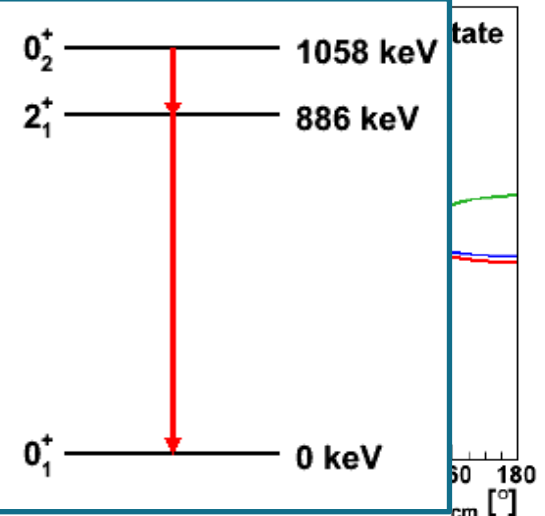
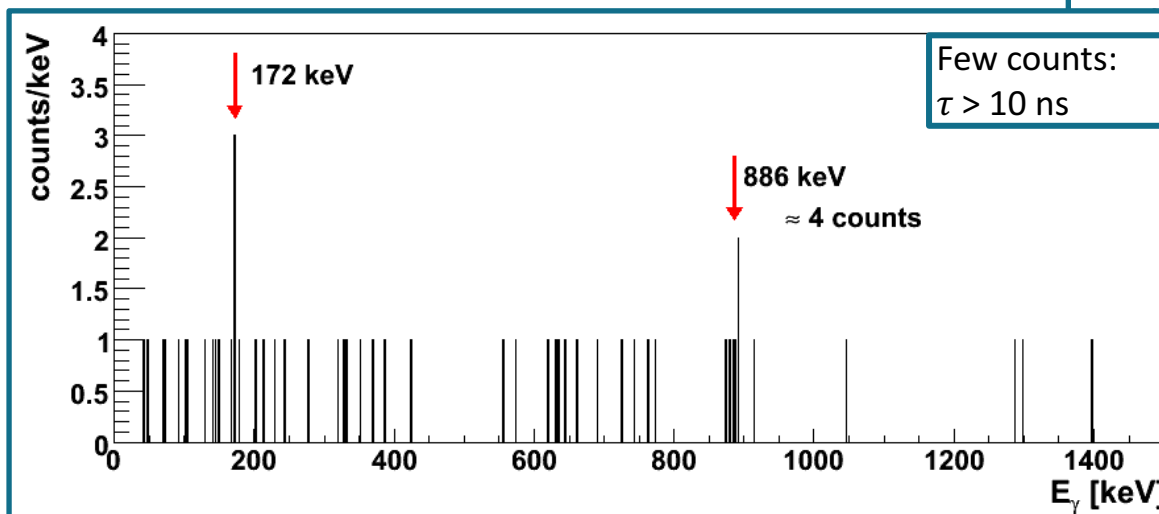
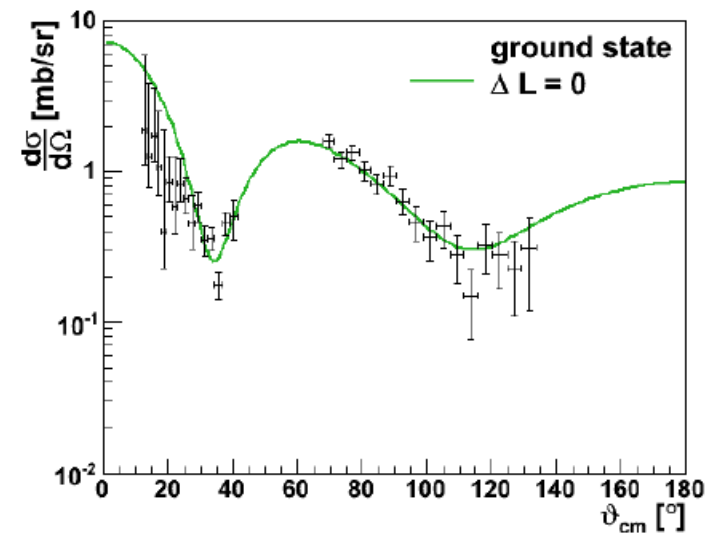
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- γ -ray coincidences with excited state: no 2^+ (18 cts expected from 2^+ at 886 keV)



