

# The $f_{7/2}$ shell: *an optimum test bench*

Silvia M. Lenzi

*Department of Physics and Astronomy “Galileo Galilei”  
University of Padova and INFN*



R. A. RICCI, *et al.*  
Aprile-Giugno 1969  
*Rivista del Nuovo Cimento*  
Serie I, Vol. 1, pag. 291-354

R. A. RICCI - P. R. MAURENZIG

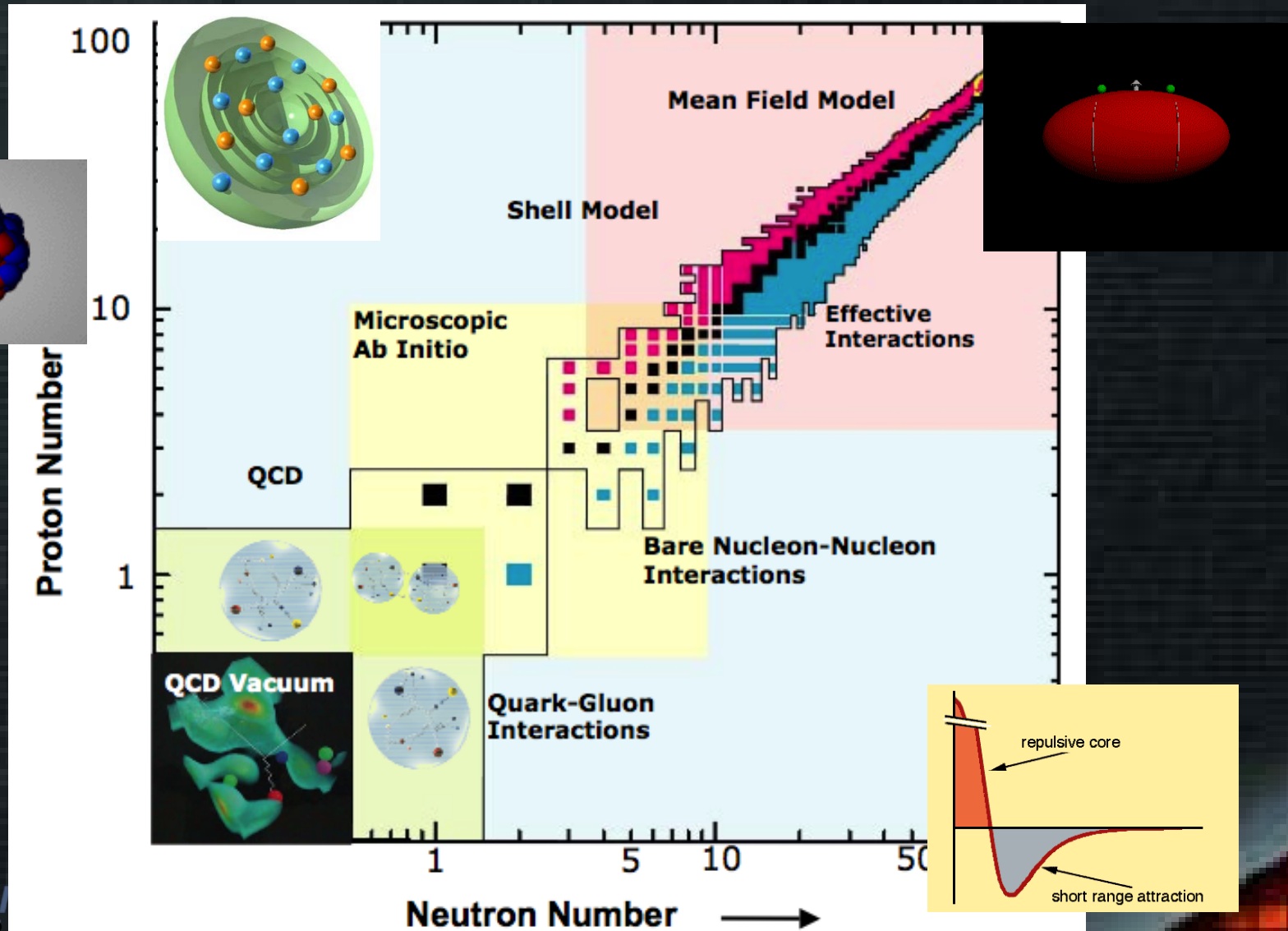
**The  $1/3$  Problem in Nuclear Spectroscopy.**

“One of the main problems in low-energy nuclear physics is the derivation of the various properties of nuclei from the realistic forces deduced from the free nucleon-nucleon interaction”

BOLOGNA  
TIPOGRAFIA COMPOSITORI  
1969



# The nuclear models



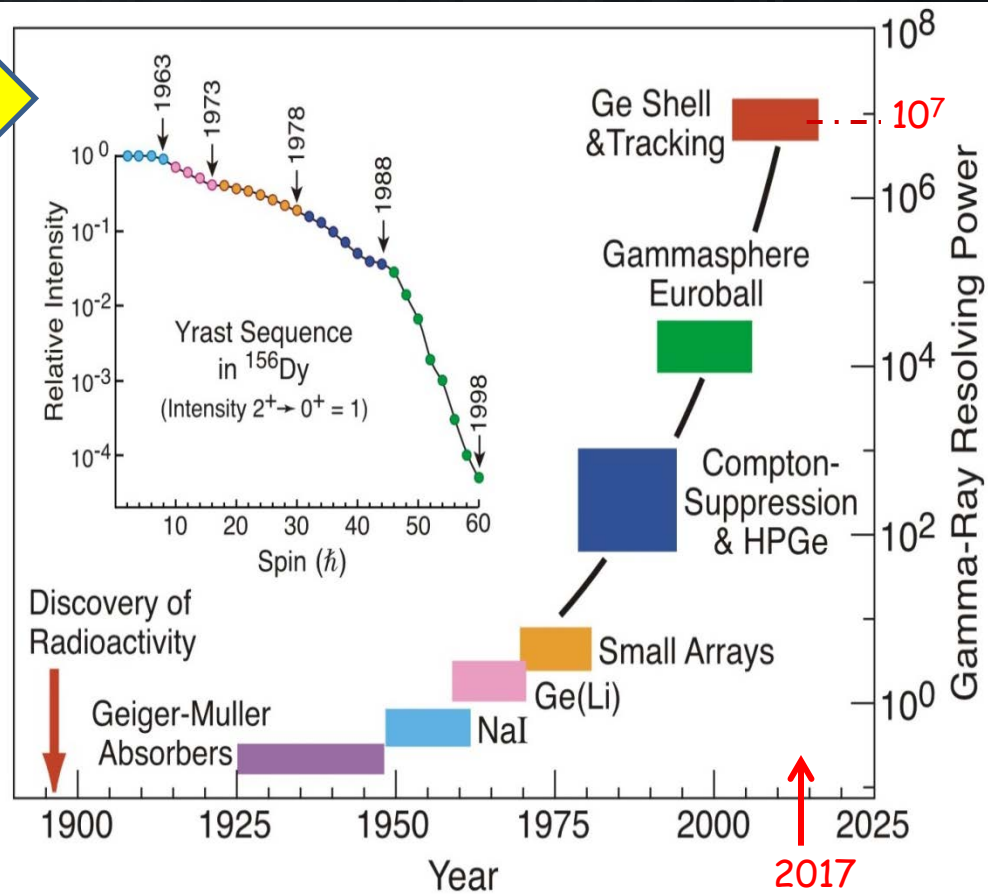


# From the experimental side

A continuous development in gamma spectroscopy

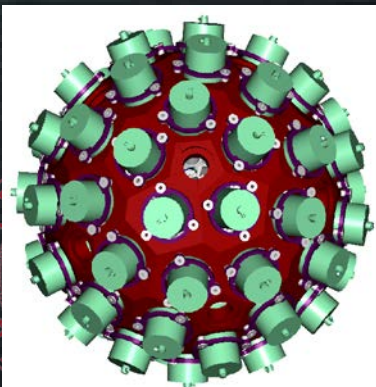
- NaI(Tl) detectors in the 60's
- Ge detectors of the 70's
- HPGe arrays of the 80-90's
- the large spectrometers of the late 90's (EUROBALL, GAMMASPHERE)
- the tracking Ge-arrays (**AGATA**, **GRETA**) of present days

Development in terms of the evolution of the observational limit (the inverse of the resolving power).



Unprecedented performance due to:

- ☐ segmented detectors
- ☐ pulse-shape analysis
- ☐ tracking the g rays
- ☐ digital electronics





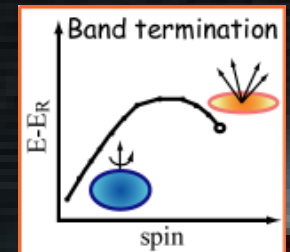
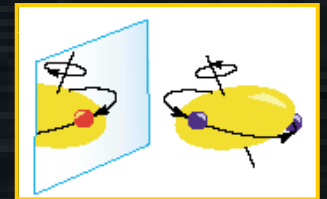
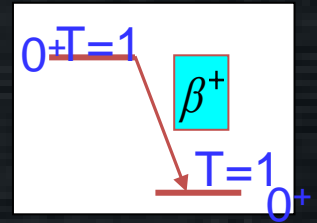
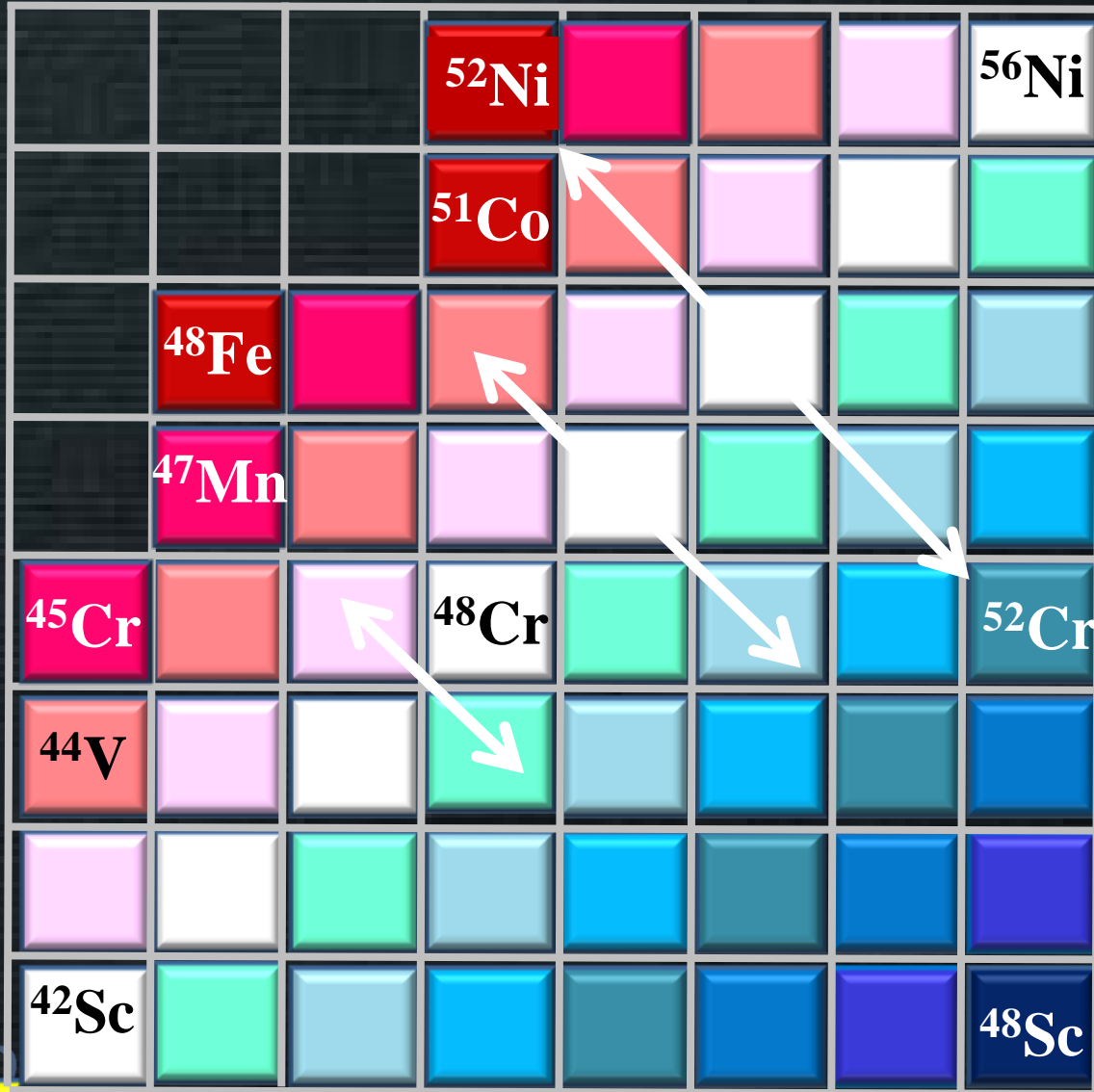
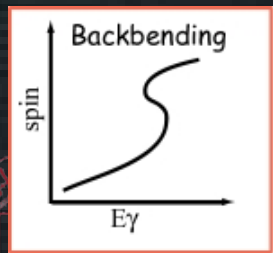
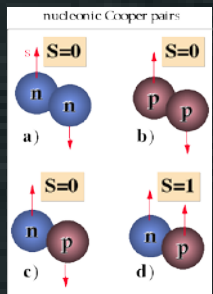
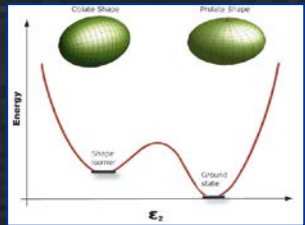
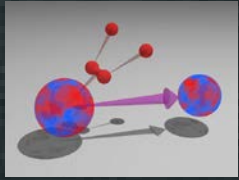
# The $f_{7/2}$ shell an optimum test bench

Isospin symmetry breaking in neutron-deficient nuclei

Development of deformation in neutron-rich nuclei



# High spin states in $f_{7/2}$ -shell nuclei



**$^{40}\text{Ca}$**

Nazionale  
Nucleare

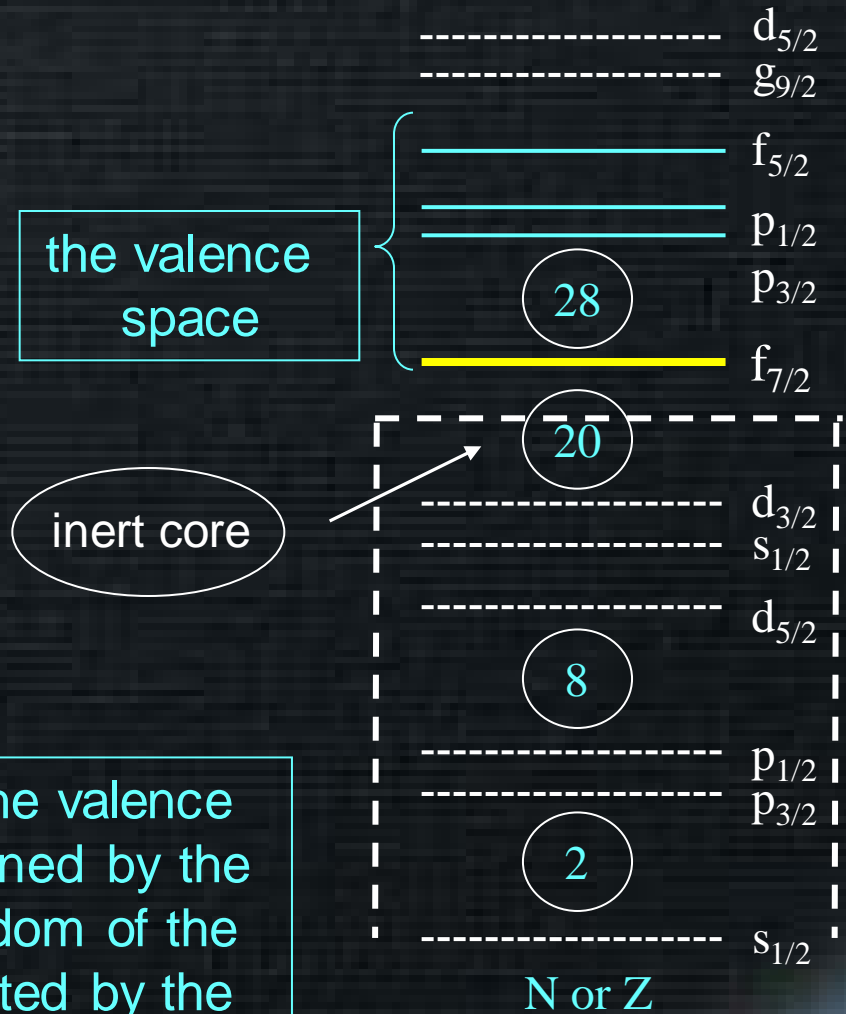
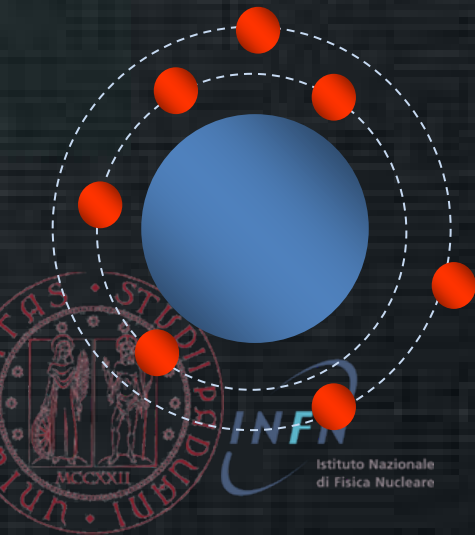


# Ingredients for Shell Model calculations

- 1) an inert core
- 2) a valence space
- 3) an effective interaction that mocks up the general hamiltonian in the restricted basis

$$H_{\text{eff}}\psi_{\alpha} = H_0 + V_{\text{eff}}\psi_{\alpha} = E_{\alpha}\psi_{\alpha}$$

