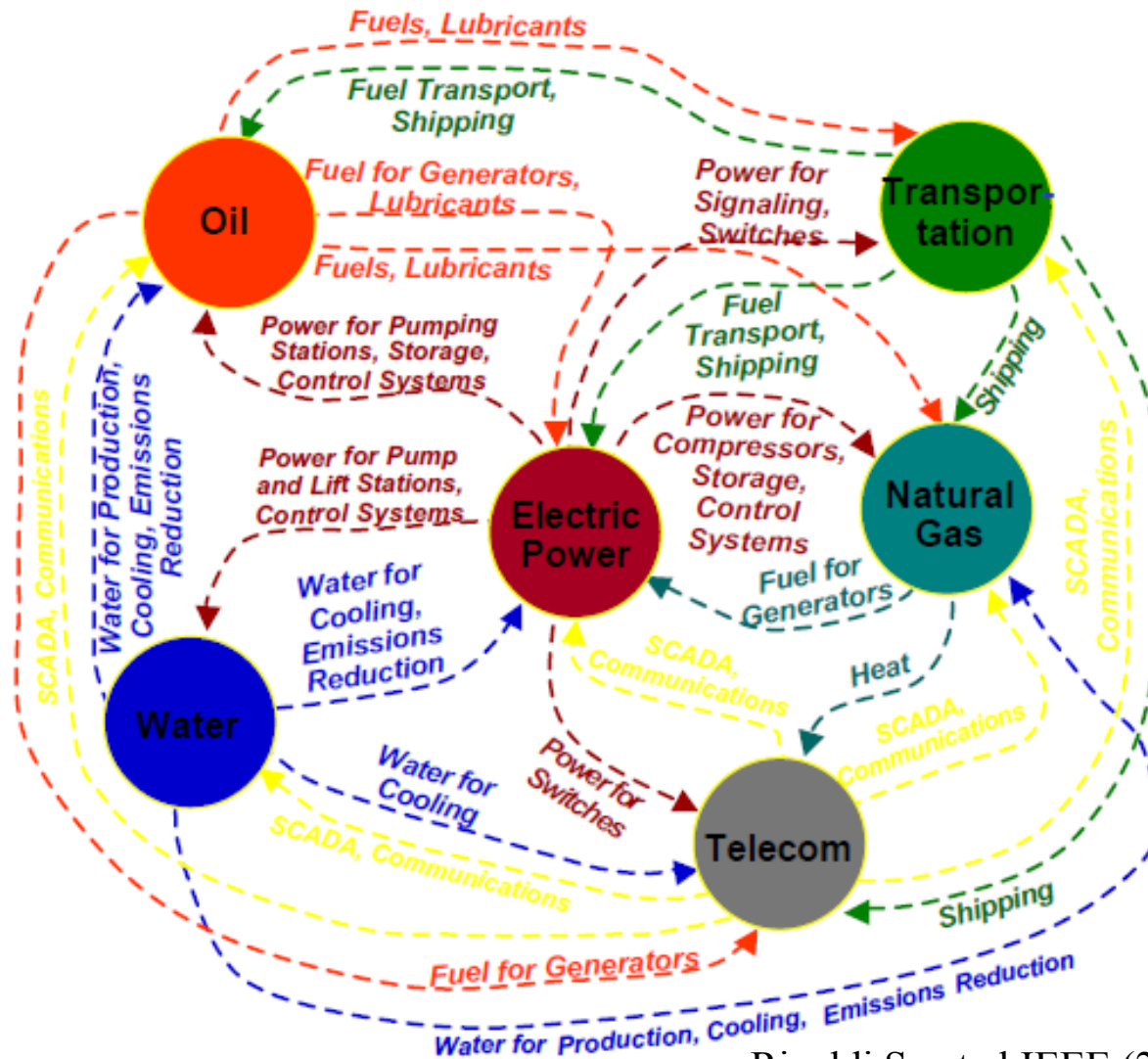


How interdependent are infrastructures?