Two-neutron transfer to ^{32}Mg

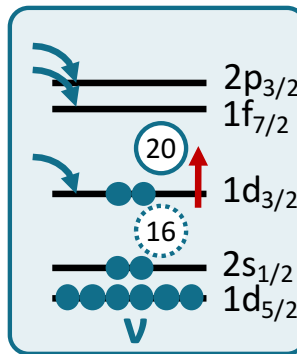
K Wimmer et al., PRL 105 (2010) 252501

Looking for the second, spherical 0^+ in ^{32}Mg

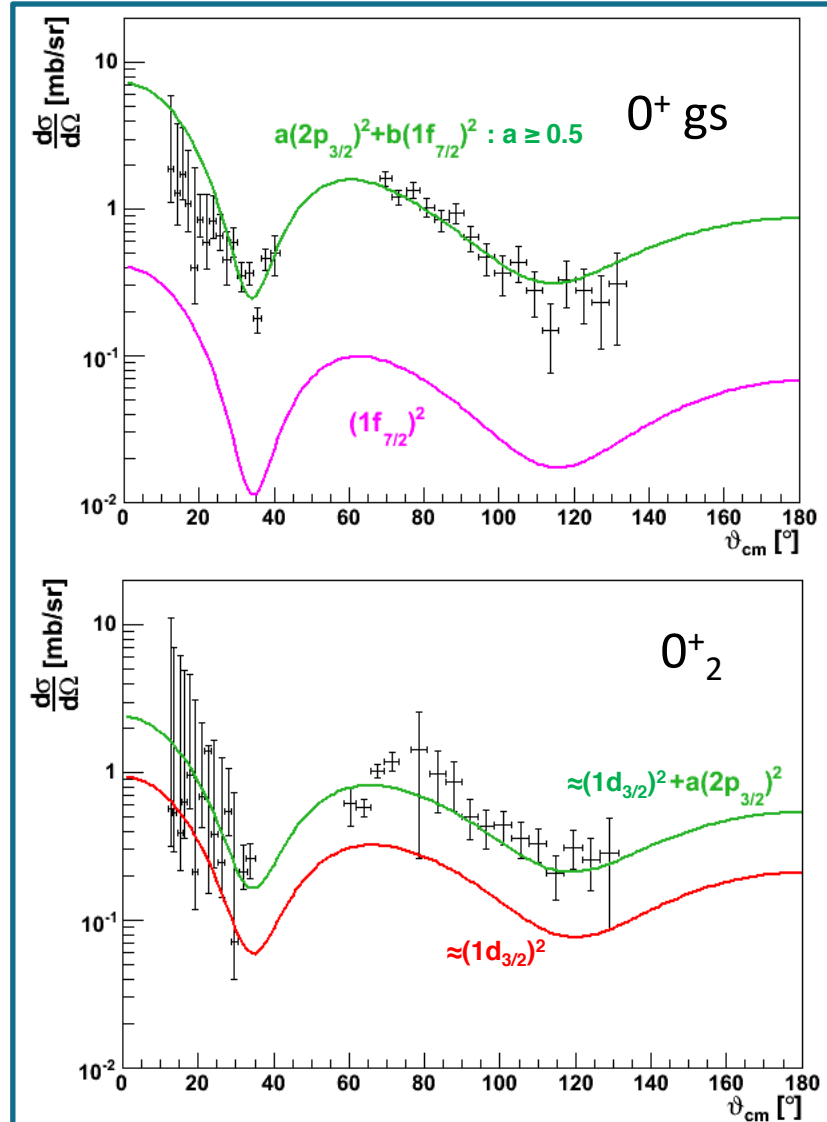
$^{30}\text{Mg}(t,p)^{32}\text{Mg}$

- Two-step transfer?
- $^{30}\text{Mg}(t,d)$ large negative Q -value

- 0^+_2 lower than predicted
- Long lifetime
- Similar cross sections



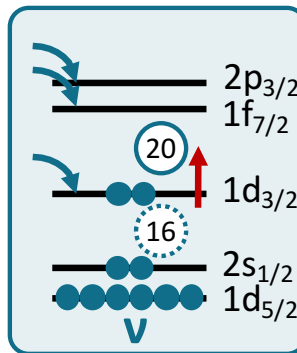
- $(p_{3/2})^2$ component, strong in the g.s.
 - Mixing between the 0^+ s?
- Measure monopole strength for 0^+_2



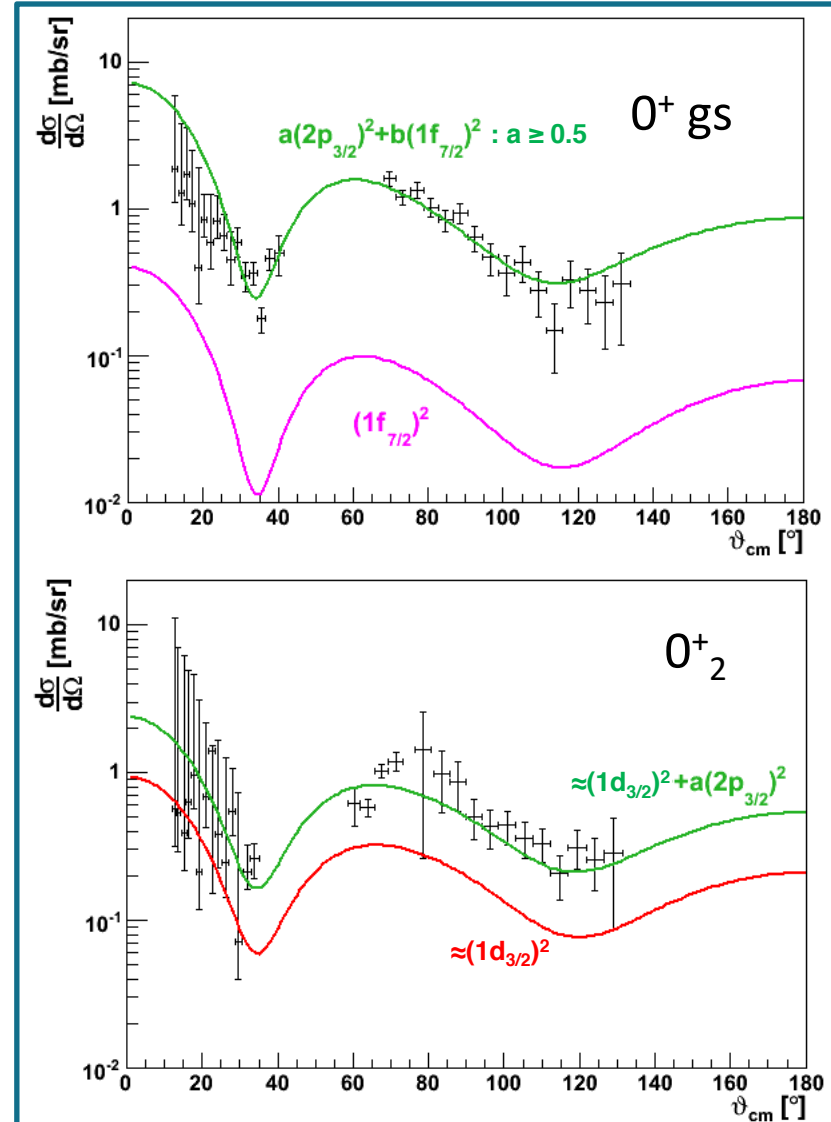


- Two-step transfer?
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- $(p_{3/2})^2$ component, strong in the g.s.
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- Measure monopole strength for 0^+ ,



The 0^+ states in ^{68}Ni

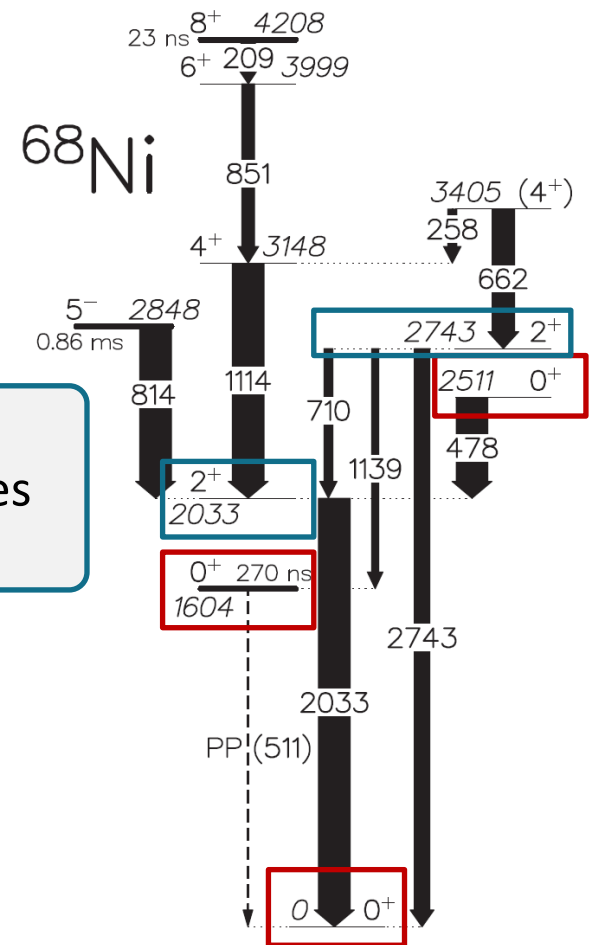
Recent experimental work

- F. Flavigny et al., PRC 91 (2015) 034310
- S. Suchyta et al., PRC 89 (2013) 021301R
- F. Recchia et al., PRC 88 (2013) 041302R
- R. Broda et al., PRC 86 (2012) 064312
- C. J. Chiara et al., PRC 86 (2012) 041304R
- A. Dijon et al., PRC 85 (2012) 031301R