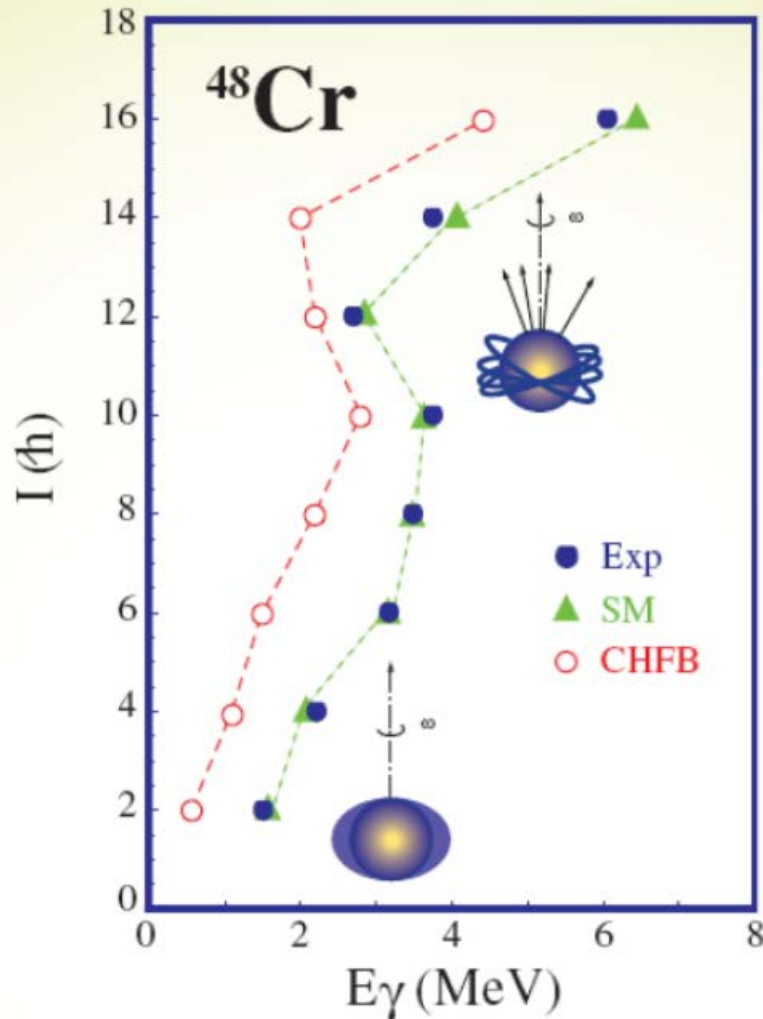
with  $H_0 = T + U$



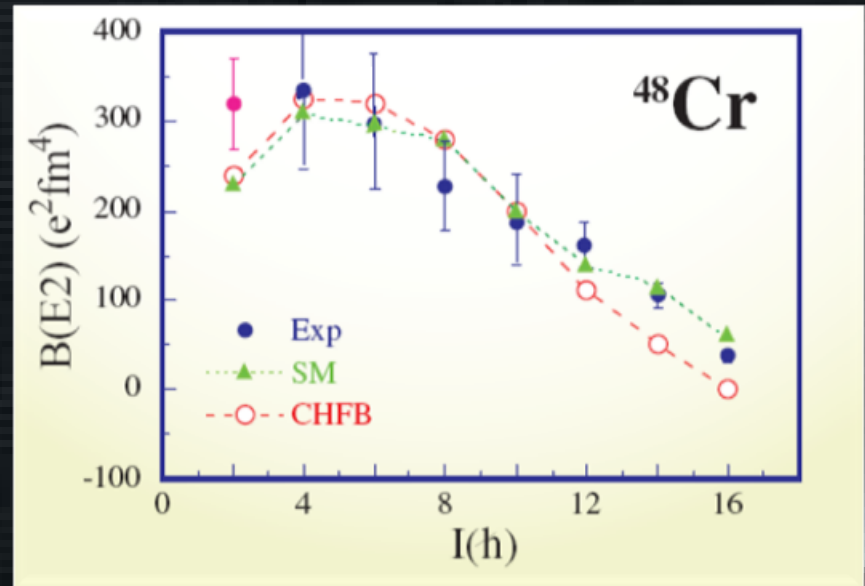
The choice of the valence space is determined by the degrees of freedom of the system and limited by the dimensions of the matrices to be diagonalized



# Shell model and collective phenomena



Shell model calculations in the full fp shell give an excellent description of the structure of collective rotations in nuclei of the  $f_{7/2}$  shell



Theory: E. Caurier et al., Phys.Rev.Lett.75(1995)225

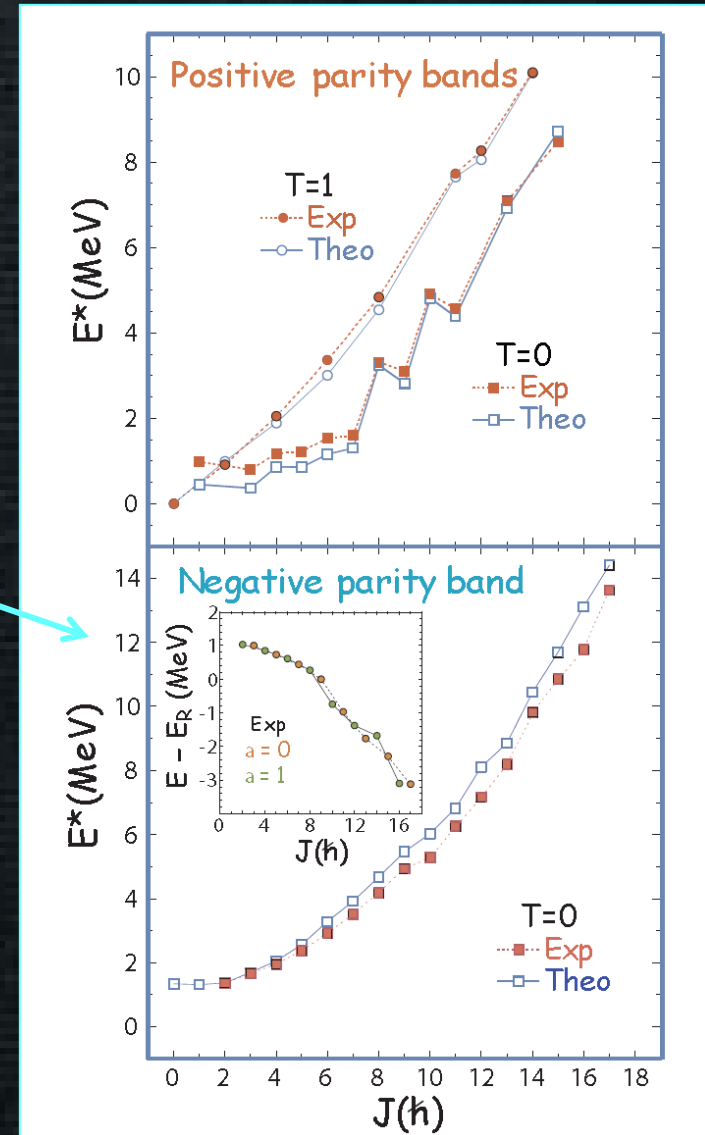
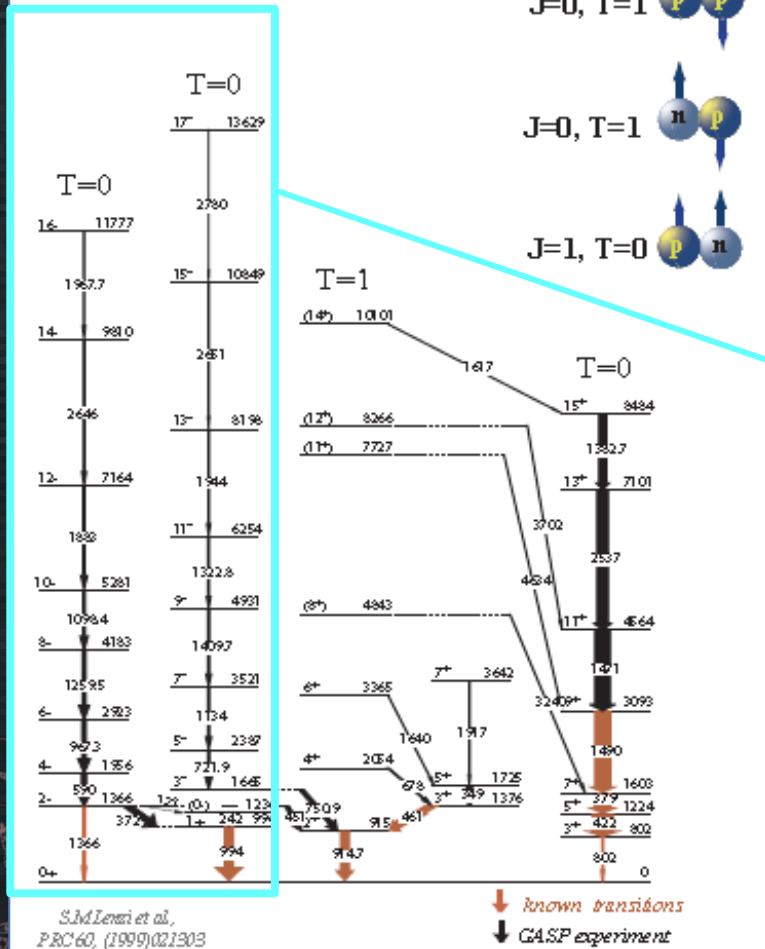
Experiments: S. M. Lenzi et al., Z.Phys.A354(1996)117 - F. Brandolini et al., Nucl.Phys.A642(1998)387



# Shape coexistence in N=Z

## Proton-neutron pairing correlations in the odd-odd N = Z nucleus

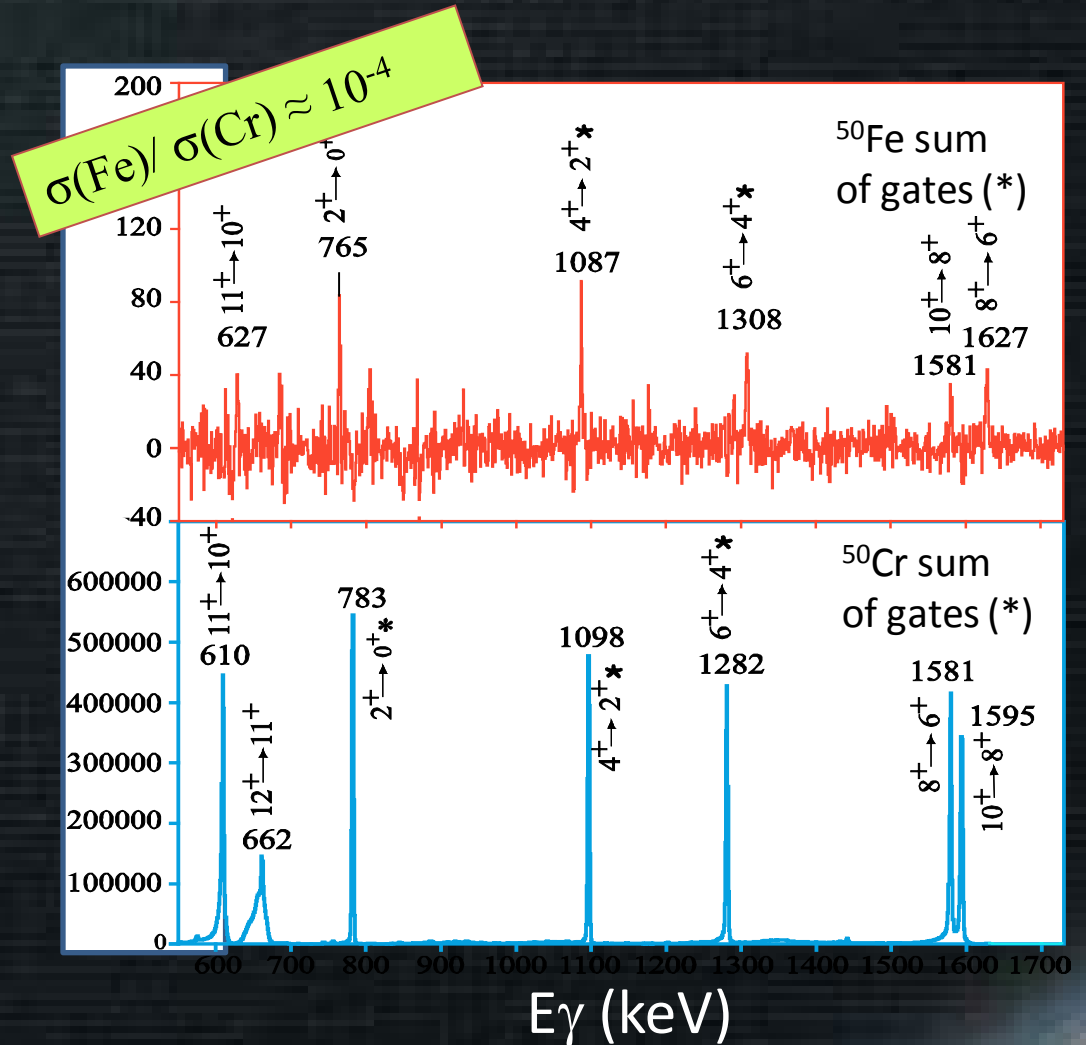
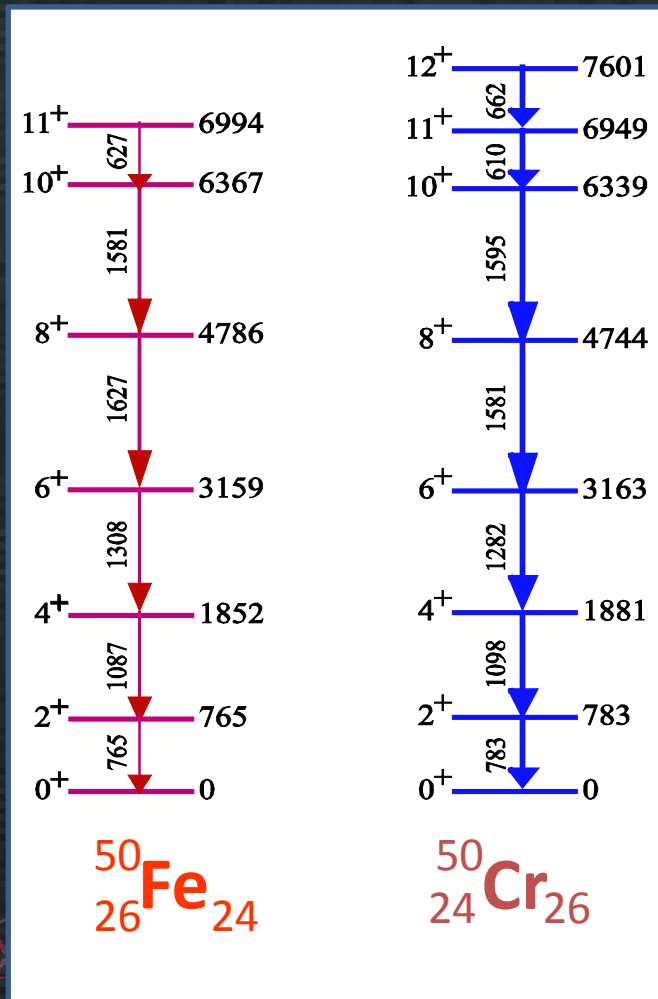
$^{46}\text{V}$





# First observation of excited states in $^{50}\text{Fe}$

The mirror pair  $A=50$



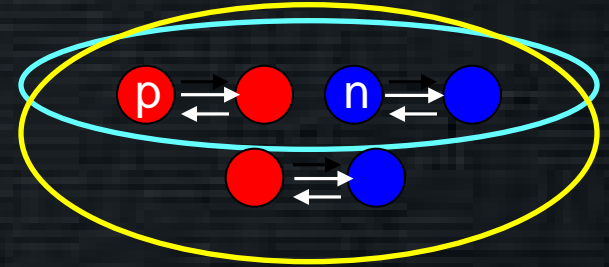
EUROBALL + EUCLIDES + NWALL

SML et al., Phys. Rev. Lett. 87, 122501 (2001)



# Neutron-proton exchange symmetry

Charge symmetry :  $V_{pp} = V_{nn}$



Charge independence:  $(V_{pp} + V_{nn})/2 = V_{np}$

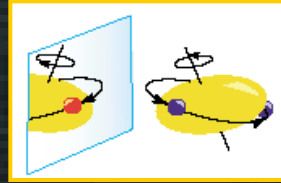
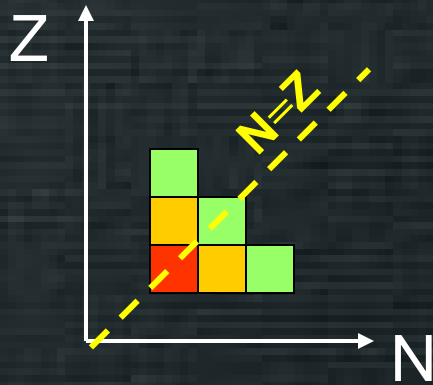
Deviations are small

Electromagnetic interactions lift the degeneracy of the analogue states, but do not generally affect the underlying symmetry.





# Differences in analogue excited states



Mirror Energy Differences (MED)

$$\text{MED}_J = Ex_{J, T_z = -T} - Ex_{J, T_z = +T}$$

Test the **charge symmetry** of the interaction



Triplet Energy Differences (TED)

$$\text{TED}_J = Ex_{J, T_z = -T} + Ex_{J, T_z = +T} - 2Ex_{J, T_z = 0}$$

Test the **charge independency** of the interaction



# Measuring MED and TED

Can we reproduce such small energy differences?  
What can we learn from them?