Rinaldi S, et al IEEE (2001)

VOLUME 279
NUMBER 73

Suggested retail price
\$1.00
\$1.50 outside of
Metro Boston

The Boston Globe

MONDAY, MARCH 14, 2011

A NEW WEEK

TODAY: Partly sunny and colder. High 37-42. Low 27-32.

TOMORROW: Mostly sunny, milder. High 42-47. Low 32-37.

HIGH TIDE: 6:42 a.m., 7:25 p.m.

SUNRISE: 6:59 SUNSET: 6:49

FULL REPORT: PAGE B13

Cascading disaster in Japan

Blast shakes a second reactor death toll soars

By Martin Fackler
and Mark McDonald
NEW YORK TIMES

SENDAI, Japan — Japan reeled from a rapidly unfolding disaster epic scale yesterday, pummeled by a death toll, destruction, and homelessness caused by the earthquake and tsunami and new hazards from damaged nuclear reactors. The prime minister called it Japan's worst crisis since World War II.

Japan's \$5 trillion economy, the world's third largest, was threatened with severe disruptions and partial paralysis as many industries shut down temporarily. The armed forces and volunteers mobilized for the far more urgent crisis of finding survivors, evacuating residents near the stricken power plants and caring for the victims of the record 8.9 magnitude quake that struck on Friday.

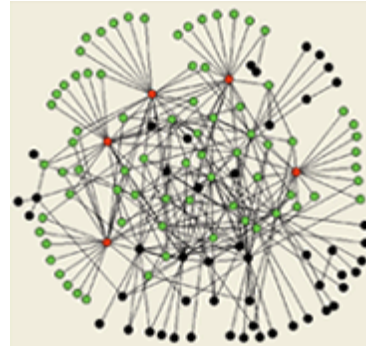
The disaster has left more than 10,000 dead, many thousands homeless, and millions without water, power, heat, or transportation.



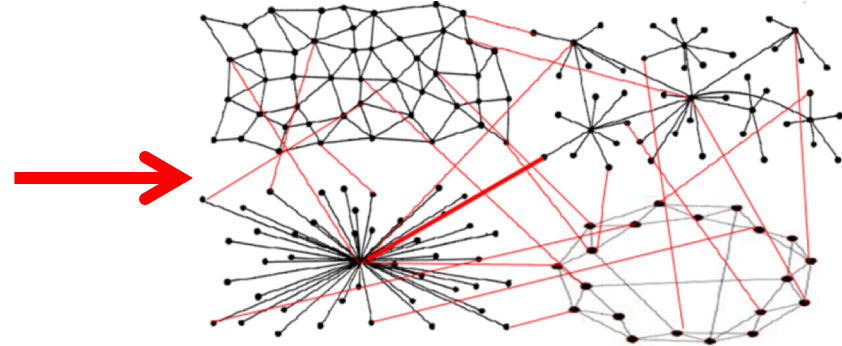
From Single Network to Network of Networks

Collaboration:

2000



2010



Shlomo Havlin

multilevel
multilayer
multiplex

Buldyrev et al, Nature, 464, 1025 (2010)

Parshani et al, PRL ,105, 0484 (2010)

Parshani et al, PNAS, 108, 1007 (2011)

Gao et al, PRL, 107, 195701 (2011)

Gao et al, Nature Phys.,8, 40 (2012)

Wei Li et al, PRL, 108, 228702 (2012)

Bashan et al, Nature Phys. 9, 667 (2013)

Majdanzik et al Nature Comm. 7, 10850 (2016)

Xin Yuan et al, PNAS 114, 3311 (2017)

Amir Bashan, BIU
Sergey Buldyrev, NY
Michael Danziger, BIU
J. Gao: Northeastern
Orr Levy, BIU
Roni Parshani: BIU
Louis Shektman, BIU
Antonio Majdanzic, BU
H. E. Stanley, BU
Dong Zhou, BIU

PARTIAL LIST

Electric grid,
Communication
Transportation
Services

Two types of links:

1. Connectivity
2. Dependency

Cascading failures-abrupt transition

Communication
SCADA

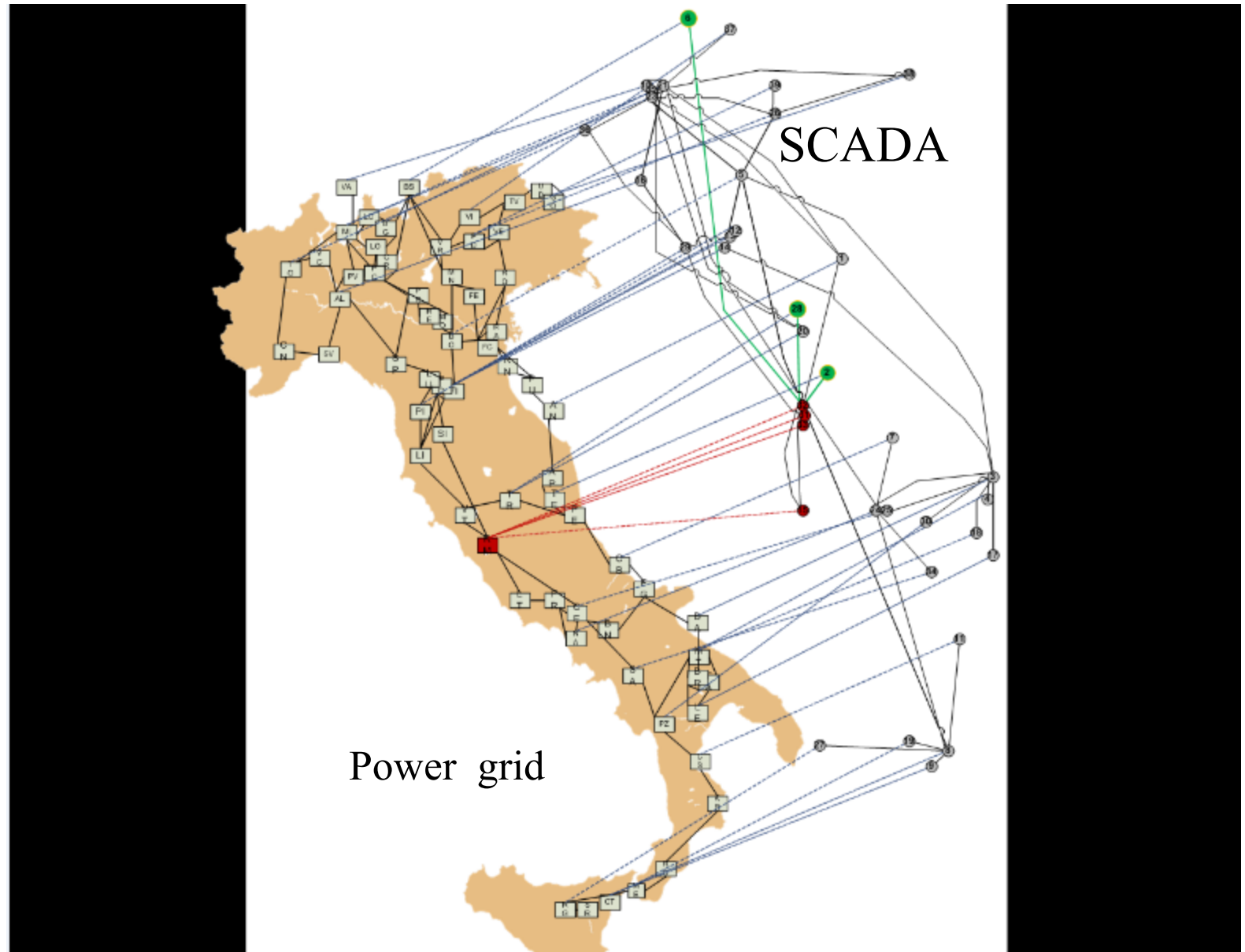
Power grid

CASCADE OF FAILURES

Rosato et al
Int. J. of Crit.
Infrastruct. 4,
63 (2008)

Railway network, health care systems, financial services, communication systems

Blackout in Italy (28 September 2003)