Crucial information

- Precise measurement of 0^+_2 energy
Since 1982: 1770(30) keV from $^{70}\text{Zn}(^{14}\text{C}, ^{16}\text{O})^{68}\text{Ni}$
Now: 1603.5(3) keV
- Two transitions feeding 0^+_2 (1139 and 2420 keV)
- Firm assignment of several spin/parities

Three 0^+ states
and two 2^+ states
below 2.8 MeV



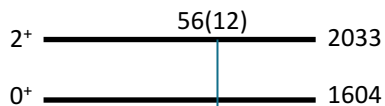
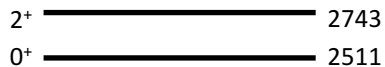
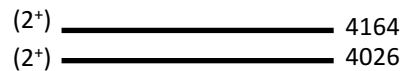
Level scheme from F. Recchia et al.
PRC 88 (2013) 041302R

The 0^+ states in ^{68}Ni

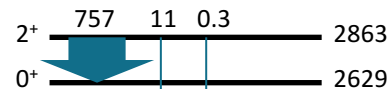
Large-scale Shell Model with LNPS interaction

S Lenzi et al, PRC 82 (2010) 054301

- ^{48}Ca core, π pf – ν pfg_{9/2}d_{5/2} to describe Fe and Cr



B(E2,down) values in e^2fm^4



LNPS

$(2p2h)^\pi + (4p4h)^\nu$
 $\beta = 0.4$ (prolate)

$(2p2h + 0p0h)^\nu$
 $\beta = -0.16$ (oblate)

$(0p0h + 2p2h)^\nu$

"dominant proton configuration has exactly two f7/2 protons less than the ground state"

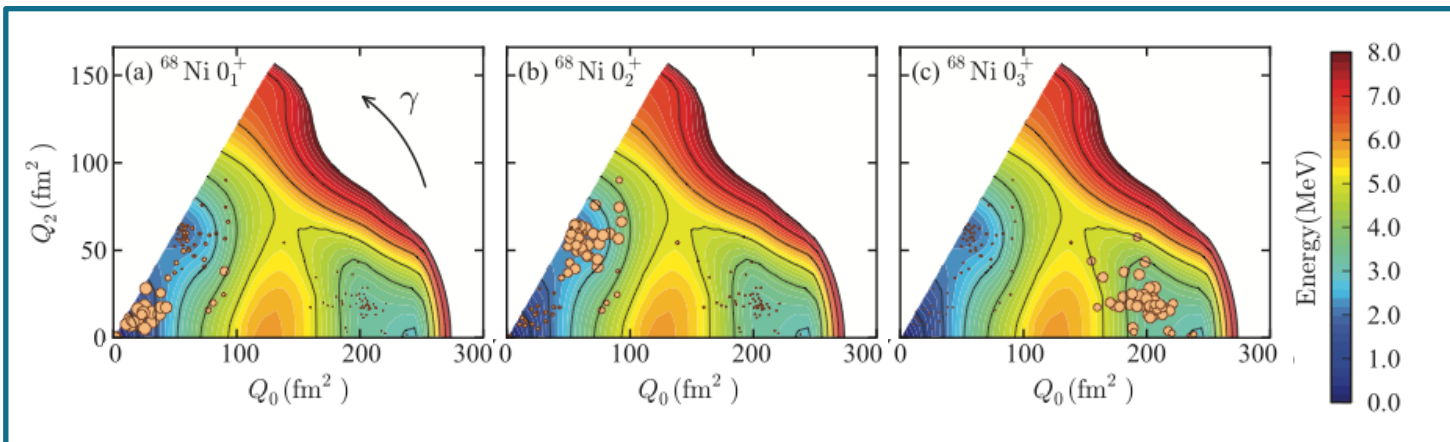
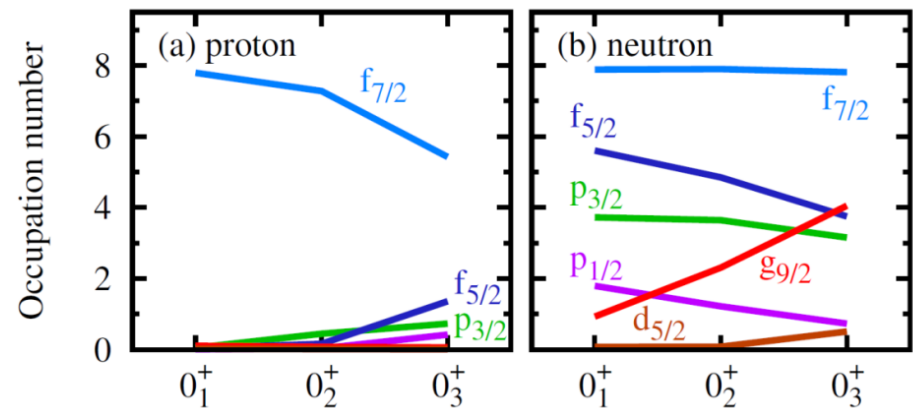
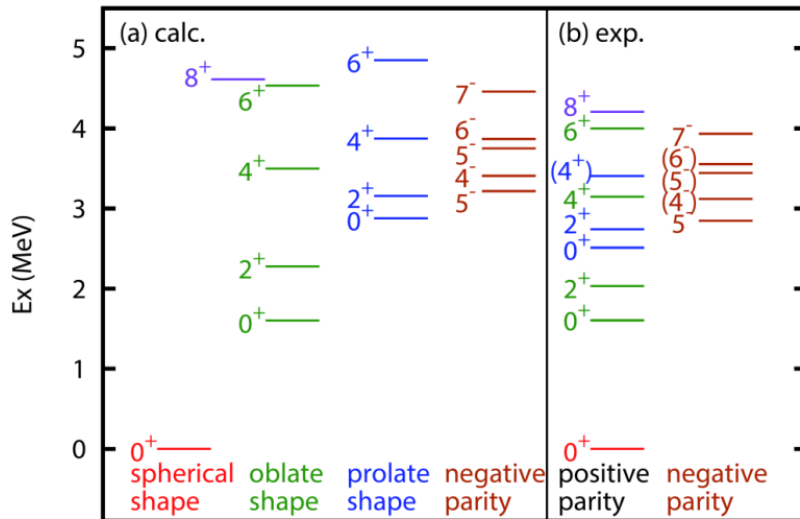
"The 0^+_1 and 0^+_2 states "are characterized by "similar proton occupancies with leading $0p-0h$ (neutron) configuration for the 0^+_1 ground state and $2p-2h$ (neutron) configurations for the 0^+_2 ."