They contain a richness of information  
about spin-dependent structural phenomena

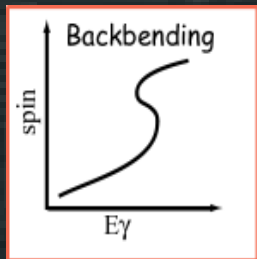
We measure **nuclear** structure features:

- How the nucleus generates its angular momentum
- Evolution of radii (deformation) along a rotational band
- Learn about the configuration of the states
- Isospin non-conserving terms of the interaction

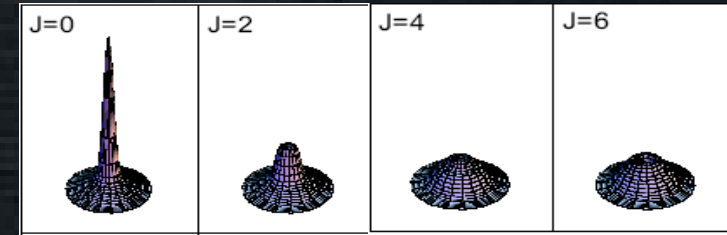




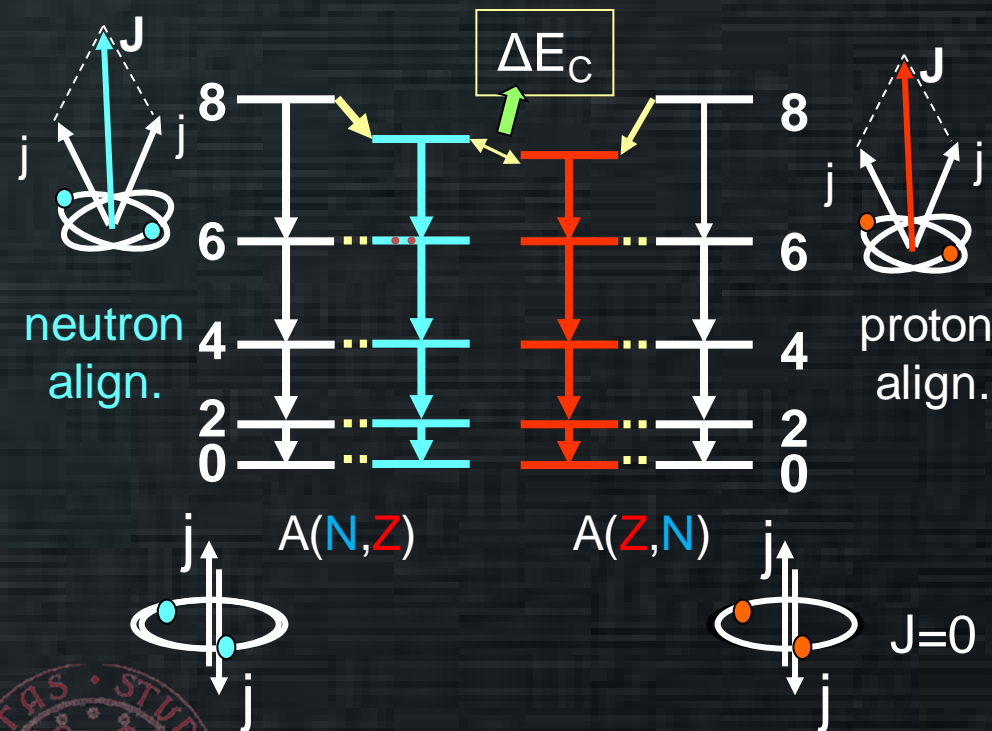
# MED and nucleon spatial correlations



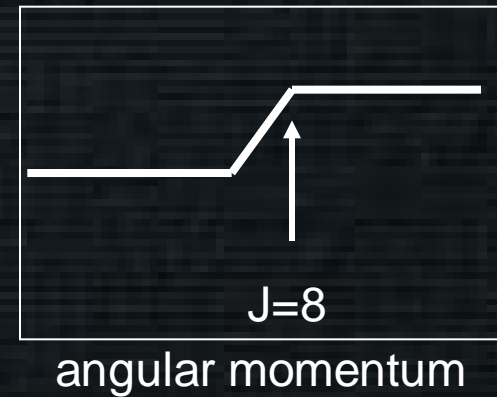
probability distribution for the relative distance of two like particles in the  $f_{7/2}$  shell



courtesy P. Van Isacker



MED

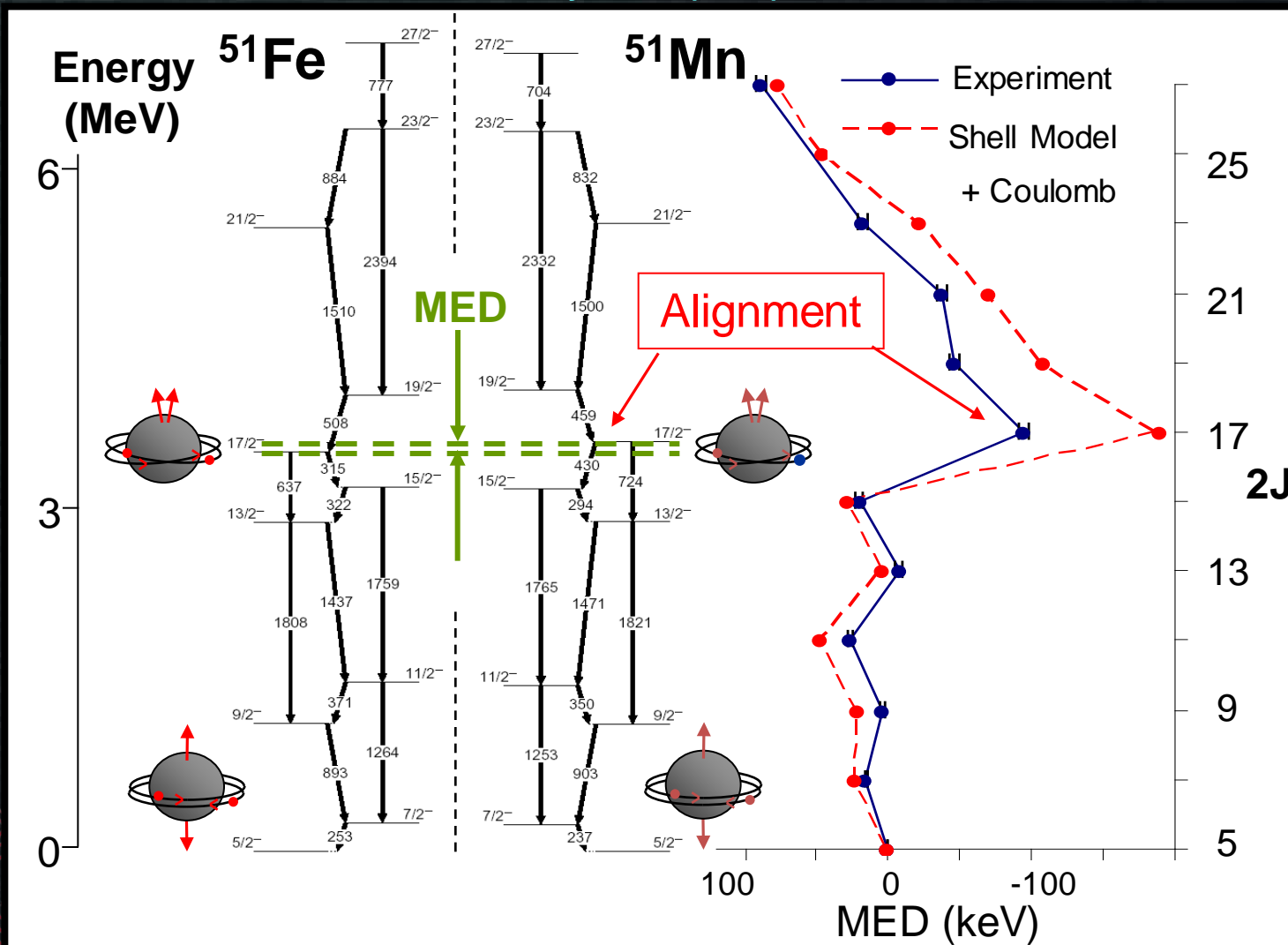


Shifts between the excitation energies of the mirror pair at the backbending indicate the type of nucleons that are aligning



# MED and nucleon alignment

D.D. Warner, M.A. Bentley and P. Van Isacker,  
Nature Physics 2 (2006) 311





# The effective interaction

A multipole expansion

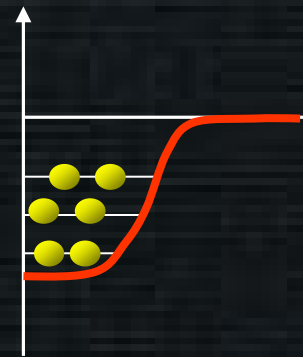
$$V = V_m + V_M$$

monopole

Multipole

$V_m$

- represents a spherical mean field extracted from the interacting shell model
- determines the single particle energies or ESPE

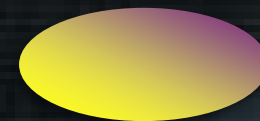


$V_M$

- correlations
- energy gains



Deformation





# Coulomb effects

$V_{CM}$  Multipole term

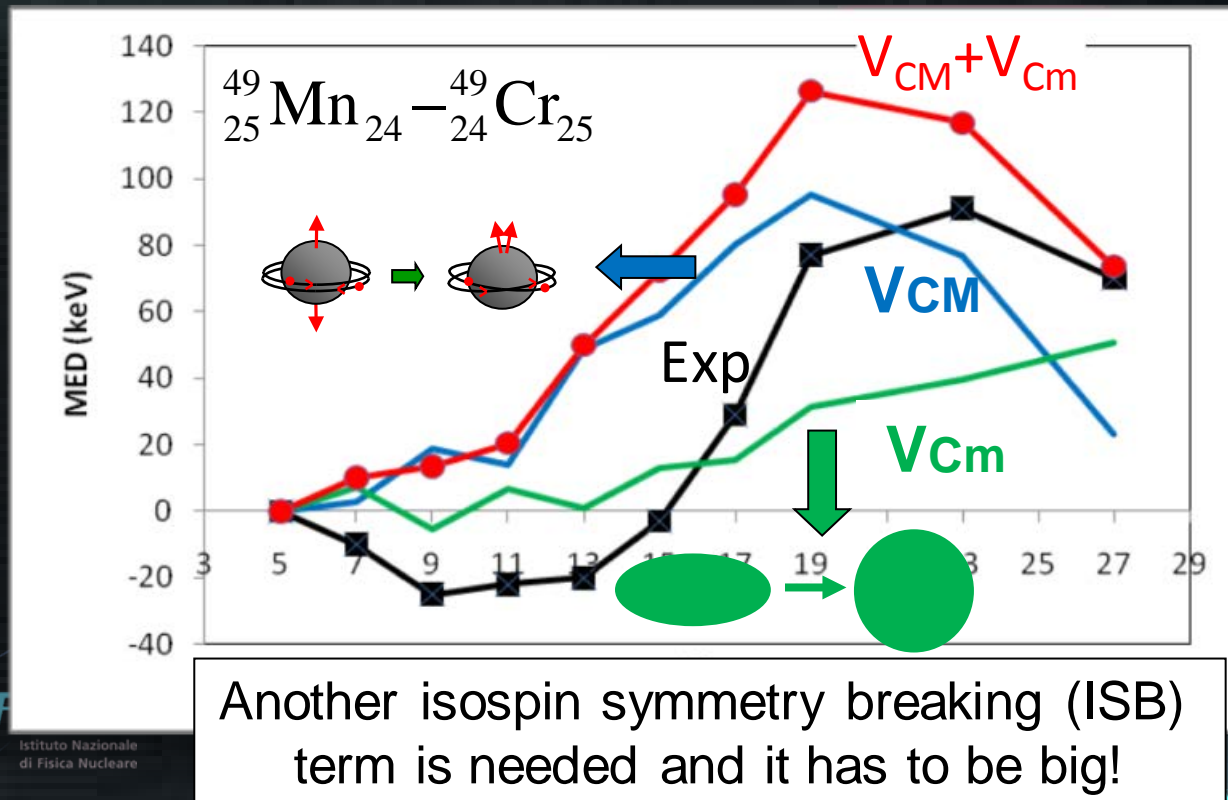
between valence  
protons only

sensitive to  
nucleon recoupling

$V_{Cm}$  Monopole term

$$E_c = \frac{3}{5} \frac{e^2 Z(Z-1)}{R}$$

radial effect:  
radius changes with J





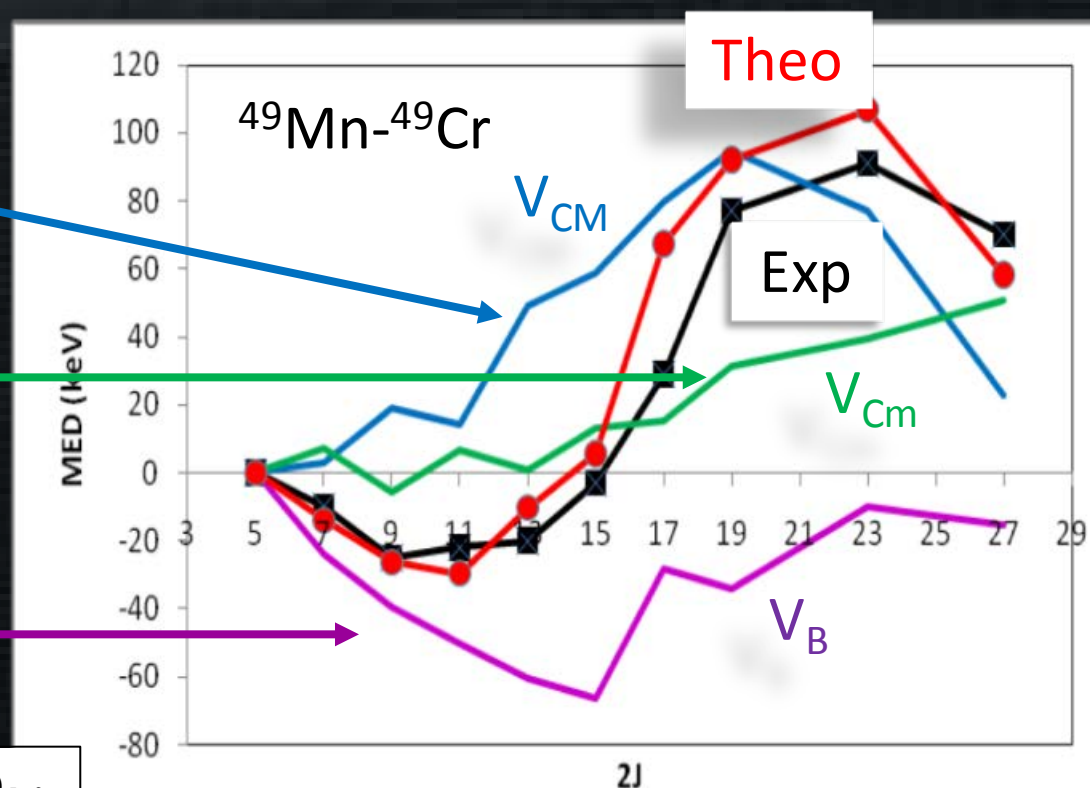
# Calculating the MED with SM

$$MED_J^{theo} = \Delta\langle V_{Cm} \rangle_J + \Delta\langle V_{CM} \rangle_J + \Delta\langle V_B \rangle_J$$

**VCm:** gives information on the nucleon alignment or recoupling

**VCm:** gives information on changes in the nuclear radius

The ISB  $V_B$  term is of the same order as the Coulomb contributions



$$\Delta\langle V_B \rangle = +100 \text{ keV} (V_{\pi\pi}^{(f_{7/2}^2)_{J=2}} - V_{\nu\nu}^{(f_{7/2}^2)_{J=2}})$$

$$V_{xx}^{(f_{7/2}^2)_{J=2}}$$

interaction of one single unitary matrix element for two nucleons in the  $f_{7/2}$  coupled to  $J=2$

*A. P. Zuker et al., PRL 89, 142502 (2002)*



# Calculating MED and TED

We rely on **isospin-conserving shell model wave functions** and obtain the energy differences in first order perturbation theory as sum of expectation values of the **Coulomb** ( $V_C$ ) and **ISB** ( $V_B$ ) interactions

$$MED_J^{\text{exp}} = E_J^*(Z_>) - E_J^*(Z_<)$$

$$MED_J^{\text{theo}} = \Delta_M \langle V_{Cm} \rangle_J + \Delta_M \langle V_{CM} \rangle_J + \Delta_M \langle V_B^{(1)} \rangle_J$$

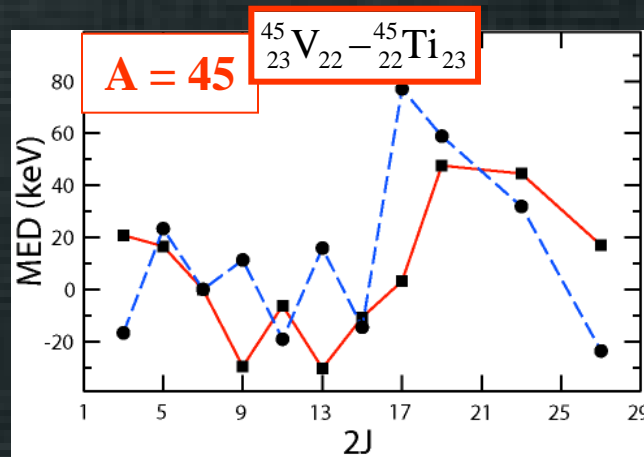
$$TED_J^{\text{exp}} = E_J^*(Z_>) + E_J^*(Z_<) - 2E_J^*(N = Z)$$

$$TED_J^{\text{Theo}} = \Delta_T \langle V_{CM} \rangle_J + \Delta_T \langle V_B^{(2)} \rangle_J$$

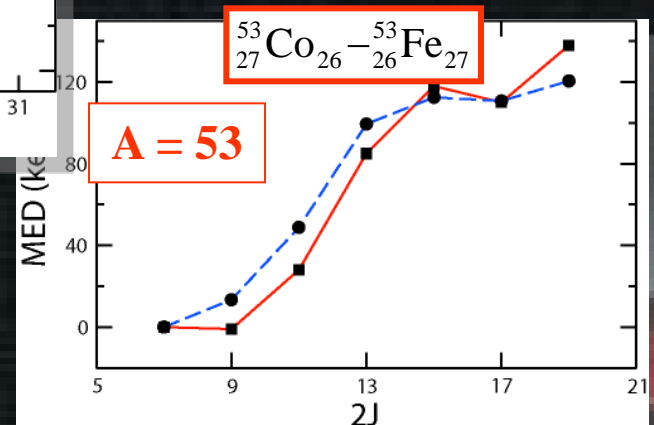
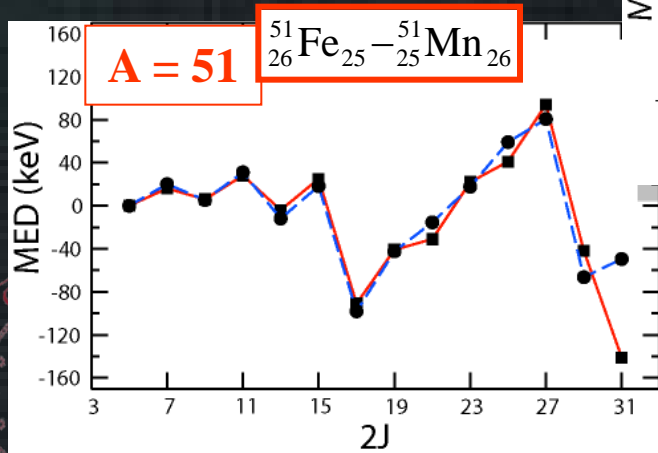
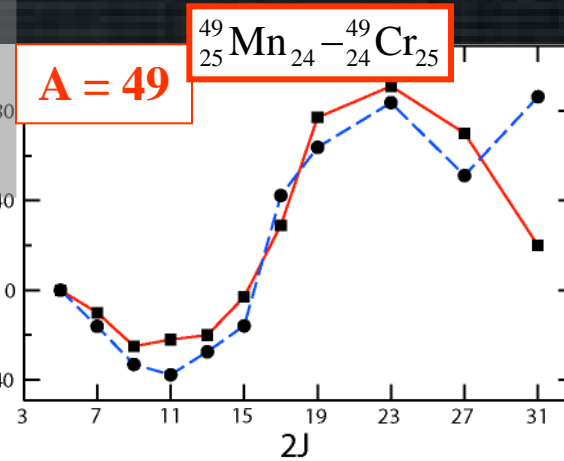
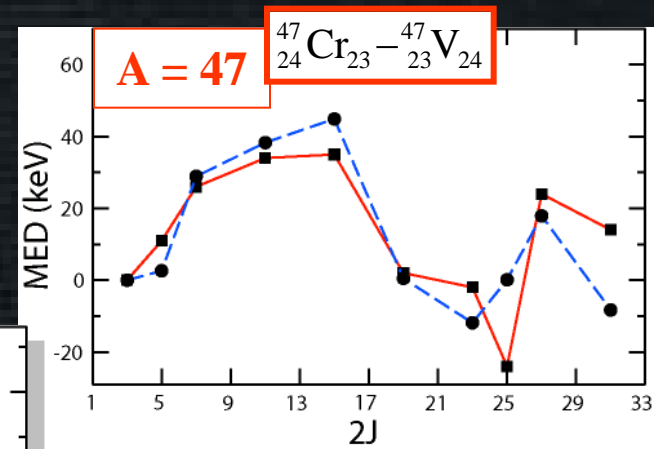