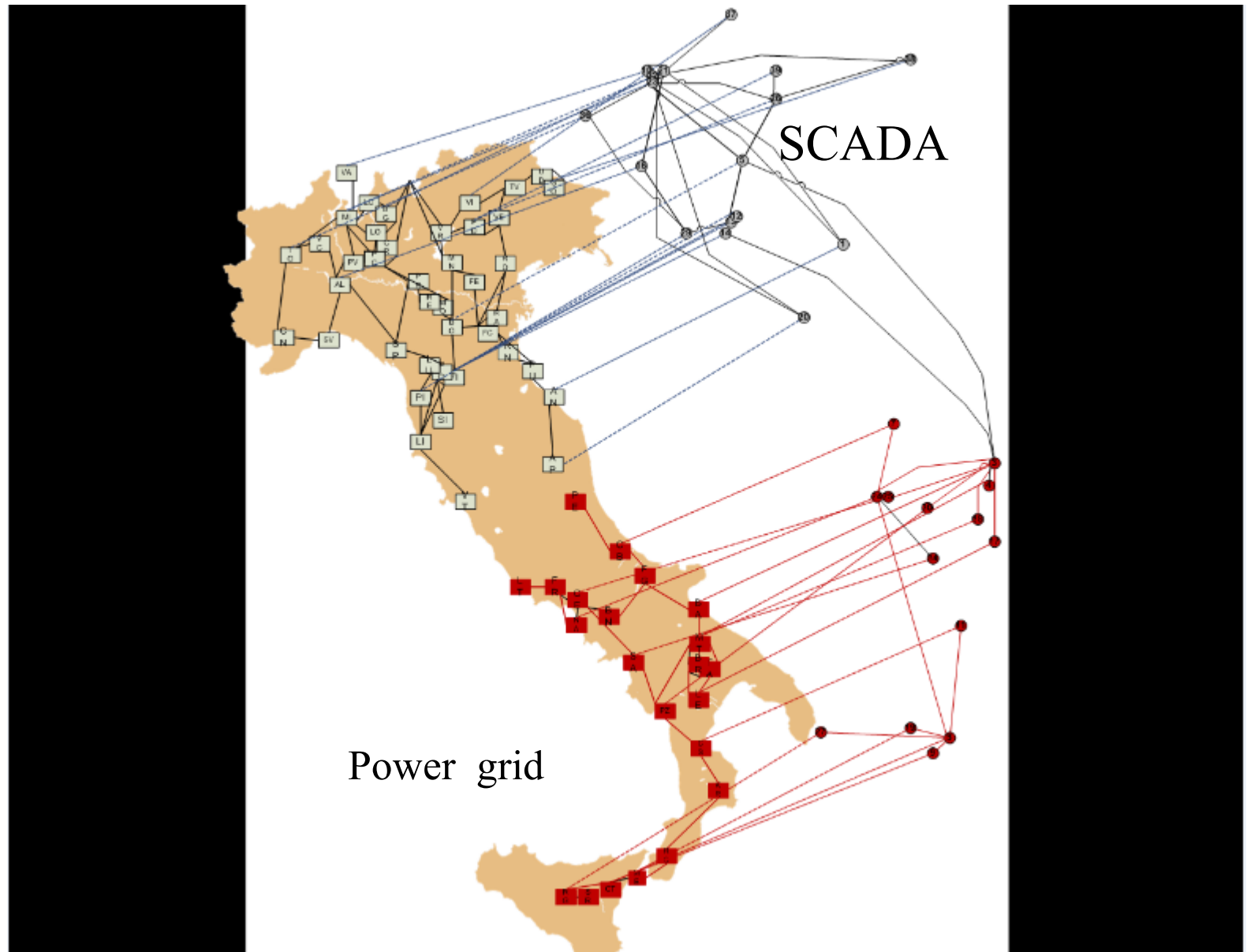
SCADA=Supervisory Control And Data Acquisition