^{68}Ni

The 0^+ states in ^{68}Ni

Monte-Carlo Shell-Model Y. Tsunoda et al., PRC 89 (2014) 031301R

- Full $\text{pf} + \text{g}_{9/2} + \text{d}_{5/2}$ for both neutrons and protons



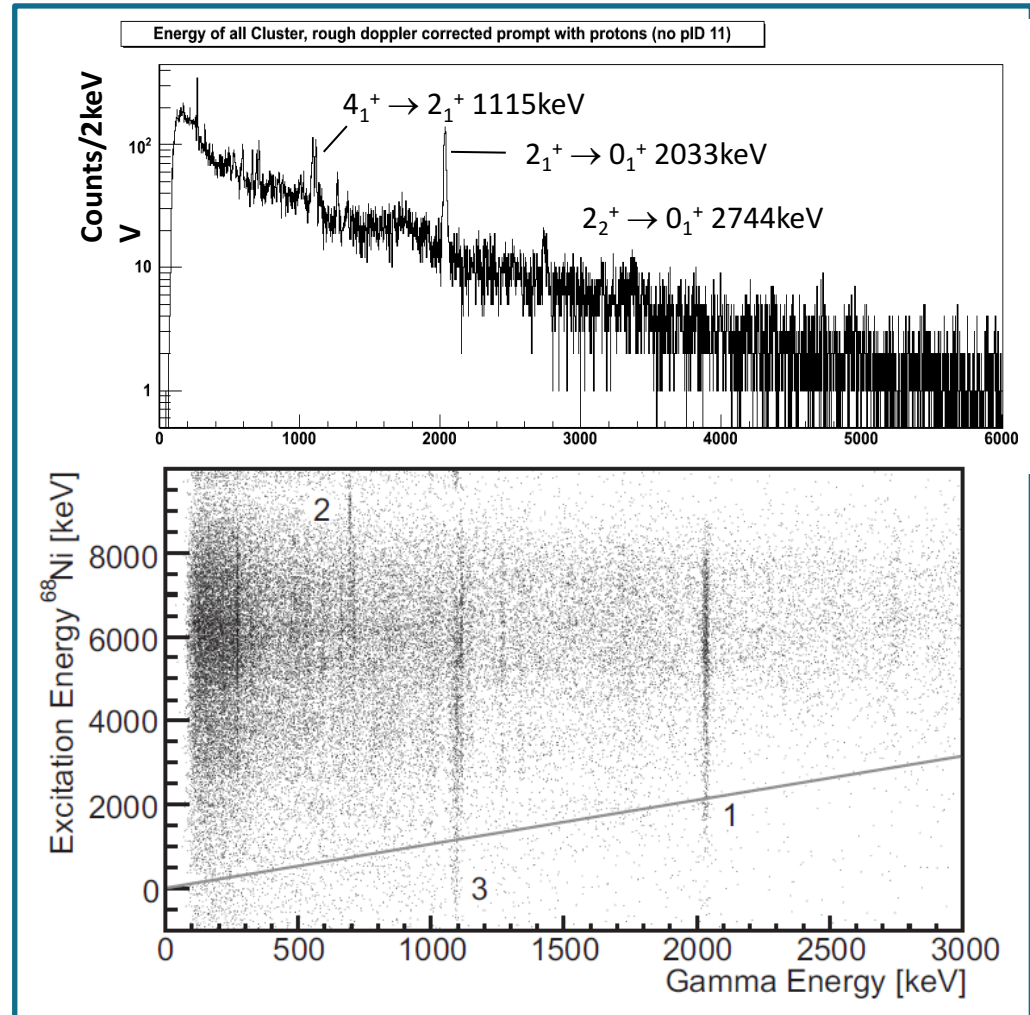
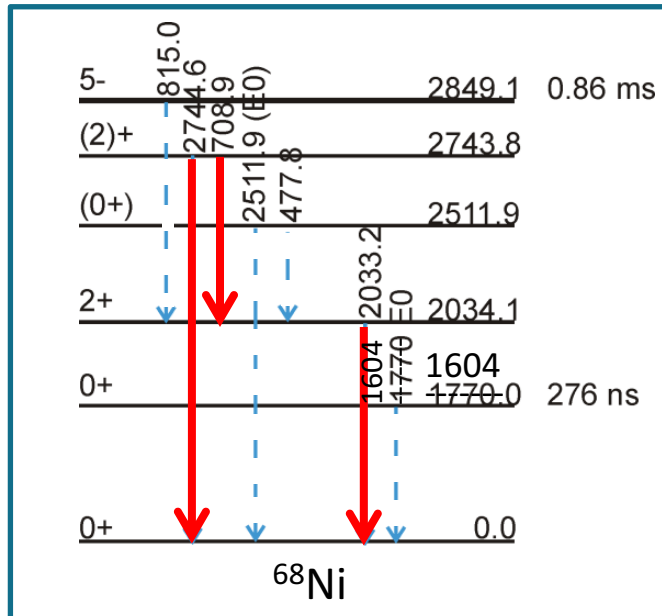
Two-neutron transfer to ^{68}Ni