# MED in T=1/2 states

Very good quantitative description of data without free parameters



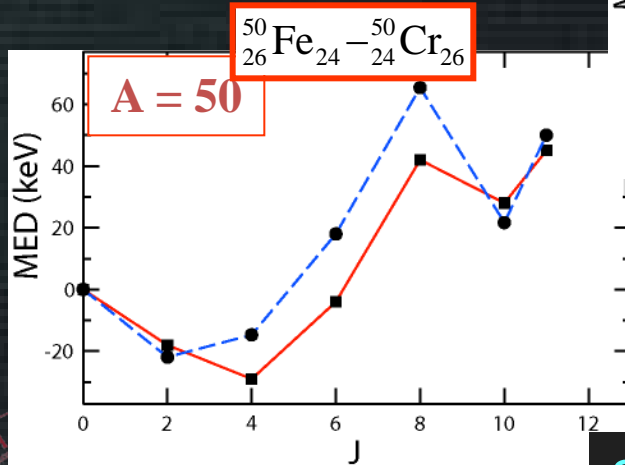
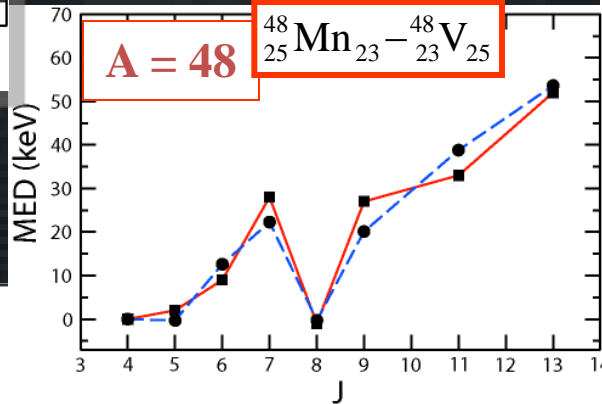
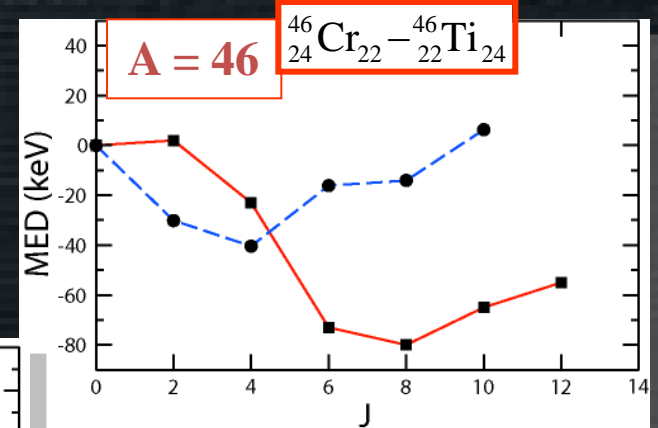
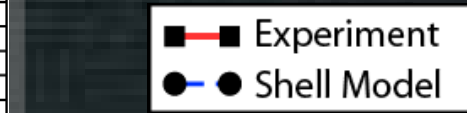
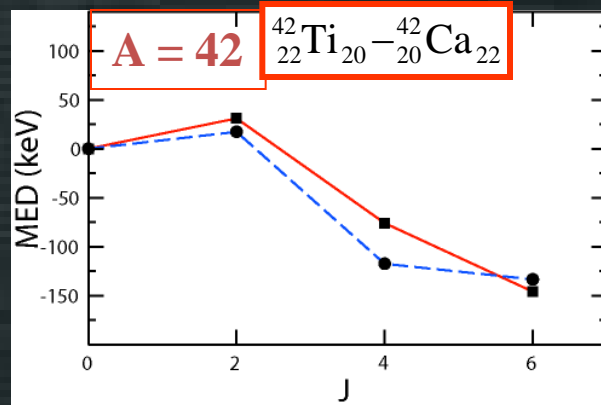
■ Experiment  
● Shell Model



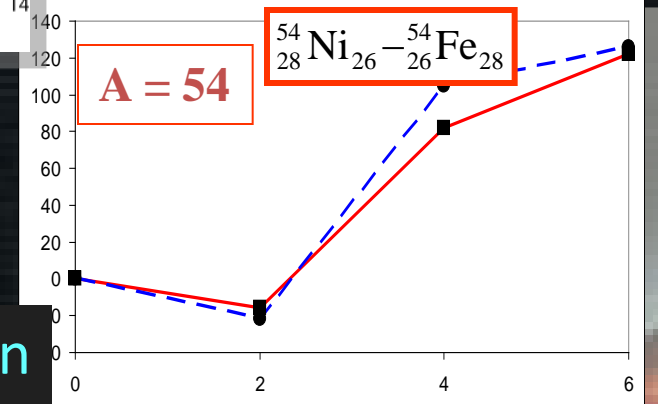
M.A. Bentley and SML,  
Prog. Part. Nucl. Phys. 59,  
497-561 (2007)



# MED in T=1 states



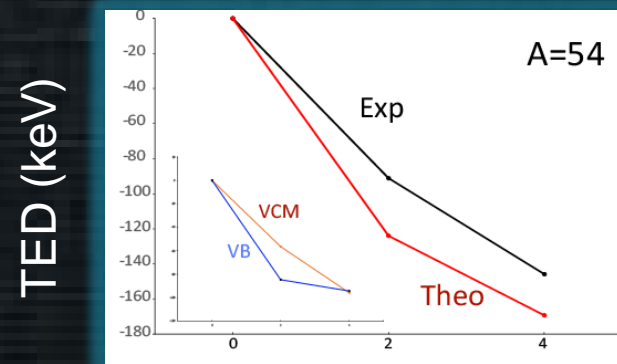
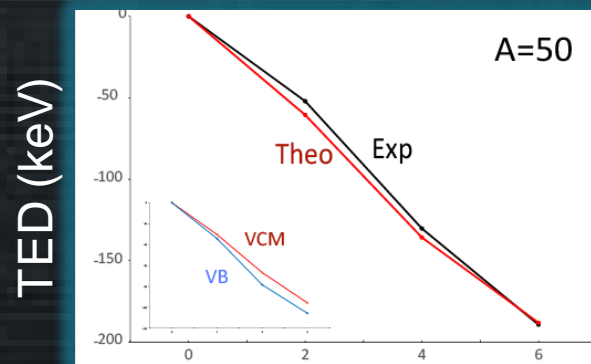
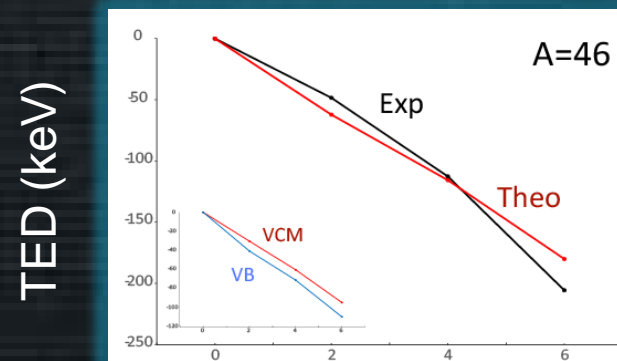
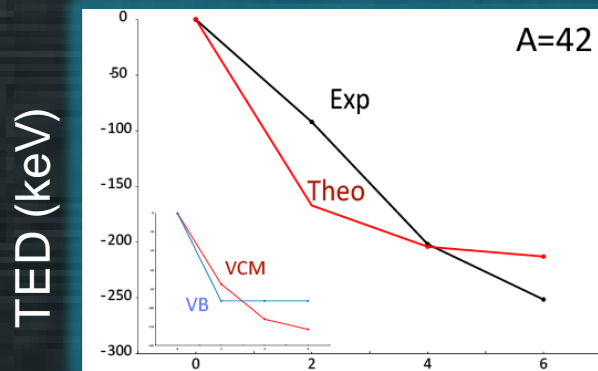
M.A. Bentley and SML,  
PPNP 59, 497(2007)



Same parameterization  
for the whole  $f_{7/2}$  shell!



# TED in the $f_{7/2}$ shell



Only multipole effects are relevant.

The ISB term VB is of the same magnitude of the Multipole Coulomb term

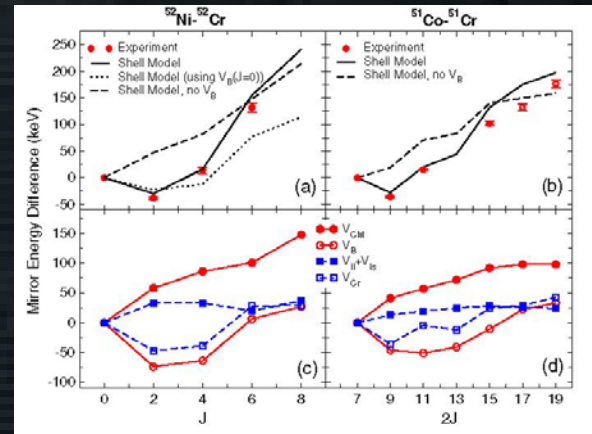




# Some questions arise...

What happens farther from stability  
or at larger  $T$  in the  $f_{7/2}$  shell?

The same prescription applies



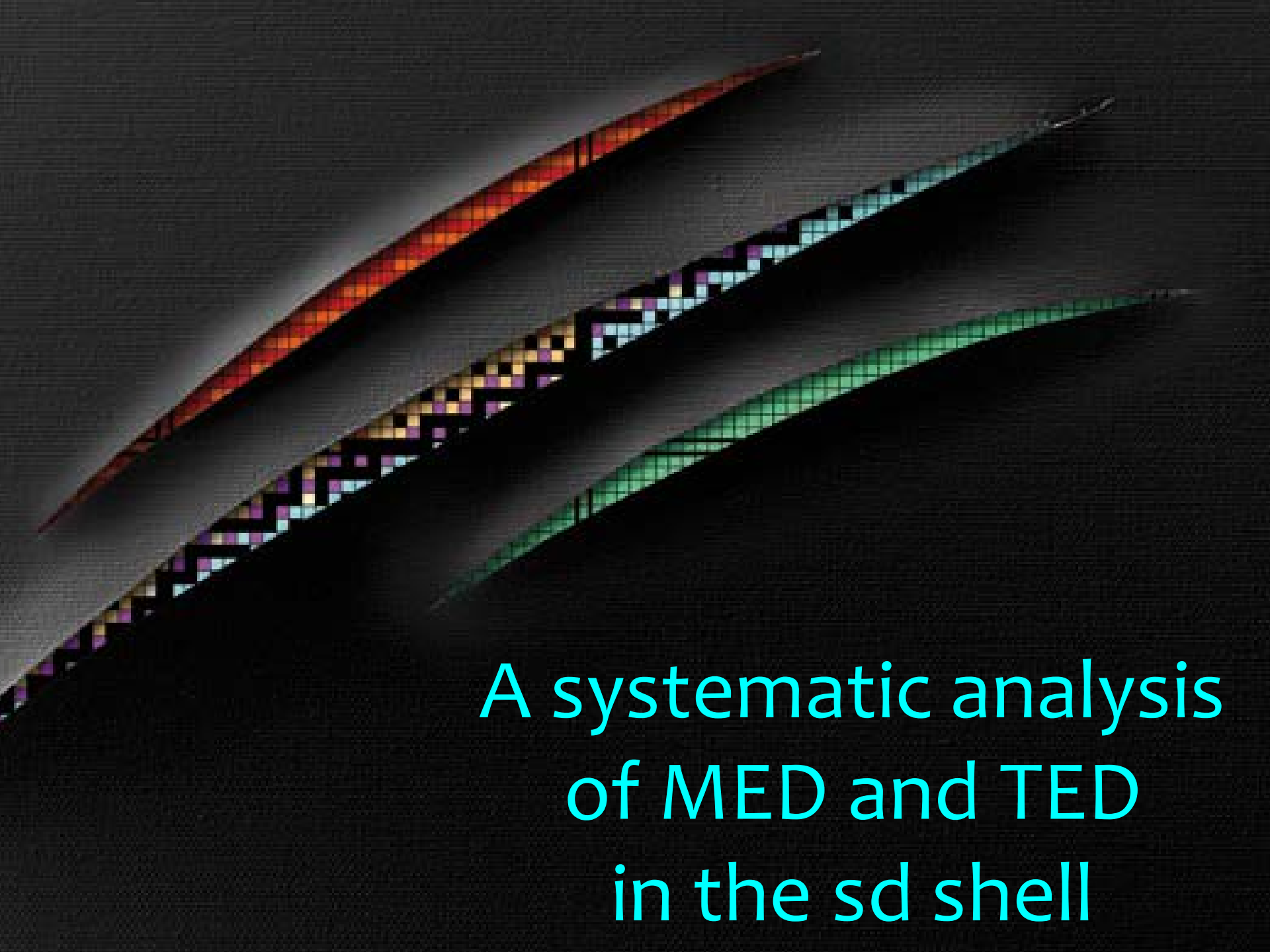
Is the ISB VB term confined to the  $f_{7/2}$  shell  
or is a general feature?

If so the same prescription should work

Can we understand the origin of the VB term?

Work in progress...

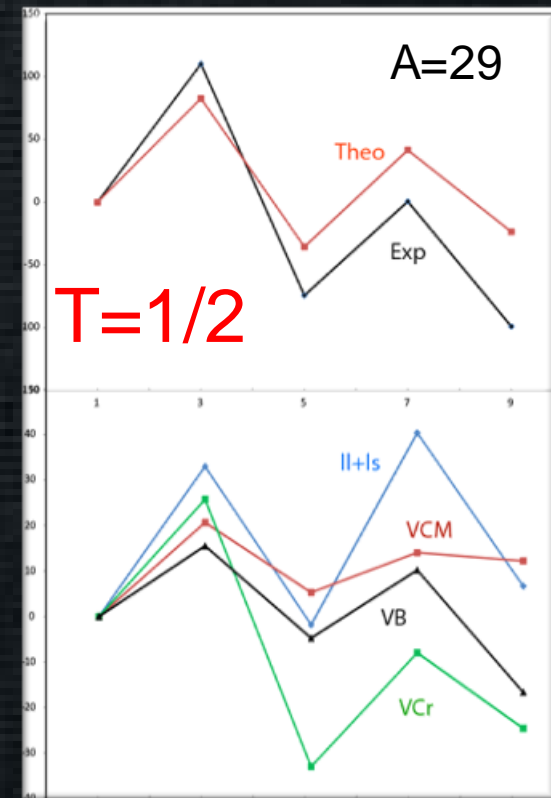
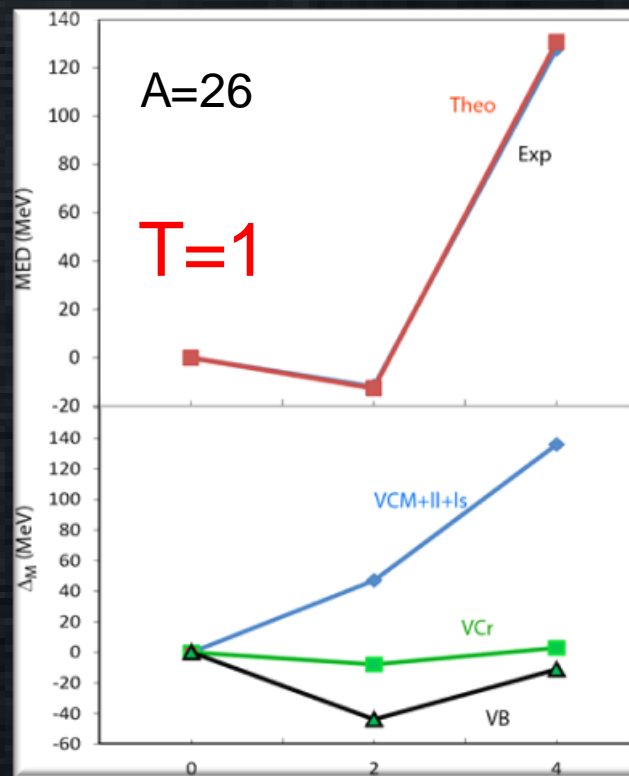
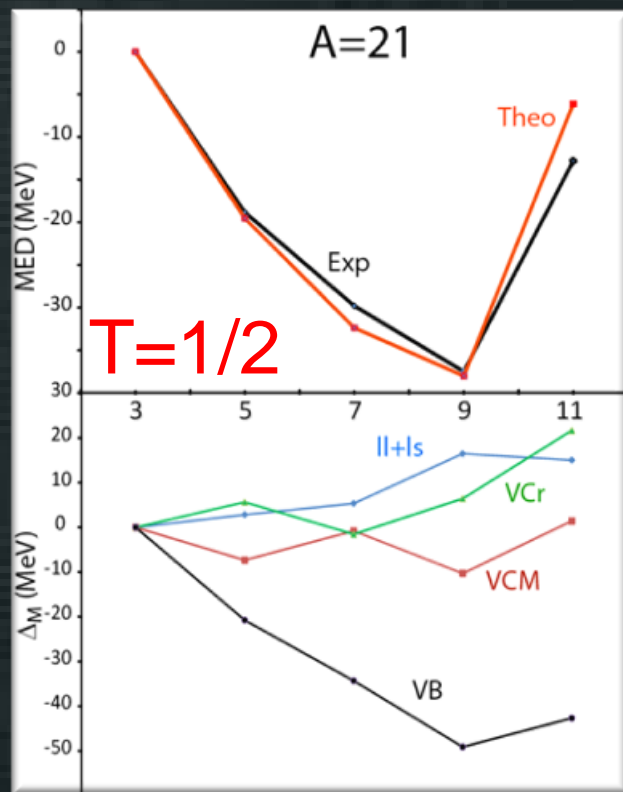