SCADA

Power grid

Power grid

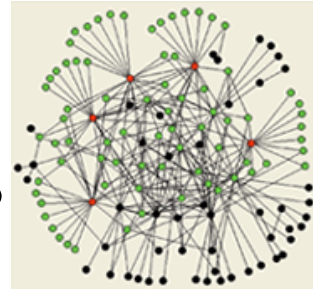
Blackout in Italy (28 September 2003)



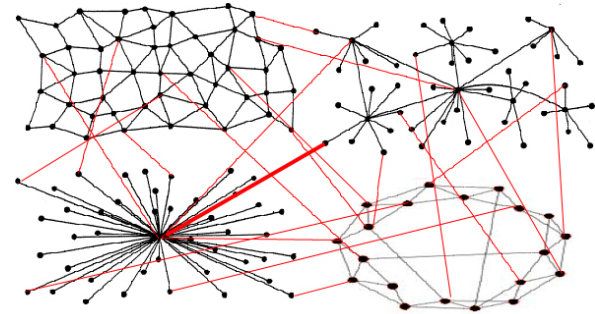
CNN SCENARIO

Interdependent Networks

- Until 2010 studies focused on a **single network** which is isolated AND does not interact or influenced by other systems

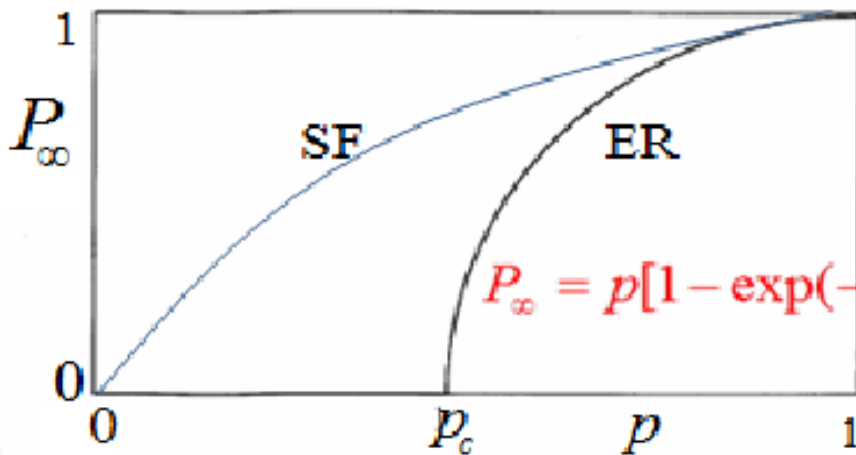


- Isolated systems **rarely** occur in nature or in technology -- analogous to **non-interacting** particles (molecules, spins).

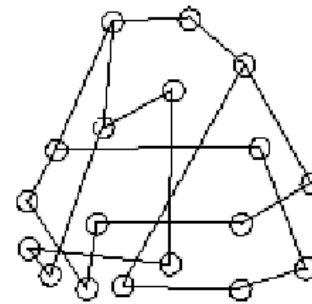


- Results for **interacting networks** are strikingly **different** from those of single networks.