J Elseviers, PhD thesis, KU Leuven

Probing the structure of 0^+ and 2^+ states in ^{68}Ni

$^{66}\text{Ni}(t,p)^{68}\text{Ni}$ at 2.6 MeV/nucleon

- Few γ 's to ground state
- No p- γ - γ coincidences

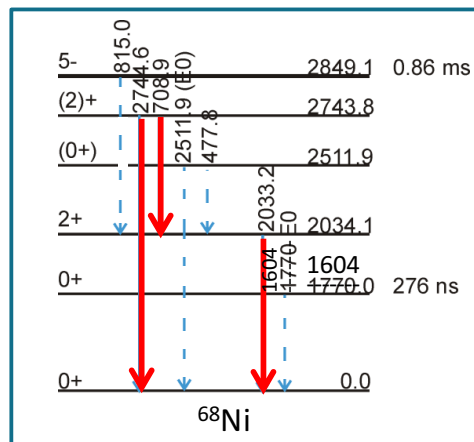
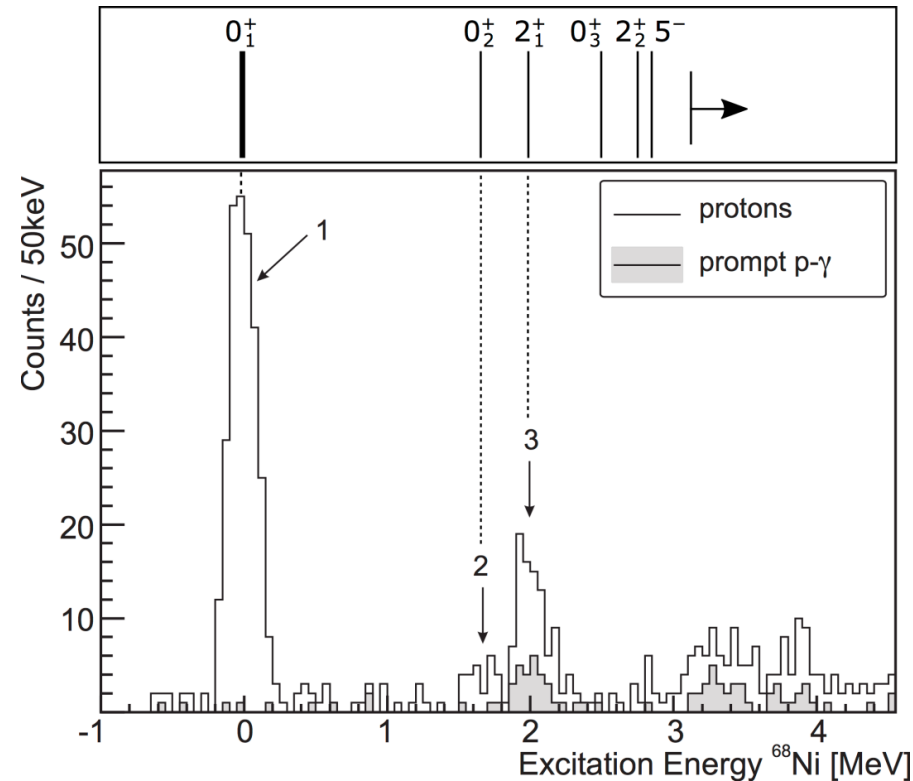
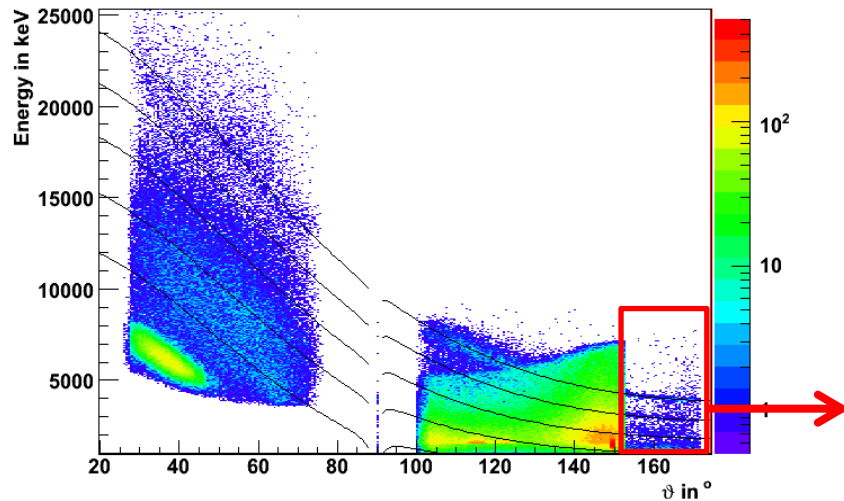


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- Population of 0^+_2 : 5.4(11)% of g.s.
- Upper limits (<4%) on population of 0^+_3 and 2^+_2

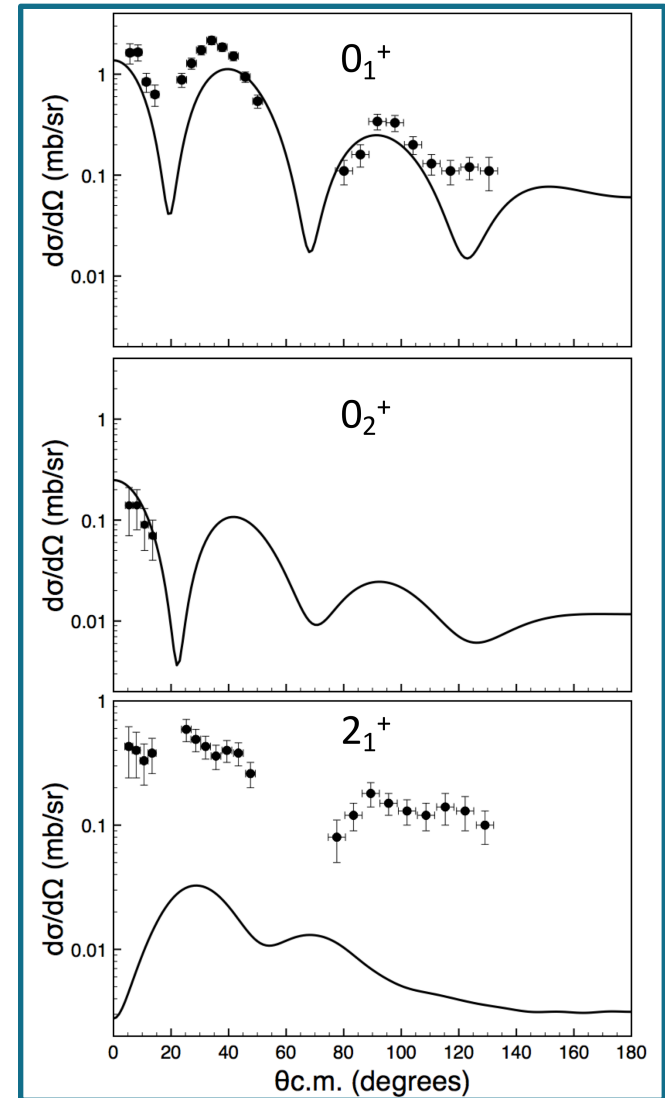
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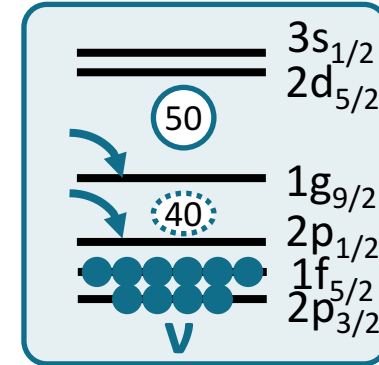
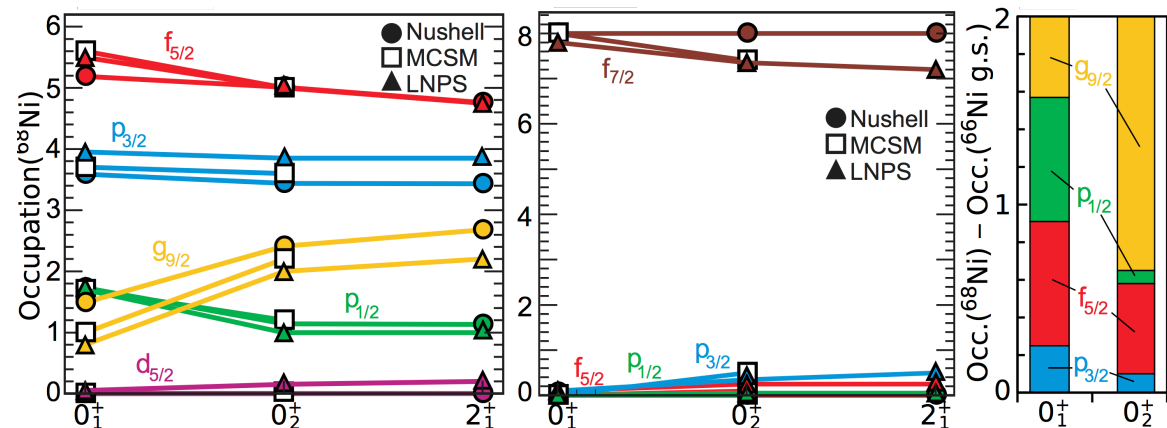
- Two-neutron overlap amplitudes from MCSM (T. Otsuka)
pf+g_{9/2}+d_{5/2} both protons and neutrons
- Works well for the 0^+ s
does not reproduce the 2^+_1