A systematic analysis  
of MED and TED  
in the sd shell



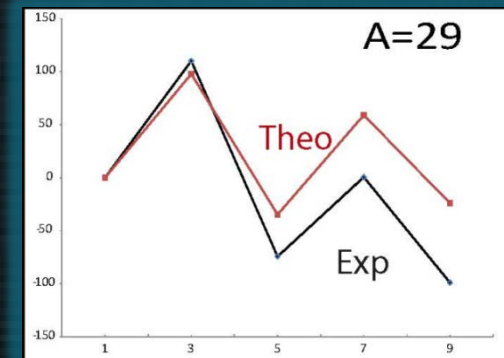
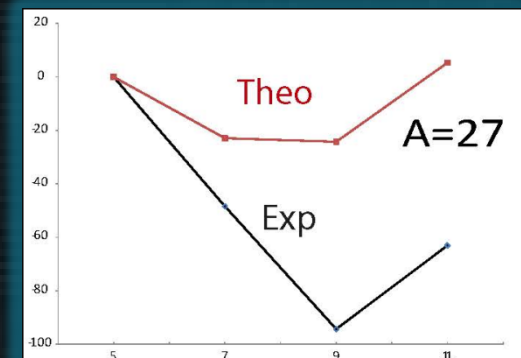
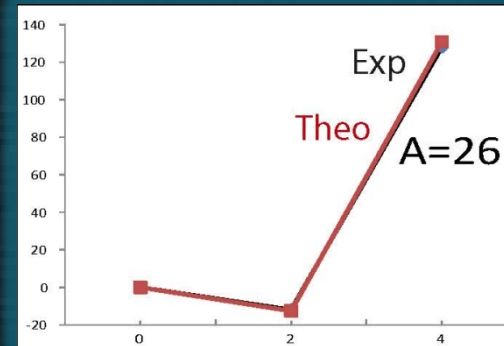
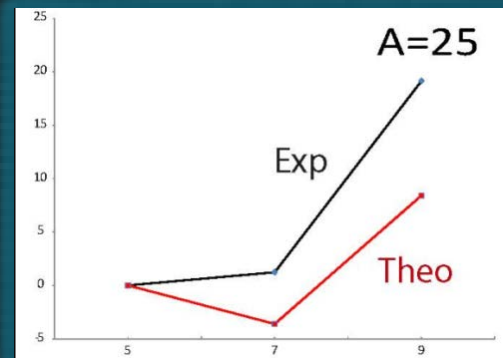
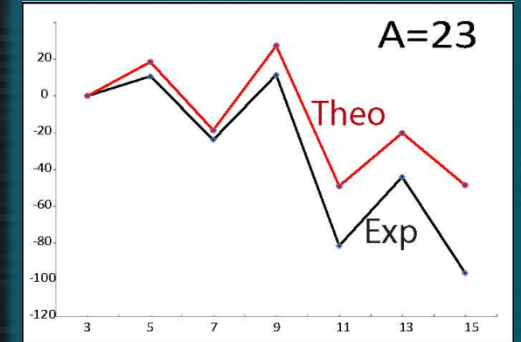
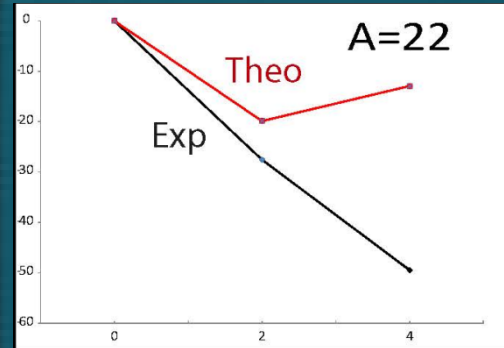
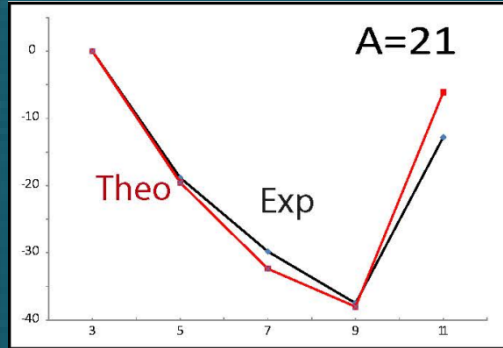
# MED: different contributions





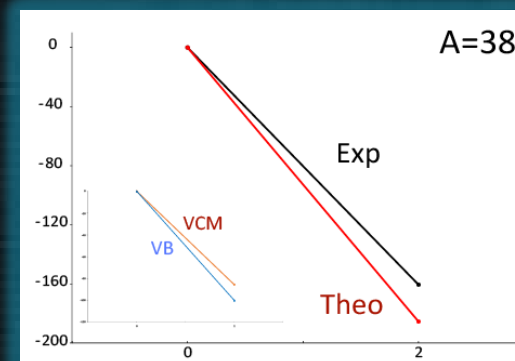
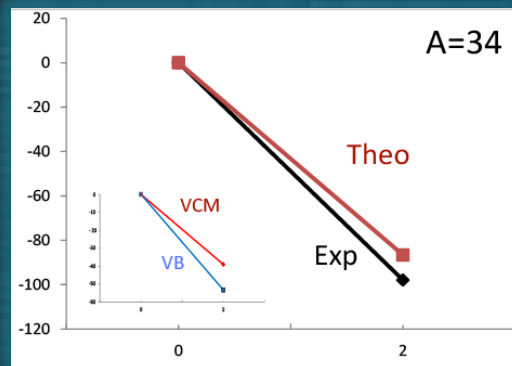
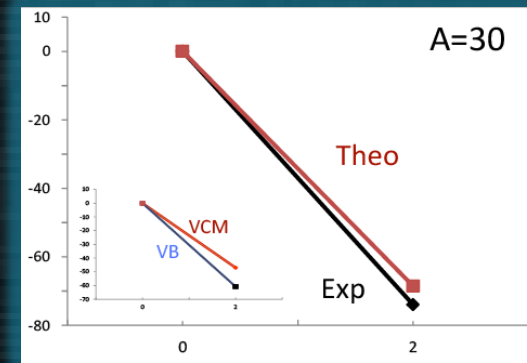
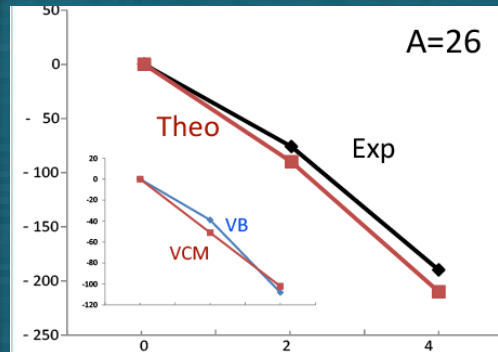
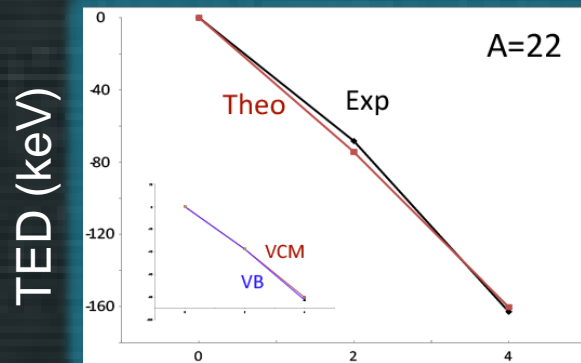
# MED in the sd shell

MED (keV)





# TED in the sd shell



The prescription applies successfully also in the sd shell!

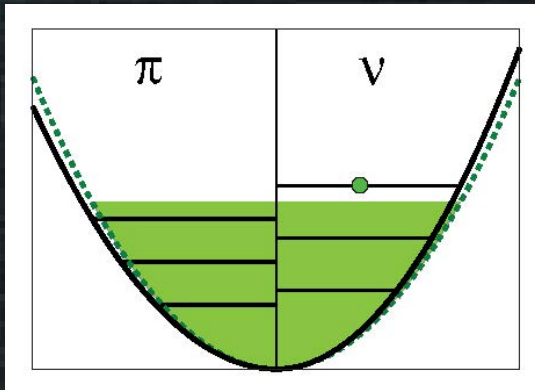




# Understanding ISB

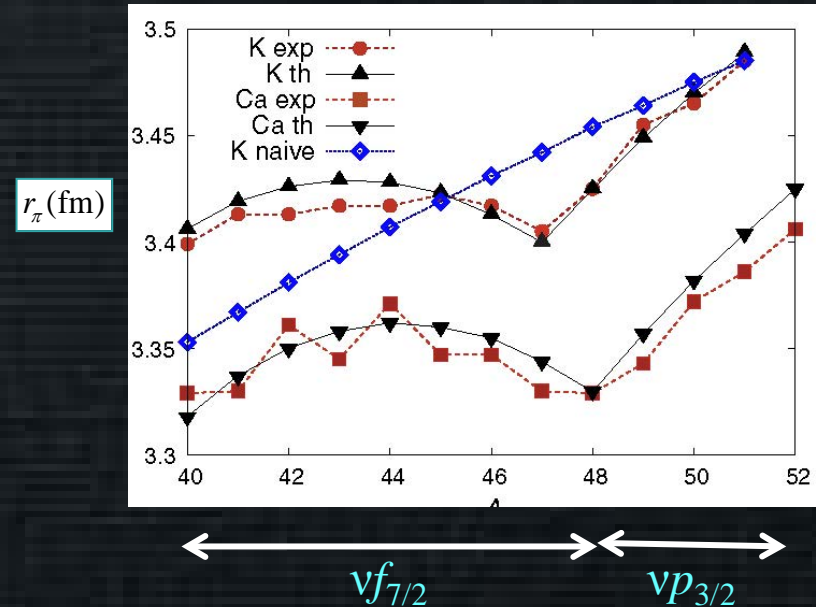
We have used a new interaction **MCI** deduced from the realistic nucleon-nucleon **N3LO** in a **no-core approach**, that includes both **Coulomb** and **ISB** nuclear interaction

An important effect to consider is the isovector polarizability



which induces changes in the potential wells of protons and neutrons

Charge radii in Ca and K isotopes



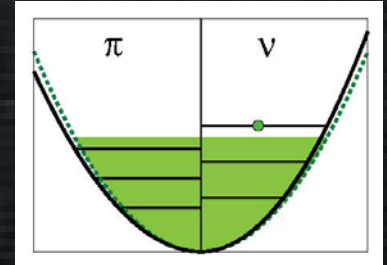
Proton radii increases when filling with neutrons the  $p_{3/2}$  shell!

J. Bonnard et al.,  
PRL 116, 212501 (2016)



# Constructing the matrix elements

We need to determine the size of the potential wells where to calculate the matrix elements of the effective interaction, different for protons and neutrons!



**How do we proceed?** The well is directly related to the nuclear radius

We know the charge radius of the neutron-rich partner, which due to isospin symmetry is the same as the neutron radius of its mirror

measured!

$$r_{\pi}(N > Z) = r_{\nu}(N < Z)$$

**We also know the difference in binding energy of the g.s. of the two mirrors**

These two observables allow to obtain

$$r_{\pi}(N < Z) = r_{\nu}(N > Z)$$

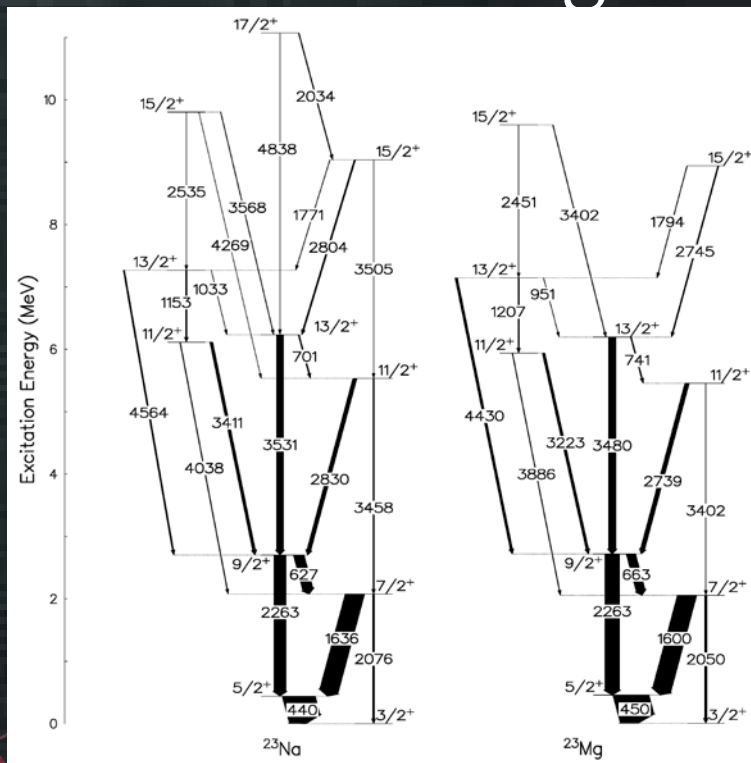
and thus the size of the two wells and the nuclear skin!

Once we have the interaction, using different wells for protons and neutrons in each nucleus, we can compute MED.



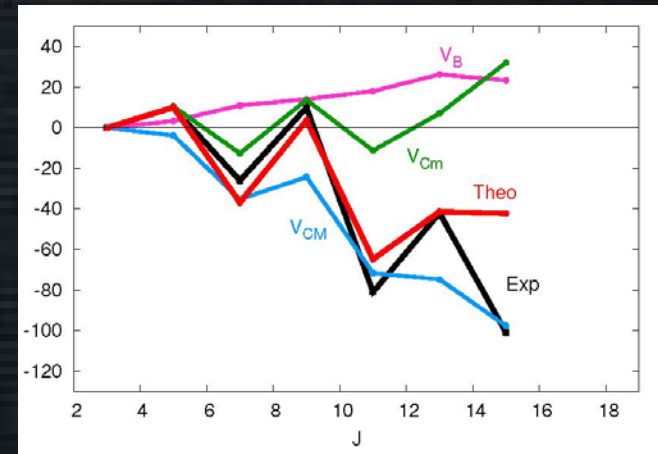
# Understanding the ISB: the mirror nuclei $A=23$

$^{23}\text{Na}$        $^{23}\text{Mg}$



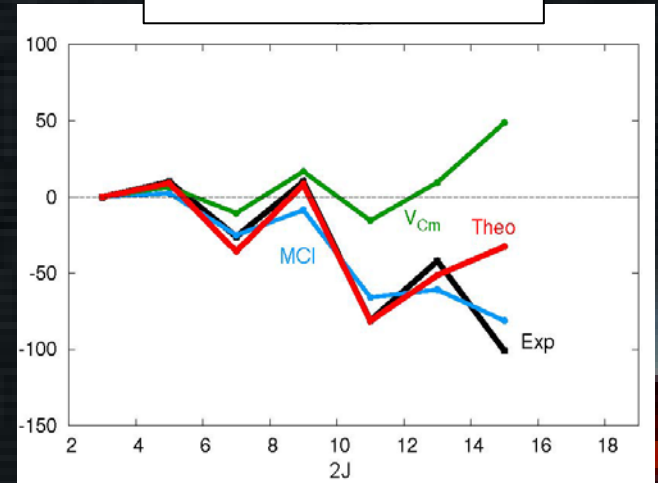
MED

Standard calculation



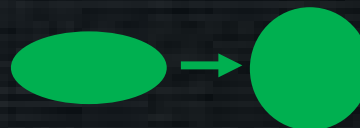
MCI calculation

MED



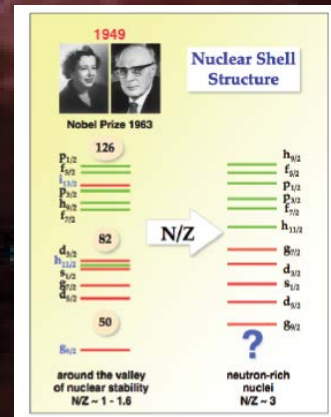
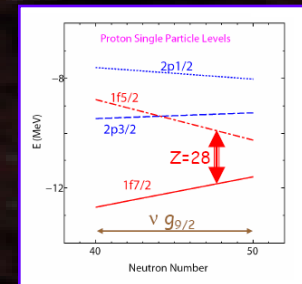
A.Boso et al.,  
to be published

$V_{CM}$





# Moving far from stability towards neutron-rich





# Shell evolution with $\gamma$ spectroscopy

Among the most fascinating current problems in nuclear structure far from stability, the **shell evolution** and the development of **new regions of deformation, the so-called Islands of Inversion (IoI)** around proton and neutron numbers that are “magic” near stability have attracted the attention of many research communities.

Many efforts from the experimental and theoretical sides allow to compose the puzzle by using the most sophisticated techniques and methods in looking at different observables.



# Understanding shell evolution

In the last years the amount and quality of these investigations have allowed to understand some of these phenomena in detail.

In particular, in some mass regions that are accessible with the current experimental facilities and allow microscopic theoretical calculations

In this presentation I will focus on a particular mass region and the theoretical description with the shell model, but these phenomena are the ideal ground where several methods can be applied and compared between them and with experimental data.