Percolation of Network-Giant Component P_∞

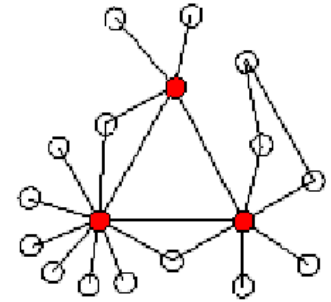


Exponential



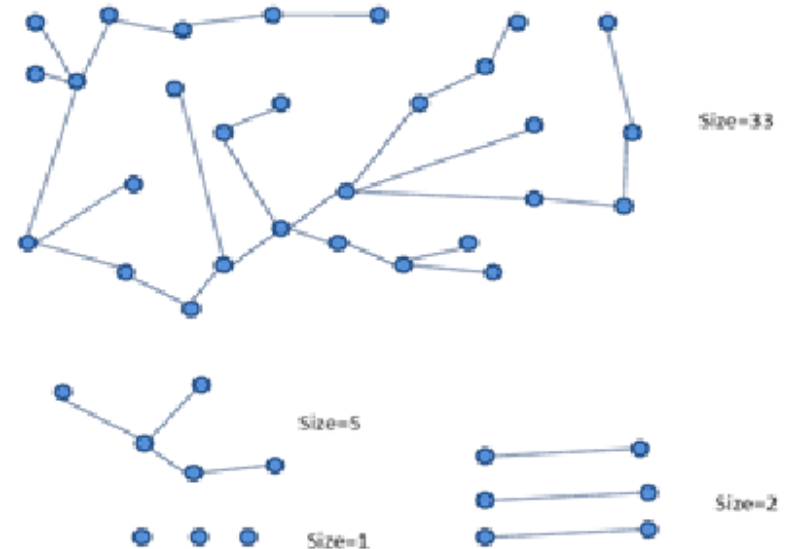
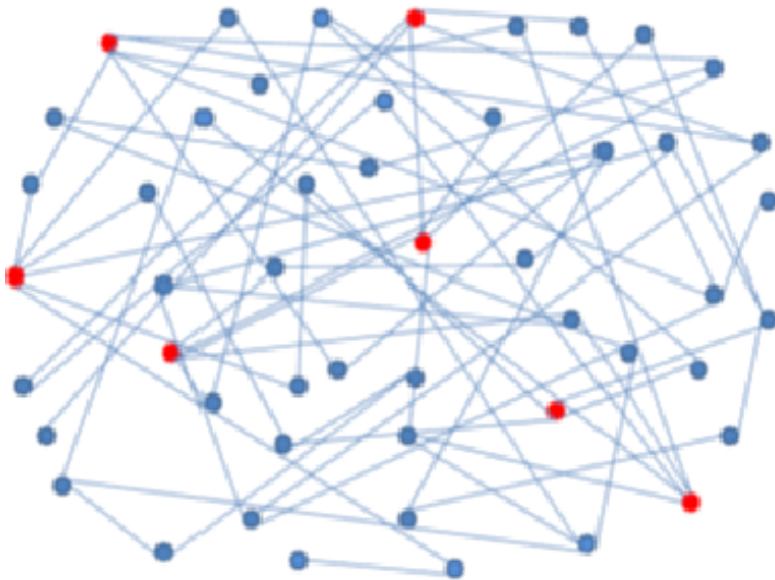
$$P(k) = e^{-\langle k \rangle} \frac{\langle k \rangle^k}{k!}$$

Scale-free



$$P(k) = \begin{cases} ck^{-\lambda} & m \leq k \leq K \\ 0 & \text{otherwise} \end{cases}$$

Scale-free network: $N=50$; $\lambda=2.5$ – attacking 7 nodes $p=43/50$



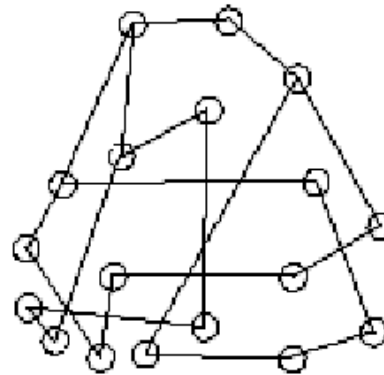
Comparing single and coupled networks: Robustness

Remove randomly (or targeted) a fraction $1 - p$ nodes

P_∞ Size of the largest connected component (cluster)

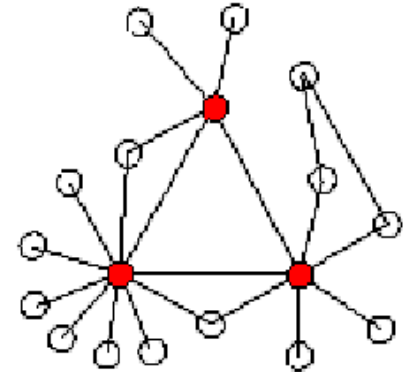
p_c Breakdown threshold

Exponential (ER)