Probing the structure of 0^+ and 2^+ states in ^{68}Ni

$^{66}\text{Ni}(t,p)^{68}\text{Ni}$ at 2.6 MeV/nucleon

- Two-neutron overlap amplitudes from MCSM (T. Otsuka)
pf+g_{9/2}+d_{5/2} both protons and neutrons

neutron - **occupation numbers** - protons

	$f_{5/2}$		$p_{3/2}$		$p_{1/2}$		$g_{9/2}$	
^{66}Ni gs	4.53		3.34		1.07		1.06	
^{68}Ni gs	5.19	+0.66	3.59	+0.25	1.73	+0.66	1.49	+0.43
^{68}Ni $0^+_{2\gamma}$	5.01	+0.48	3.44	+0.10	1.14	+0.07	2.41	+1.35

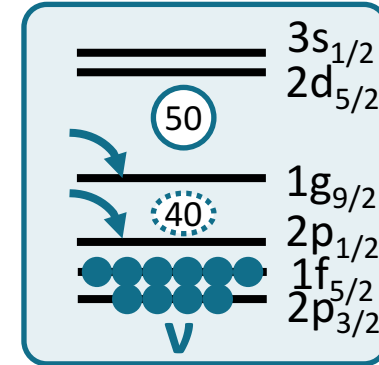
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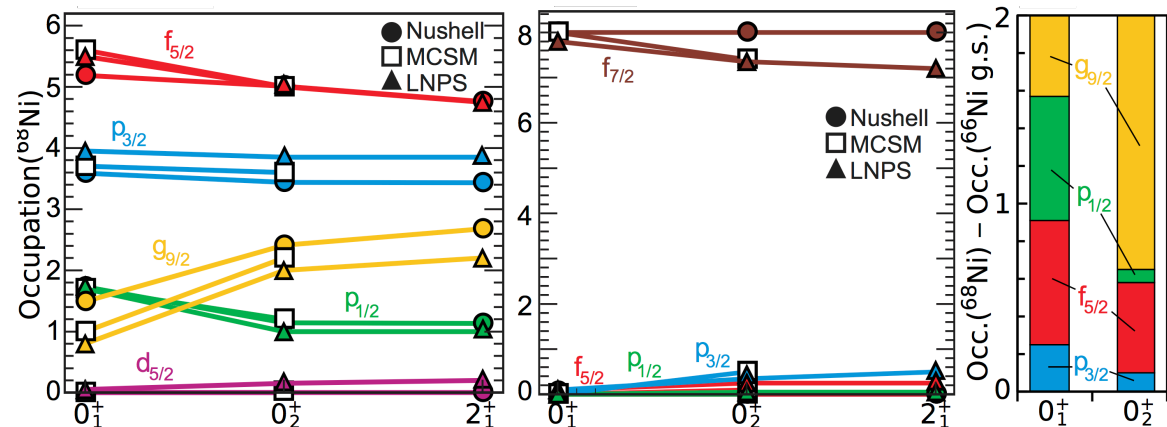
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$^{66}\text{Ni}(t,p)^{68}\text{Ni}$ at 2.6 MeV/nucleon

- Two-neutron overlap amplitudes from MCSM (T. Otsuka)
 $pf+g_{9/2}+d_{5/2}$ both protons and neutrons



neutron - occupation numbers - protons



Agreement for $0^+_{1,2}$ states

0^+_1 state populated by transfer filling N=40

0^+_2 state populated by transfer across N=40

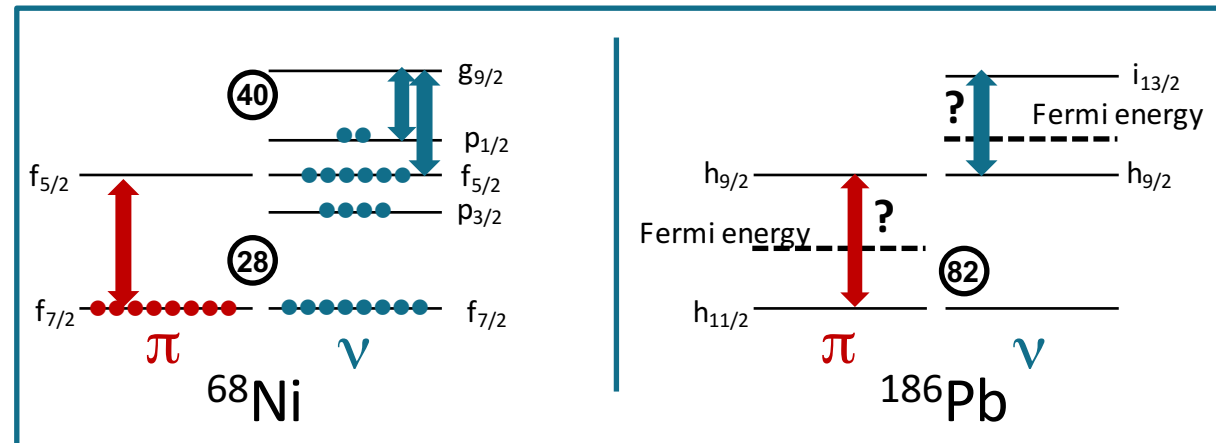
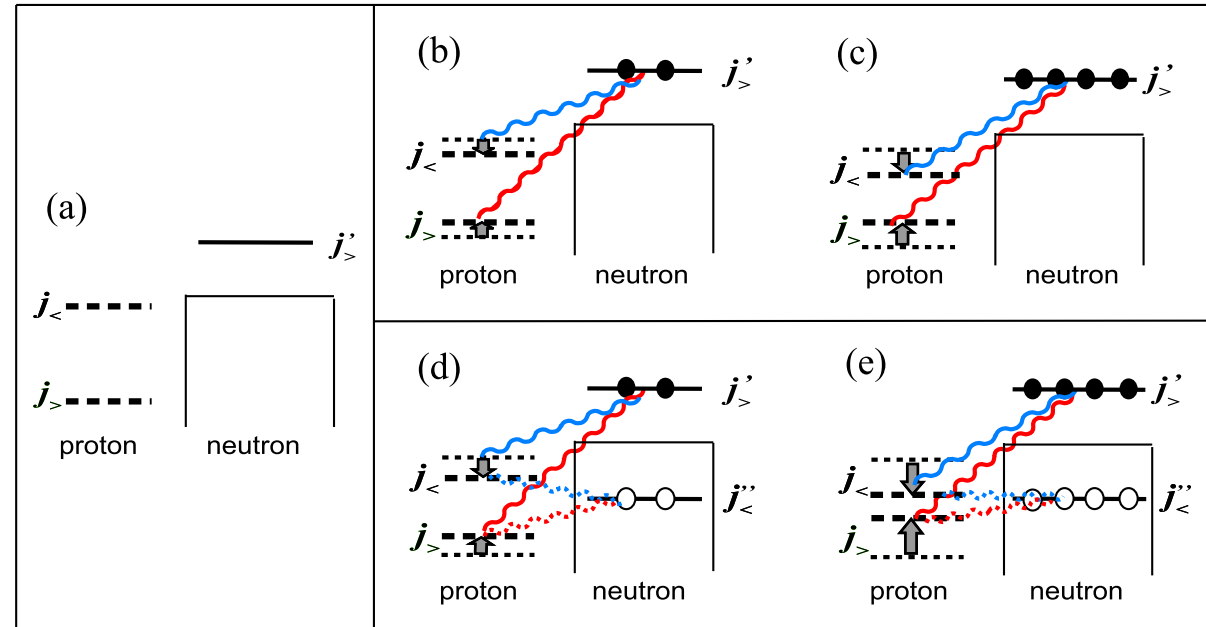
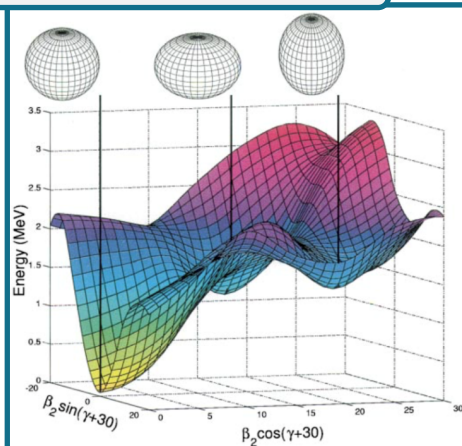
0^+ s in Pb: same mechanism?