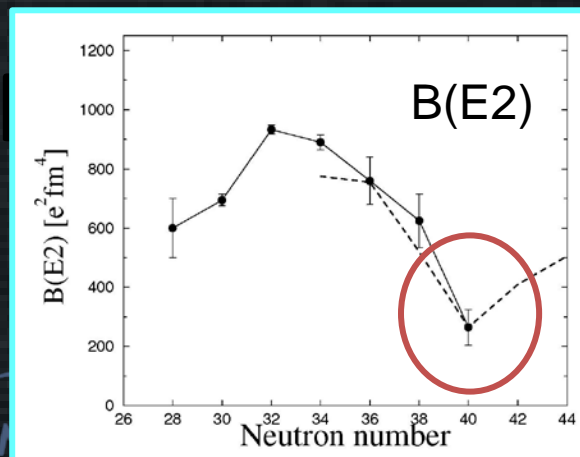
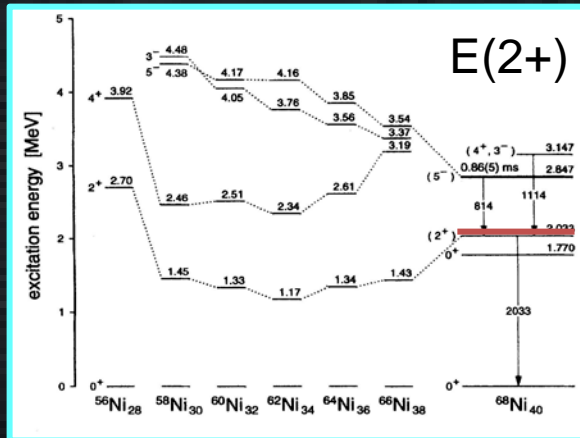


# A promenade south of $^{68}\text{Ni}$

First hints of a doubly-closed shell structure in  $^{68}\text{Ni}$



R. Broda et al.,  
PRL 74, 868 (1995)



O. Sorlin et al. PRL  
88, 092501 (2002)





# Deformation at $N \sim 40$ in Cr isotopes

Approaching  $N=40$  Cr isotopes show the development of deformation

Eur. Phys. J. A 16, 55–61 (2003)  
DOI 10.1140/epja/i2002-10069-9

THE EUROPEAN  
PHYSICAL JOURNAL A

## beta decay @ GANIL

New region of deformation in the neutron-rich  $^{60}\text{Cr}_{36}$  and  $^{62}\text{Cr}_{38}$

O. Sorlin<sup>1,a</sup>, C. Donzaud<sup>1</sup>, F. Nowacki<sup>2</sup>, J.C. Angélique<sup>3</sup>, F. Azaiez<sup>1</sup>, C. Bourgeois<sup>1</sup>, V. Chisté<sup>1</sup>, Z. Dlouhy<sup>4</sup>, S. Grévy<sup>5</sup>, D. Guillemaud-Mueller<sup>1</sup>, F. Ibrahim<sup>1</sup>, K.-L. Kratz<sup>6</sup>, M. Lewitowicz<sup>6</sup>, S.M. Lukyanov<sup>7</sup>, J. Mrasek<sup>4</sup>, Yu.-E. Penionzhkevich<sup>7</sup>, F. de Oliveira Santos<sup>6</sup>, B. Pfeiffer<sup>5</sup>, F. Pougheon<sup>1</sup>, A. Poves<sup>8</sup>, M.G. Saint-Laurent<sup>6</sup>, and M. Stanoiu<sup>6</sup>



ELSEVIER

Available online at www.sciencedirect.com

SCIENCE @ DIRECT®

Physics Letters B 633 (2006) 696–700

PHYSICS LETTERS B

www.elsevier.com/locate/physletb

## multinucleon transfer @ LNL

Shape transitions far from stability: The nucleus  $^{58}\text{Cr}$

N. Mărginean<sup>a,c,\*</sup>, S.M. Lenzi<sup>b</sup>, A. Gadea<sup>a</sup>, E. Farnea<sup>b</sup>, S.J. Freeman<sup>c</sup>, D.R. Napoli<sup>a</sup>, D. Bazzacco<sup>b</sup>,

PHYSICAL REVIEW C 74, 064315 (2006)

## deep-inelastic @ ANL

Level structure of the neutron-rich  $^{56,58,60}\text{Cr}$  isotopes: Single-particle and collective aspects

S. Zhu,<sup>1</sup> A. N. Deacon,<sup>2</sup> S. J. Freeman,<sup>2</sup> R. V. F. Janssens,<sup>1</sup> B. Fornal,<sup>3</sup> M. Honma,<sup>4</sup> F. R. Xu,<sup>5</sup> R. Broda,<sup>3</sup> I. R. Calderin,<sup>6</sup>

PRL 102, 012502 (2009)

PHYSICAL REVIEW LETTERS

week ending  
9 JANUARY 2009

## (p,p') @ RIKEN Development of Large Deformation in $^{62}\text{Cr}$

N. Aoi,<sup>1</sup> E. Takeshita,<sup>1,2</sup> H. Suzuki,<sup>3</sup> S. Takeuchi,<sup>1</sup> S. Ota,<sup>4</sup> H. Baba,<sup>1</sup> S. Bishop,<sup>1</sup> T. Fukui,<sup>4</sup> Y. Hashimoto,<sup>5</sup> H. J. Ong,<sup>6</sup>

## inelastic scattering @ NSCL (MSU)

PHYSICAL REVIEW C 81, 051304(R) (2010)

Collectivity at  $N = 40$  in neutron-rich  $^{64}\text{Cr}$

A. Gade,<sup>1,2</sup> R. V. F. Janssens,<sup>3</sup> T. Baugher,<sup>1,2</sup> D. Bazin,<sup>1</sup> B. A. Brown,<sup>1,2</sup> M. P. Carpenter,<sup>3</sup> C. J. Chiara,<sup>3,4</sup> A. N. Deacon,<sup>5</sup> S. J. Freeman,<sup>5</sup> G. F. Grinyer,<sup>1</sup> C. R. Hoffman,<sup>3</sup> B. P. Kay,<sup>3</sup> F. G. Kondev,<sup>6</sup> T. Lauritsen,<sup>3</sup> S. McDaniel,<sup>1,2</sup> K. Meierbachtol,<sup>1,7</sup> A. Ratkiewicz,<sup>1,2</sup> S. R. Stroberg,<sup>1,2</sup> K. A. Walsh,<sup>1,2</sup> D. Weisshaar,<sup>1</sup> R. Winkler,<sup>1</sup> and S. Zhu<sup>3</sup>

RAPID COMMUNICATIONS



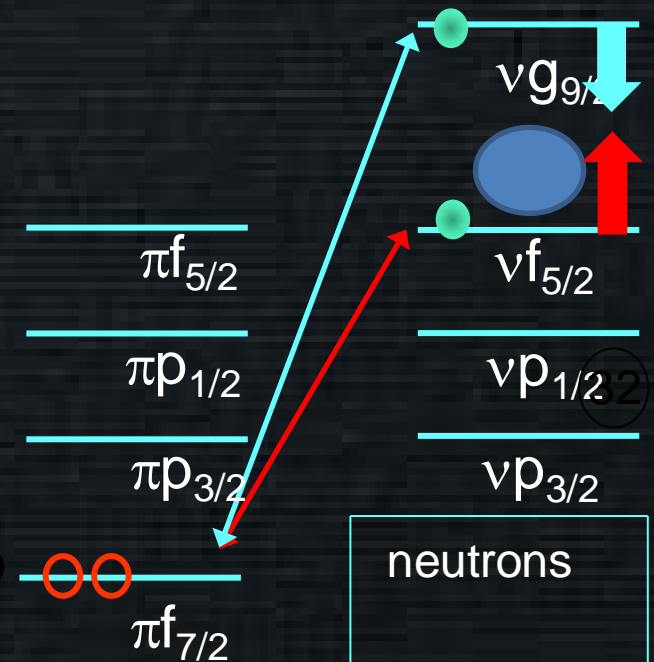
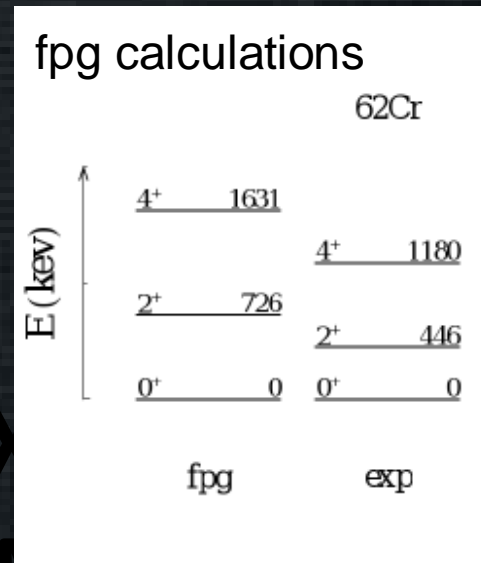
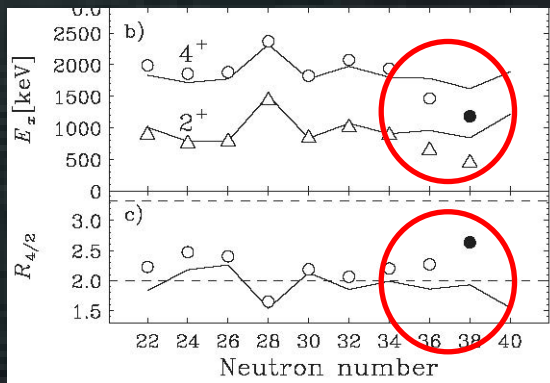
INFN  
Istituto Nazionale  
di Fisica Nucleare



# How to explain this phenomenon?

Different theoretical calculations and, in particular, the shell model failed to reproduce the data on  $^{60-62}\text{Cr}$

$f_{5/2}$  \_\_\_\_\_  
 $p_{1/2}$  \_\_\_\_\_  
 $p_{3/2}$  \_\_\_\_\_  
 $f_{7/2}$  \_\_\_\_\_



protons

The monopole migration was not able to justify and reproduce the data

neutrons

These valence spaces do not include the quadrupole degrees of freedom of the systems



The background of the slide features three curved, pixelated bands of color. The top band is red, the middle band is purple, and the bottom band is green. These bands are set against a dark, textured background that resembles a night sky or a deep space environment. The text is overlaid on the lower right portion of the image.

# Development of deformation and Islands of Inversion



# The effective interaction

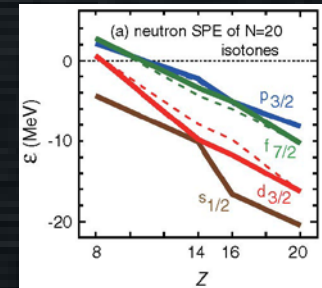
A multipole expansion

$$V_{eff} = V_m + V_M$$

monopole      Multipole

$V_m$

- determines the single particle energies and the shell evolution
- main components: central, tensor and s.o.



$V_M$

- responsible for the correlations, main components **Pairing and Quadrupole**
- determines the energy gains and collective behavior

Deformation



**It is the interplay of the monopole with the multipole terms what determines the different phenomena we observe.**



Istituto Nazionale  
di Fisica Nucleare



# Nuclear deformation: a simple model

## Elliott's SU(3)

In the limit of **degeneracy** of the single-particle energies of a major shell and in the presence of an **attractive Q.Q** interaction among protons and neutrons, the ground state of the many-body nuclear system is **maximally deformed**.

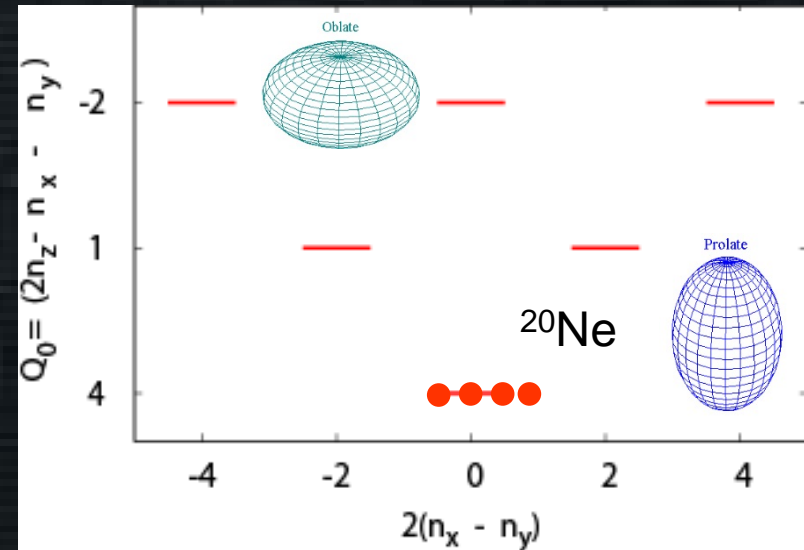
The quadrupole moment of a nucleon is:

$$Q_0 = (2n_z - n_x - n_y)$$

where the principal quantum number  $N = (n_x + n_y + n_z)$

In the  $sd$  shell  $N = 2$   
there are 6 possible states:  
(2,0,0) (0,2,0) (0,0,2)  
(1,1,0) (1,0,1) (0,1,1)

$$Q_0 = 4, 1, -2$$



Elliott's SU3 works well in the  $sd$  shell but fails for upper shells where the SO interaction introduces large energy shifts





# SU3 approximate symmetries

Two variants of SU3 apply in specific spaces

## Quasi SU3

applies to the lowest  $\Delta j = 2$ ,  $\Delta l = 2$   
orbits in a major HO shell



## Pseudo SU3

applies to a HO space where the  
largest  $j$  orbit has been removed.



A.P. Zuker et al., PRC **52**, R1741 (1995).

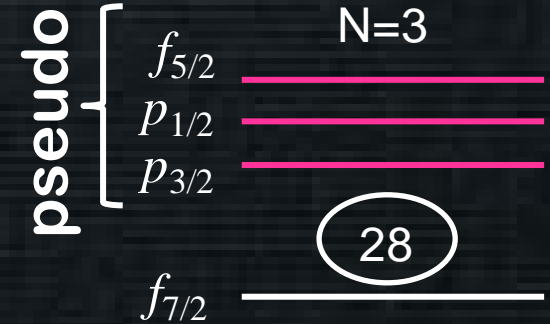
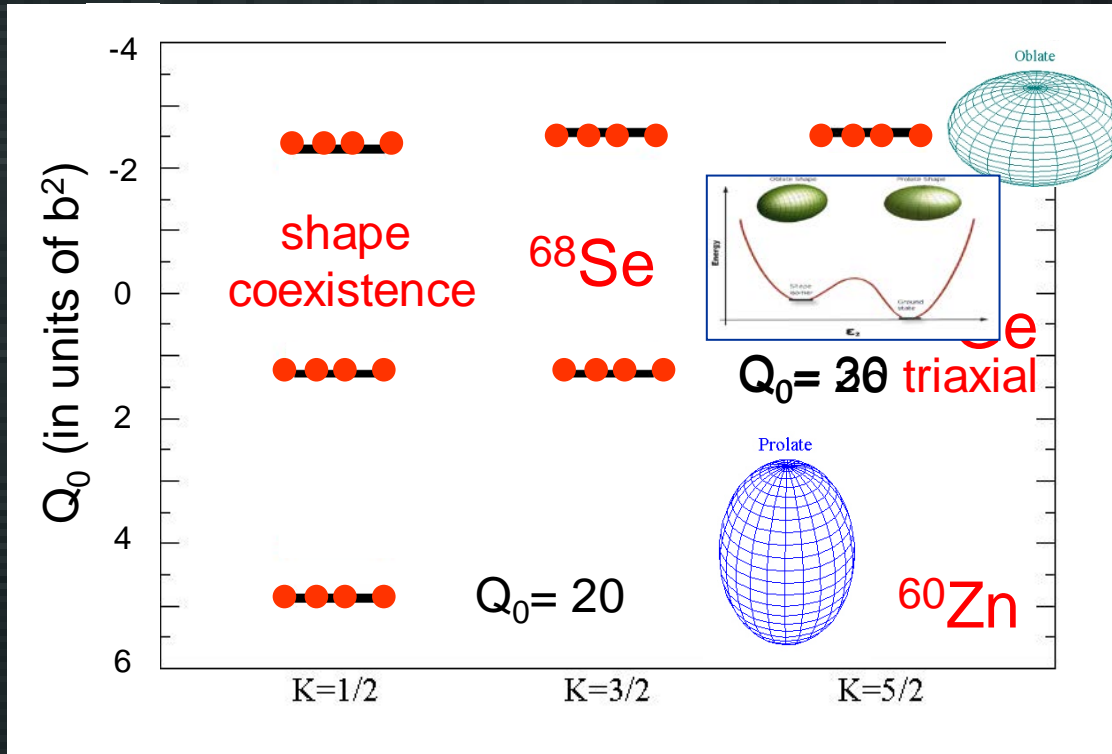
Zuker, Poves, Nowacki, Lenzi, PRC **92**, 024320 (2015)



Istituto Nazionale  
di Fisica Nucleare



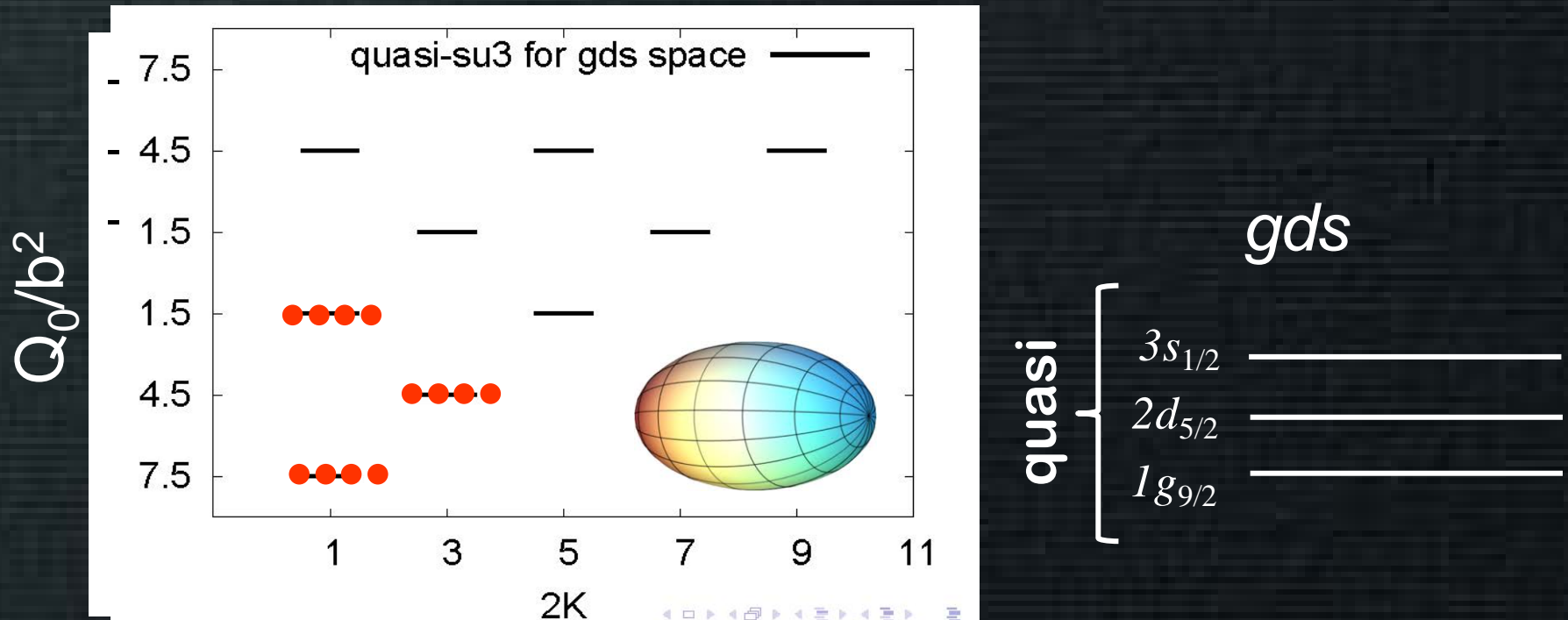
# Quadrupole moments in Pseudo SU<sub>3</sub>