T Otsuka and Y Tsunoda, JPG 43 (2016) 024009

T Otsuka and Y Tsunoda
JPG 43 (2016) 024009

- Type-I shell evolution: number of nucleons in different isotopes
- Type-II shell evolution: occupancies within the same nucleus

From Ni to n-deficient Pb region



Contents

- Nuclear reactions
 - Types of reactions
 - Characteristics of direct reactions
- Why use transfer reactions
 - Information from reactions
 - Q-value, angular momentum, spectroscopic factors
- Reactions and RIBs
 - Motivations
 - Challenges: inverse kinematics
- **Case studies**
 - Light nuclei, $N=8$
 - The emergence of $N=16$
 - The spin-orbit term
 - Mg and Ni, the 0^+ s
 - ...

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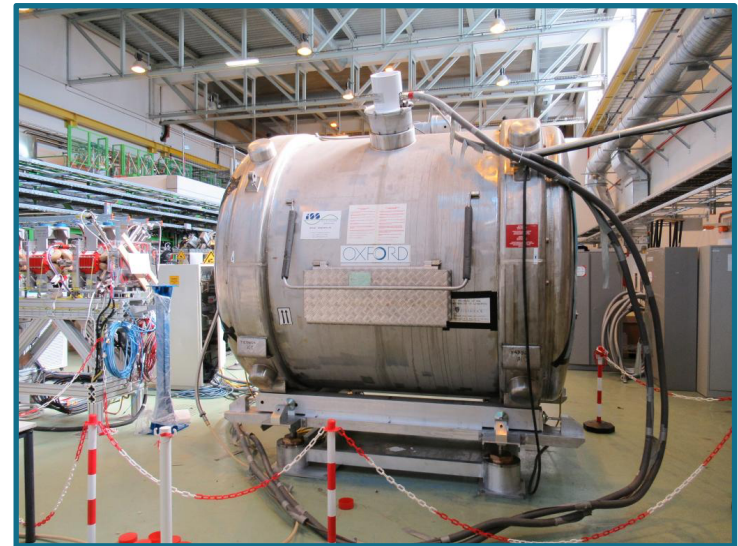
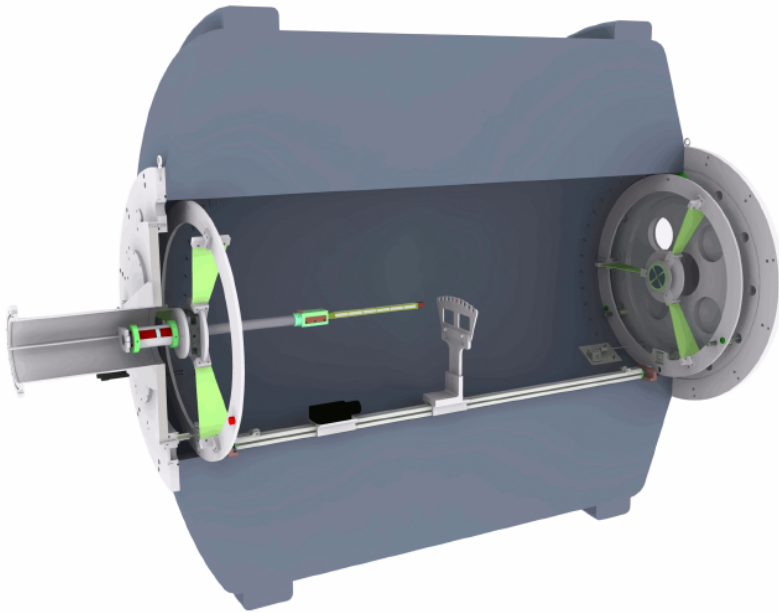
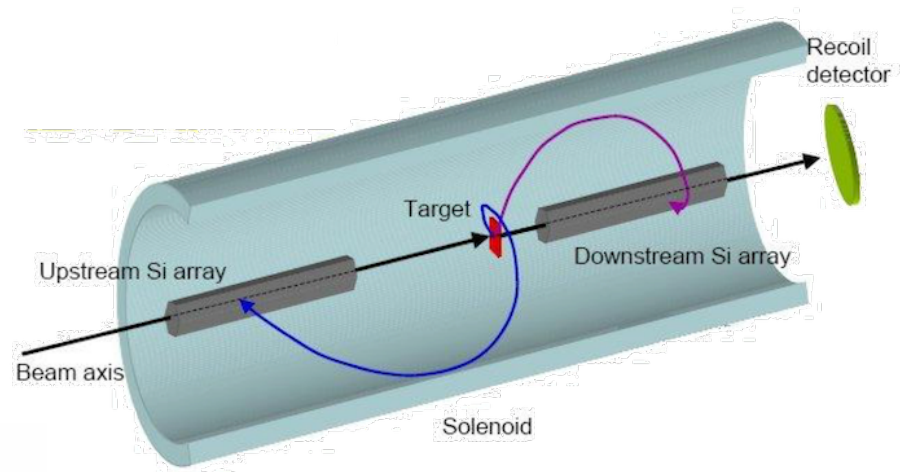
- Nuclear reactions
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 - **TRIUMF, GANIL, ISOLDE, Oak Ridge, Argonne...**