We obtain  $Q_0$  by summing those of the single particles/holes in each “orbit”



# Quadrupole moments in Quasi SU<sub>3</sub>

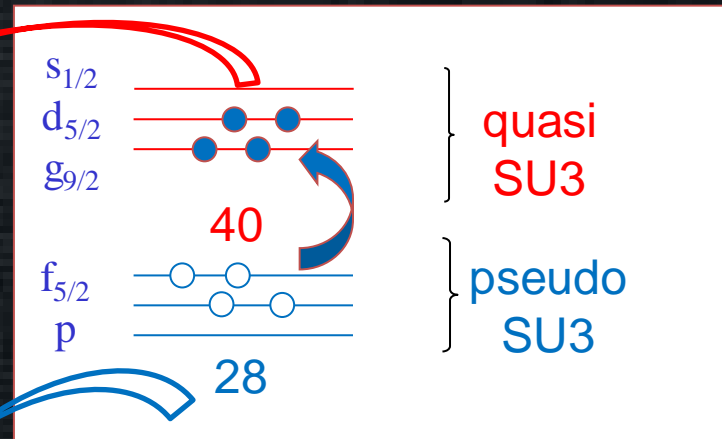
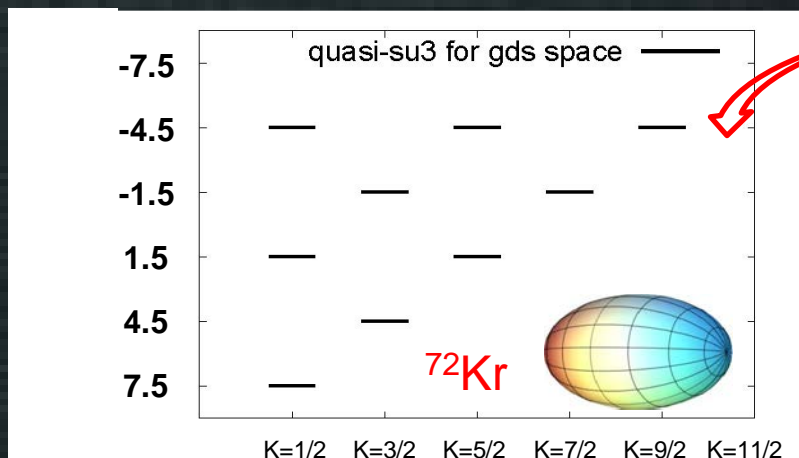


We obtain  $Q_0$  by summing those of the single particles in each “orbit”



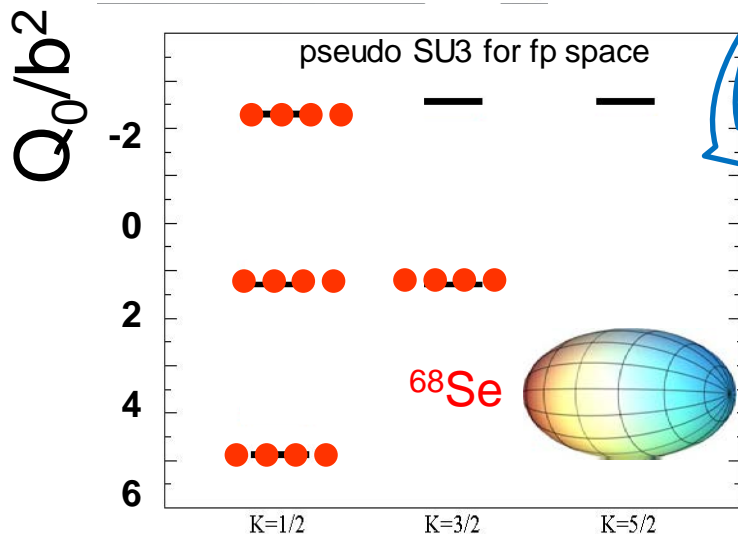
# Maximizing quadrupole correlations

quasi



Particle-hole excitations in the pseudo + quasi space maximize the quadrupole moment.

pseudo



The quadrupole correlation energy results much larger than the energy cost to promote the particles

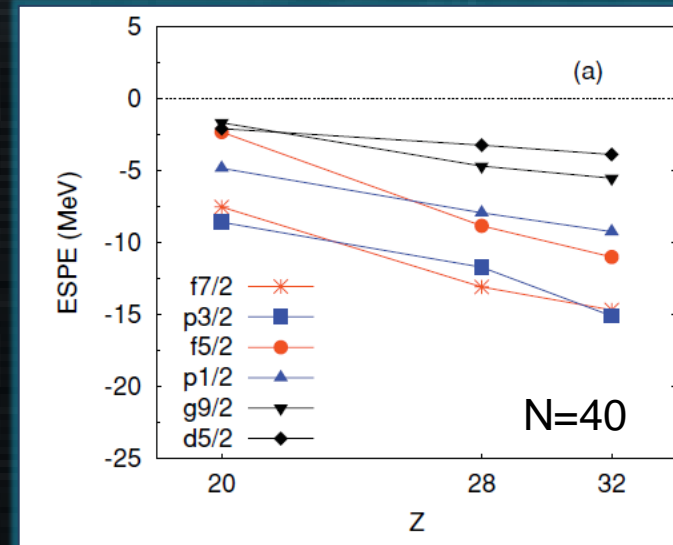
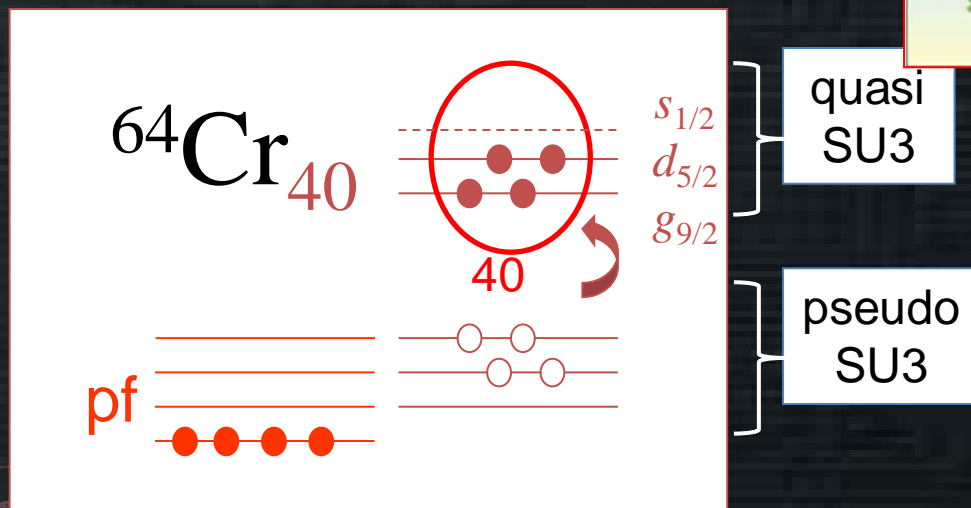




# The model space that includes the quadrupole degrees of freedom

It is the interplay of the monopole terms of the interaction with multipole terms, like pairing and quadrupole, which determines the different phenomena we observe.

This explains the development of the Islands of inversion at the “traditional” magic numbers



Lenzi, Nowacki, Poves, Sieja  
(LNPS interaction)  
PRC 82, 054301 (2010)

Other effective interactions:  
 $V_{\text{low } k}$ : L. Coraggio et al., PRC 89, 024319 (2014).  
A3DA: Tsunoda et al., PRC 89, 031301 (2014).



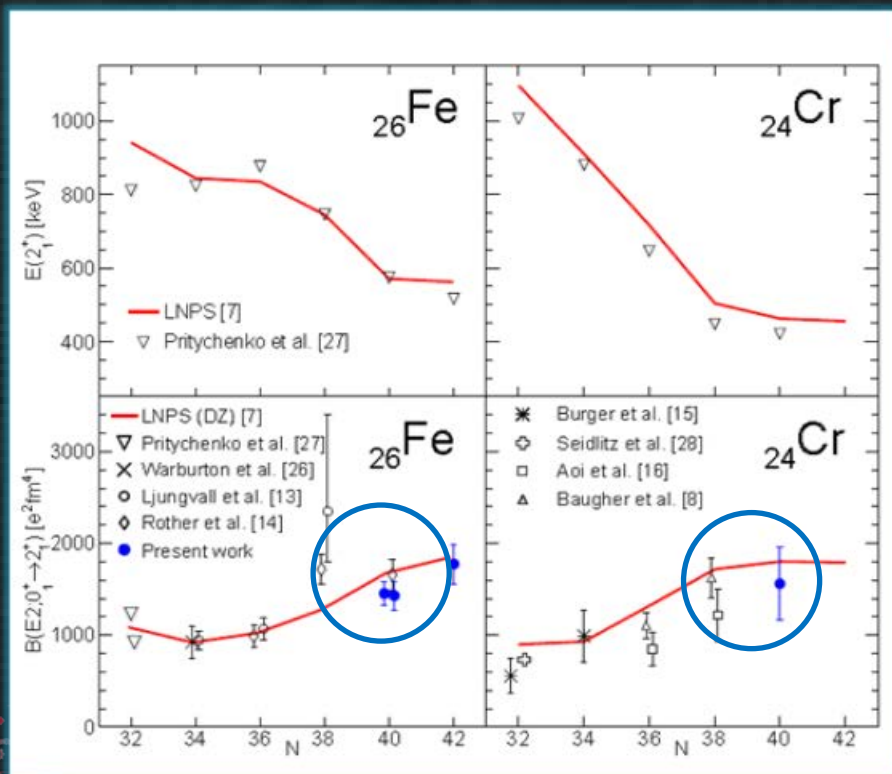
The background of the slide features three distinct, curved, pixelated lines that sweep across the frame from the bottom left towards the top right. The topmost line is primarily red and orange. The middle line is a complex pattern of purple, blue, and yellow pixels. The bottom line is primarily green. The text 'Continuing our promenade' is overlaid in a light blue, sans-serif font, positioned in the lower right area of the image.

Continuing our promenade



# Measurement of deformation with radioactive beams

Intermediate-energy Coulomb excitation measurements at NSCL-MSU



p-h excitations across  $Z=28$  and  $N=40$  in  $N=40$  isotones

Nucleus	$\nu g_{9/2}$	$\nu d_{5/2}$	0p0h	2p2h	4p4h	6p6h	$E_{\text{corr}}$
$^{68}\text{Ni}$	0.98	0.10	55.5	35.5	8.5	0.5	-9.03
$^{66}\text{Fe}$	3.17	0.46	1	19	72	8	-23.96
$^{64}\text{Cr}$	3.41	0.76	0	9	73	18	-24.83
$^{62}\text{Ti}$	3.17	1.09	1	14	63	22	-19.62
$^{60}\text{Ca}$	2.55	1.52	1	18	59	22	-12.09

deformation  $\beta \sim 0.3$

See also:  $^{68-70}\text{Fe}$  G. Benzoni et al., PLB 751 (2015) 107

H. L. Crawford et al., PRL 110, 242701 (2013)

T. Baugher et al., PRC 86, 011305(R) (2012)

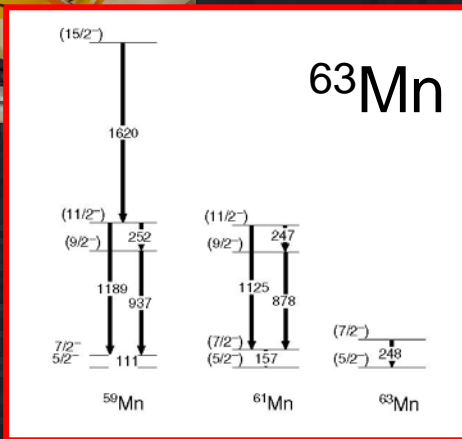
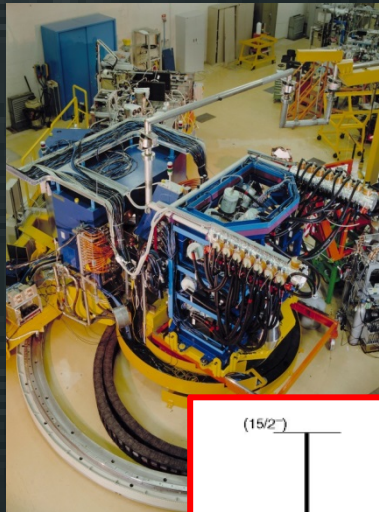
Istituto Nazionale  
di Fisica Nucleare



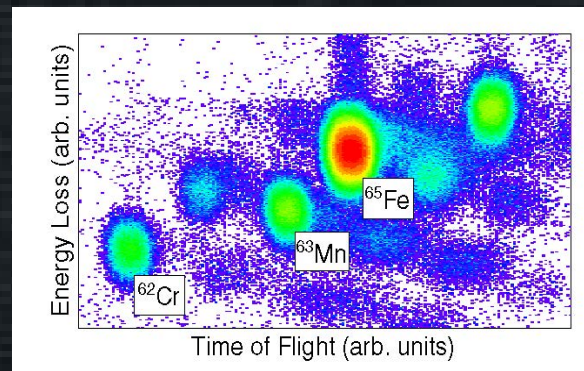
# Spectroscopy on heavy Mn

First level schemes from multi-nucleon transfer reactions using CLARA + PRISMA at LNL

Inelastic scattering following fragmentation with SEGA @ MSU



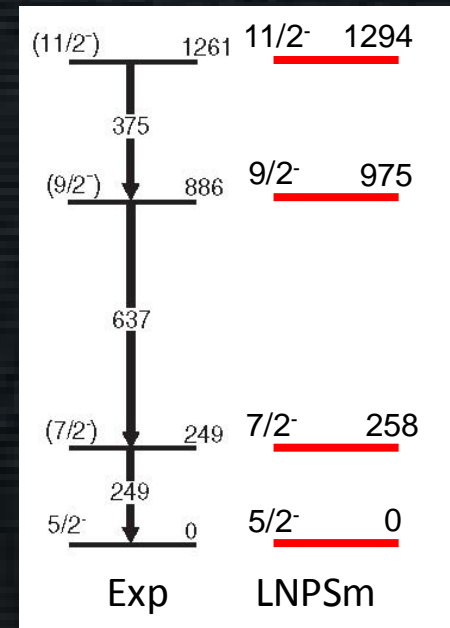
J.J. Valiente-Dobon et al.,  
PRC 78, 024302 (2008)



T. Baugher et al.,  
PRC 93, 014313 (2016)

More data on heavier Mn isotopes coming soon from RIKEN.

## $^{63}\text{Mn}$





# Deformation in $^{58,60}\text{Ti}$ : towards $^{60}\text{Ca}$

PRL **112**, 112503 (2014)

PHYSICAL REVIEW LETTERS

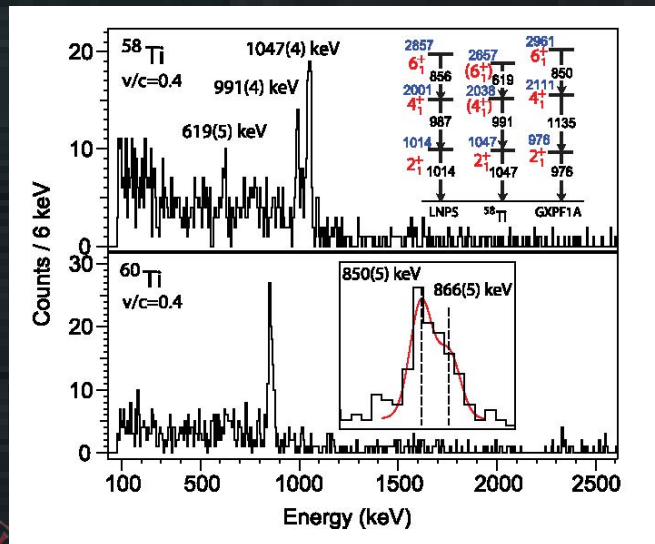
week ending  
21 MARCH 2014

## Nuclear Structure Towards $N = 40$ $^{60}\text{Ca}$ : In-Beam $\gamma$ -Ray Spectroscopy of $^{58,60}\text{Ti}$

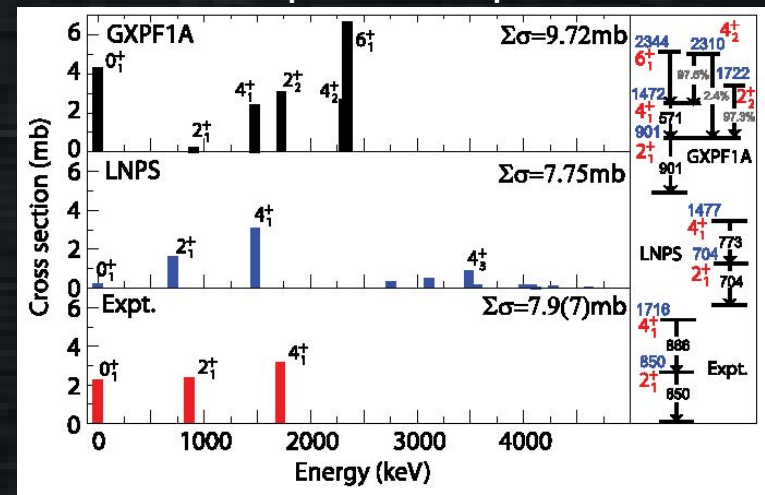
A. Gade,<sup>1,2</sup> R. V. F. Janssens,<sup>3</sup> D. Weisshaar,<sup>1</sup> B. A. Brown,<sup>1,2</sup> E. Lunderberg,<sup>1,2</sup> M. Albers,<sup>3</sup> V. M. Bader,<sup>1,2</sup> T. Baugher,<sup>1,2</sup> D. Bazin,<sup>1</sup> J. S. Berryman,<sup>1</sup> C. M. Campbell,<sup>4</sup> M. P. Carpenter,<sup>3</sup> C. J. Chiara,<sup>5,3</sup> H. L. Crawford,<sup>4,5</sup> M. Cromaz,<sup>4</sup> U. Garg,<sup>6</sup> C. R. Hoffman,<sup>3</sup> F. G. Kondev,<sup>7</sup> C. Langer,<sup>1,8</sup> T. Lauritsen,<sup>3</sup> I. Y. Lee,<sup>4</sup> S. M. Lenzi,<sup>9</sup> J. T. Matta,<sup>6</sup> F. Nowacki,<sup>10</sup> F. Recchia,<sup>1,†</sup> K. Sieja,<sup>10</sup> S. R. Stroberg,<sup>1,2</sup> J. A. Tostevin,<sup>11</sup> S. J. Williams,<sup>1</sup> K. Wimmer,<sup>12,1</sup> and S. Zhu<sup>3</sup>

GRETINA data  
from NSCL

A decrease of quadrupole deformation is observed at  $Z=22$  indicating the smooth transition at the border of the Island of Inversion



Knockout cross section obtained  
with SM spectroscopic factors

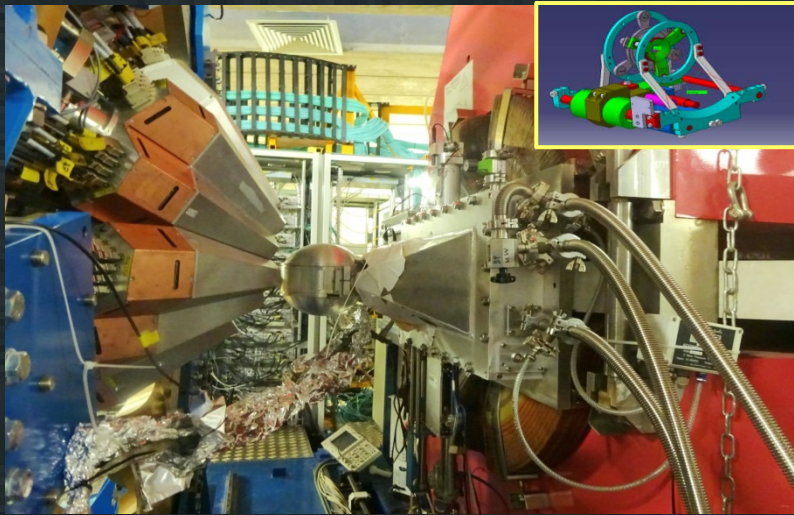


$^{60}\text{Ti}$  represents an important benchmark from which to extrapolate towards  $^{60}\text{Ca}$  and the location of the neutron drip line in the Ca isotopic chain.

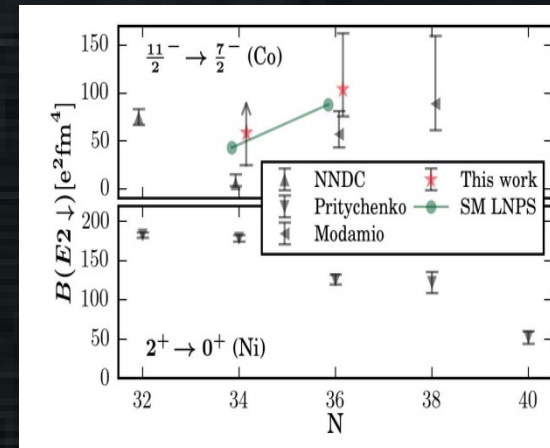
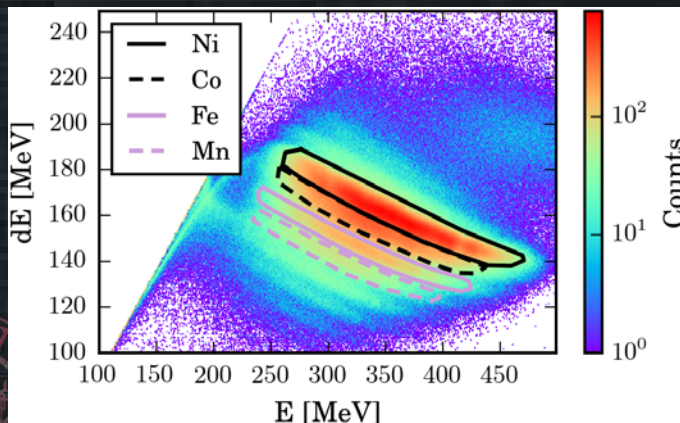
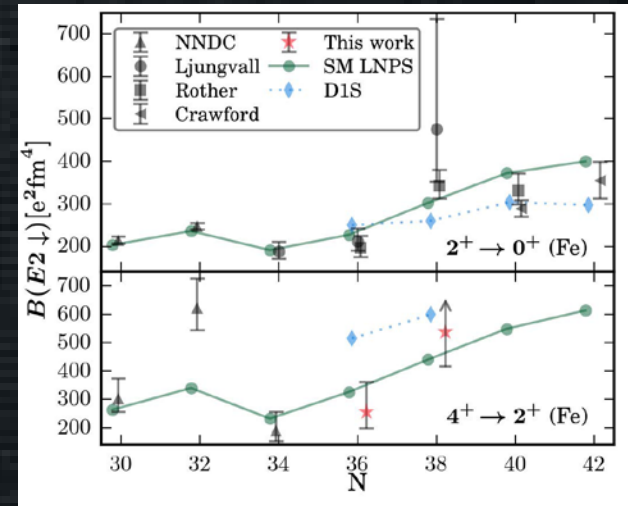


# Lifetimes in Mn, Fe, Co and Ni

AGATA + VAMOS experiment



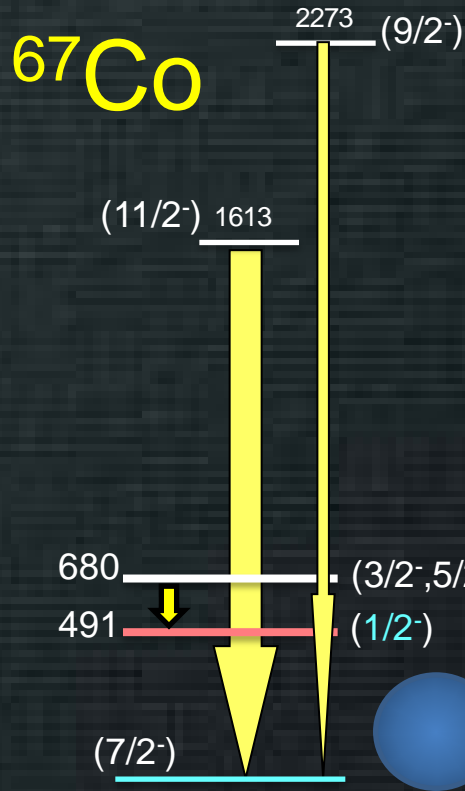
Multinucleon transfer+ punger



M. Klintefjord et al., PRC 95, 024312 (2017)

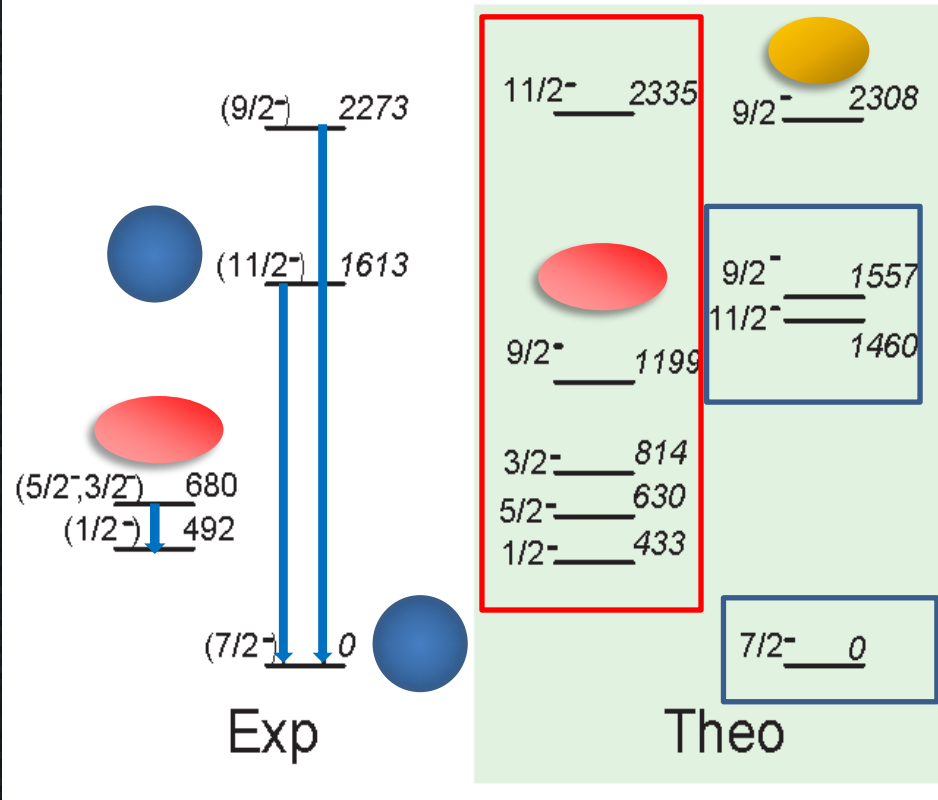


# Shape coexistence in $^{67}\text{Co}$



The deformation driven by the neutrons induces a reduction of the Z=28 gap and gives rise to a deformed low-lying 1/2<sup>-</sup> state

CLARA+PRISMA LNL  $^{67}\text{Co}$



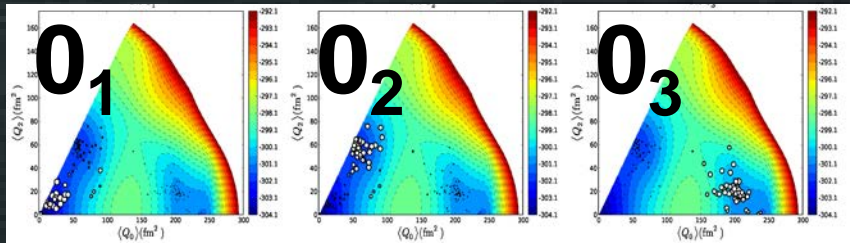
D. Pauwels et al., PRC 78, 041307 (2008) and PRC 79, 044309 (2009)

F. Recchia et al., PRC 85, 064305 (2012)



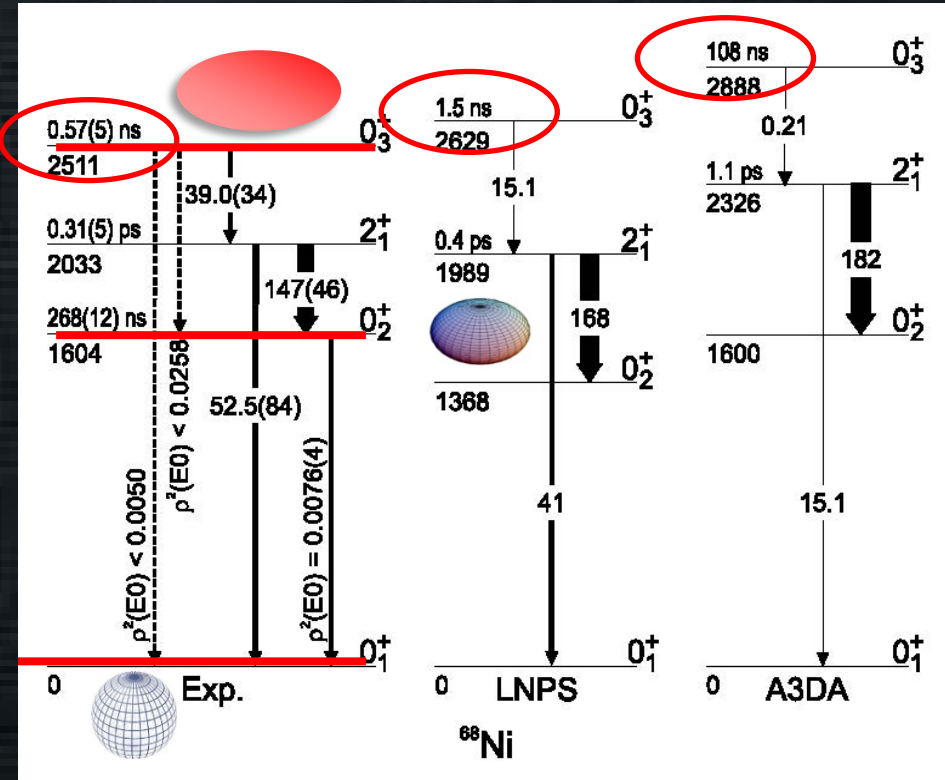
# Triple shape coexistence in $^{68}\text{Ni}$

The first three  $0^+$  states are predicted to have different shapes by MCSM calculations



Y. Tsunoda et al., PRC 89, 024313(R) (2014)

In  $^{68}\text{Ni}$  as in  $^{40}\text{Ca}$  (super- deformed band at low excitation energy) the magic closures are probed by the action of the nuclear correlations, pairing and quadrupole, that favor the intruder configurations



F. Flavigny et al., PRC 91, 034310 (2015)

F. Recchia et al., PRC **88**, 041302(R) (2013)

Istituto Nazionale  
di Fisica Nucleare

B.P. Crider et al., PLB 763 (2016) 108  
lifetime measurement beta-decay  
NSCL with LaBr3(Ce) + SEGA





# Doorway excited states in magic nuclei

Excited (intruder) states in doubly-closed shell nuclei act as precursors of what becomes the ground states of lighter isotones.

Valence spaces spanned by a single major shell do not contain the degrees of freedom necessary for the development of collectivity.

Two main shells have to be included, but just keeping the relevant orbitals where the Quadrupole Deformation develops. The choice is ruled by dynamical symmetries, variants of  $SU(3)$



# Approaching $N=50$



# The N=40 Iol continues to N=50

(p,2p) reactions at using DALI2 and MINOS

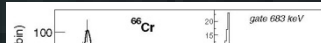
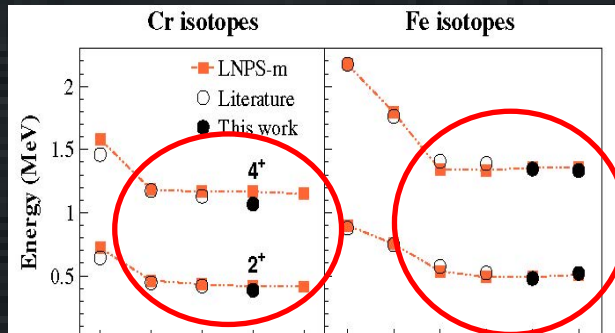
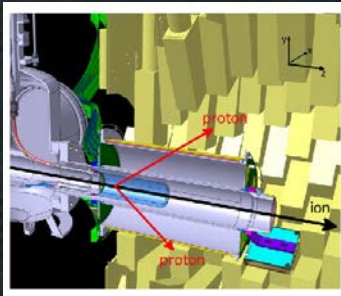
PRL **115**, 192501 (2015)

PHYSICAL REVIEW LETTERS

week ending  
6 NOVEMBER 2015

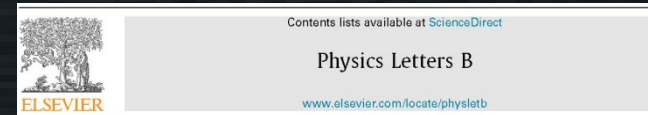
## Extension of the $N = 40$ Island of Inversion towards $N = 50$ : Spectroscopy of $^{66}\text{Cr}$ , $^{70,72}\text{Fe}$

C. Santamaria,<sup>1,2</sup> C. Louchart,<sup>3</sup> A. Obertelli,<sup>1,2</sup> V. Werner,<sup>3,4</sup> P. Doornenbal,<sup>2</sup> F. Nowacki,<sup>5</sup> G. Authalet,<sup>1</sup> H. Baba,<sup>2</sup>



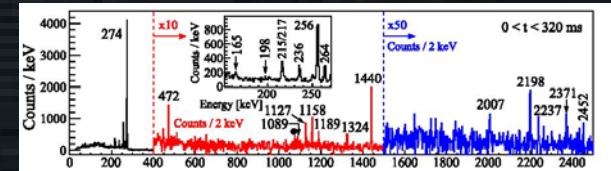
Nucleus	$n^{\nu}(g_{9/2} + d_{5/2})$		$0p0h$	$2p2h$	$4p4h$	$6p6h$	$\Delta E^*_{\text{Pairing}}$
	IPM	SM					
$^{60}\text{Cr}$	0	1.8	14	75	7	0	1.84
$^{62}\text{Cr}$	0	3.5	1	25	71	3	1.49
$^{64}\text{Cr}$	0	4.3	0	8	71	20	1.25
$^{66}\text{Cr}$	2	5.2	0	40	56	3	1.13
$^{68}\text{Cr}$	4	6.0	6	79	11	0	1.24

$\beta$ -decay with EURICA



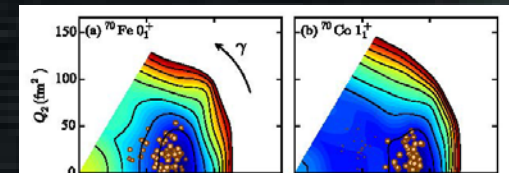
Type II shell evolution in  $A = 70$  isobars from the  $N \geq 40$  island of inversion

A.I. Morales<sup>a,b,\*</sup>, G. Benzon<sup>a</sup>, H. Watanabe<sup>c,d</sup>, Y. Tsunoda<sup>e</sup>, T. Otsuka<sup>f,g,h</sup>, S. Nishimura<sup>i</sup>



Low-lying state in  $^{70}\text{Co}$  is deformed

$^{70}\text{Fe} \rightarrow ^{70}\text{Co}$			
$J_p^{\pi}$	$J_d^{\pi}$	$B(\text{GT})$	$\log ft$
$0^+$	$1^+$	$4 \times 10^{-5}$	7.9
	$1^+$	$3.7 \times 10^{-2}$	5.02
	$1^+$	$1.8 \times 10^{-1}$	4.33

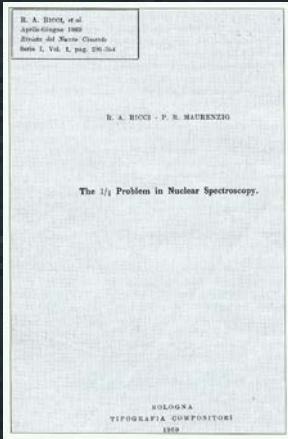




Silvia Lenzi – Varenna, 17/7/17



# Conclusions and perspectives



The  $f_{7/2}$ -shell nuclei are the ideal benchmark to understand nuclear structure properties such as:

- development of deformation
- shape coexistence
- proton-neutron pairing
- charge-symmetry broken
- islands of inversion far from stability

High-resolution gamma ray spectroscopy allows to get detailed insight into several nuclear properties by means of different experimental techniques and, therefore, to have a comprehensive picture of the nuclear dynamics and its evolution far from stability.

The subtle balance between correlations induced by the multipole interaction and the monopole field determines these phenomena. Dynamical symmetries help to choose the model spaces that contain the relevant degrees of freedom of the system.

Low- $\ell$  orbits play a very important role in determining different nuclear properties, as e.g. the Mirror Energy Differences.  
More is coming!





# Special thanks to

A. Boso, M. Bentley, J. Bonnard, F. Recchia,  
F. Nowacki, A. Poves and A. Zuker

# Thank you for your attention