Improvements – Experimental side

Kinematic compression

- Solved by the HELIOS approach

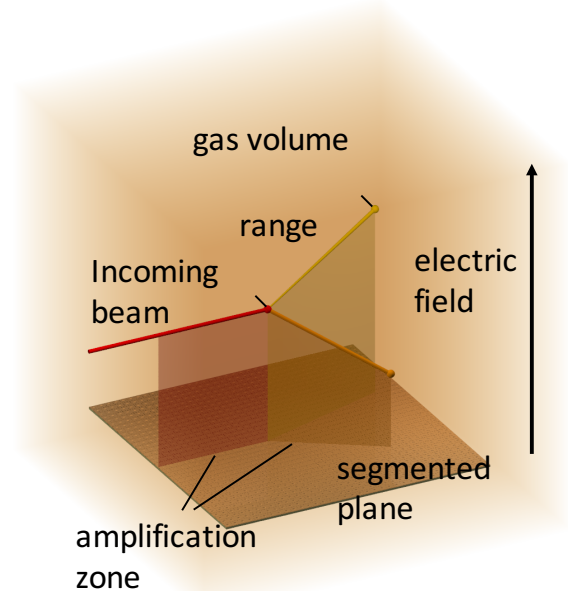
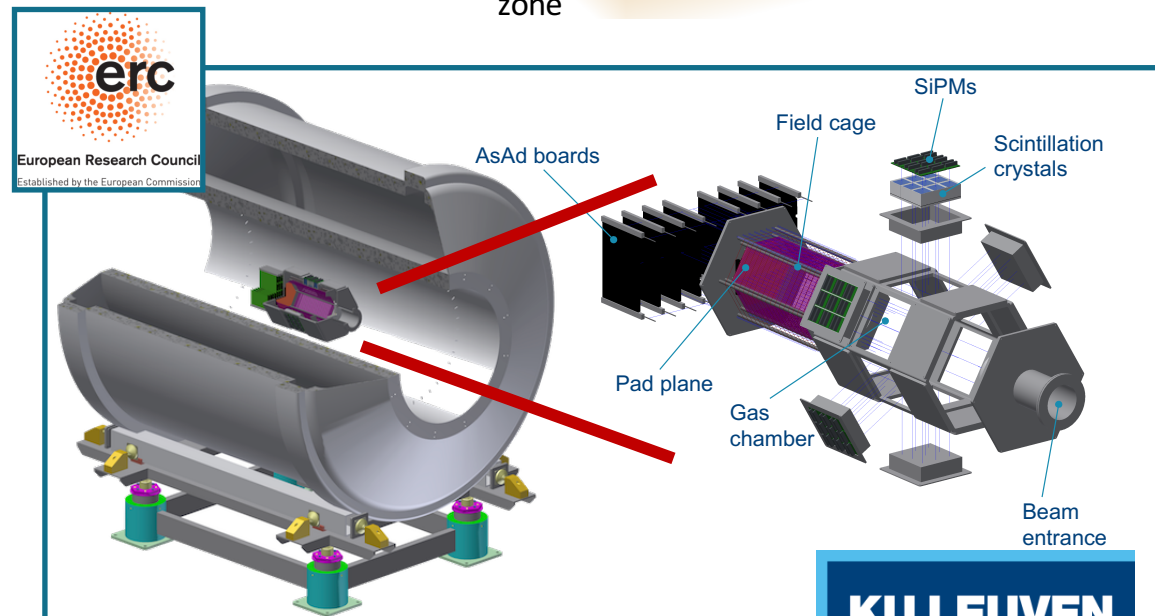
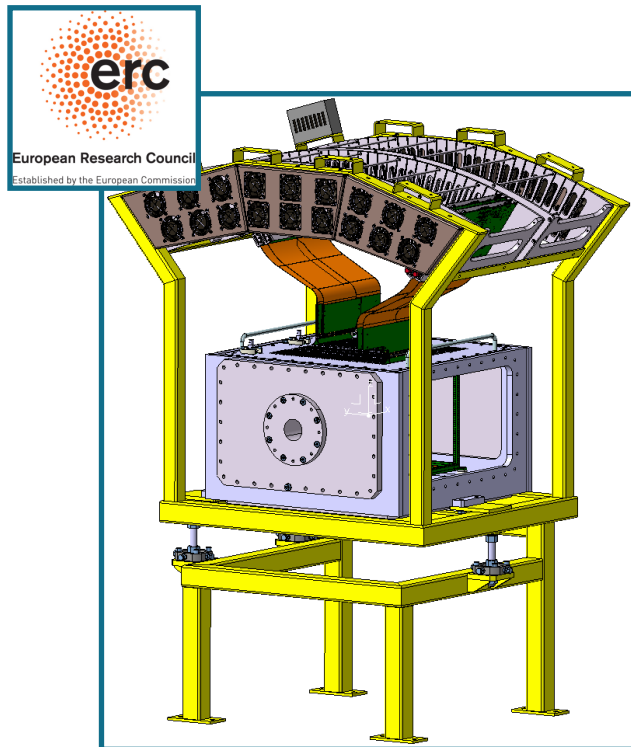
$$E_{\text{lab}} = E_{\text{cm}} - A + Bz$$
- At Argonne and soon at ISOLDE



Improvements – Experimental side

Target thickness vs resolution

- Solved by the Active Target approach
Large thickness but detection of the vertex
- ACTAR TPC, SpecMAT

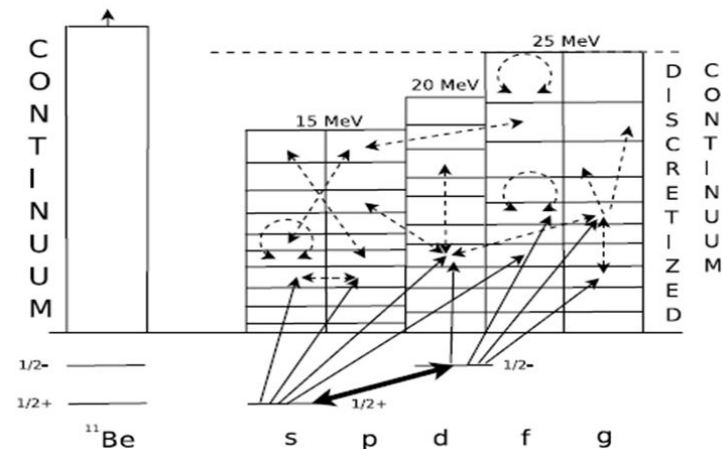


Improvements – Theoretical side

Reaction mechanism

- Weakly bound nuclei
 - Effects of extended matter distributions
 - Effects of continuum
- Transfer to the continuum
 - Spectroscopic factors?
- Multi-step processes
 - Importance at low energies
 - Include in calculations

Schematic representation of bound and continuum states and their couplings in CDCC calculations



Full lines: Hagino 2000.

Dashed lines: additional couplings by Diaz-Torres and Thompson 2002

...thank you for your attention!