$$P(k) = e^{-\langle k \rangle} \frac{\langle k \rangle^k}{k!}$$

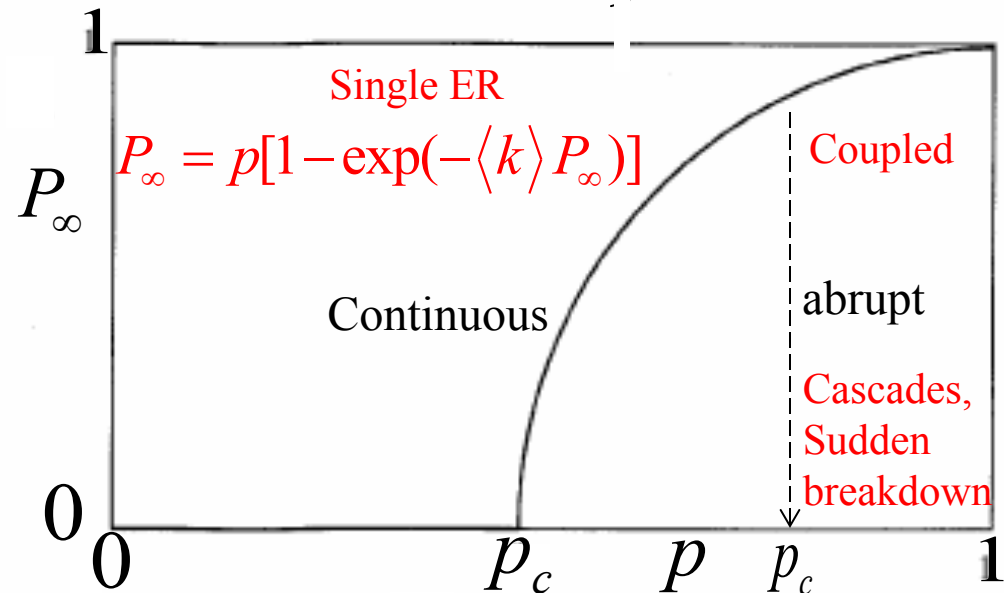
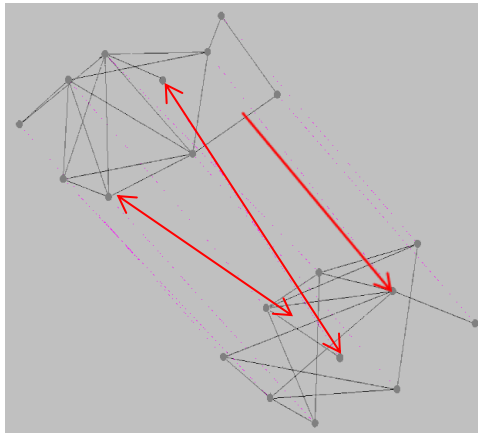
Scale-free (SF)



$$P(k) = \begin{cases} ck^{-\lambda} & m \leq k \leq K \\ 0 & \text{otherwise} \end{cases}$$

Single networks:

Continuous transition



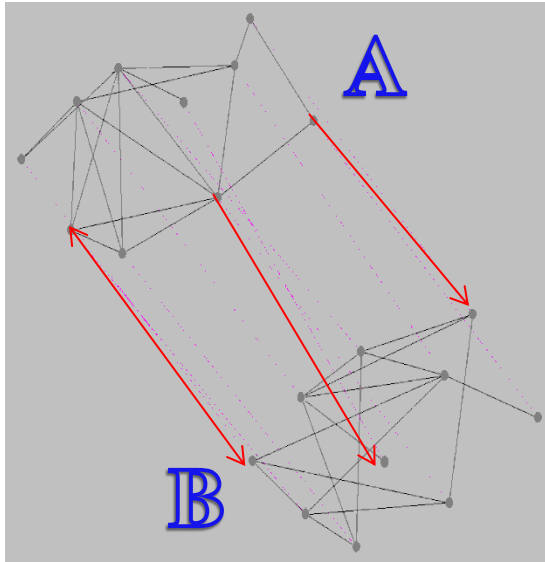
Coupled networks:

New paradigm-Abrupt transition

Cascading Failures

Message: our world is extremely unsafe!

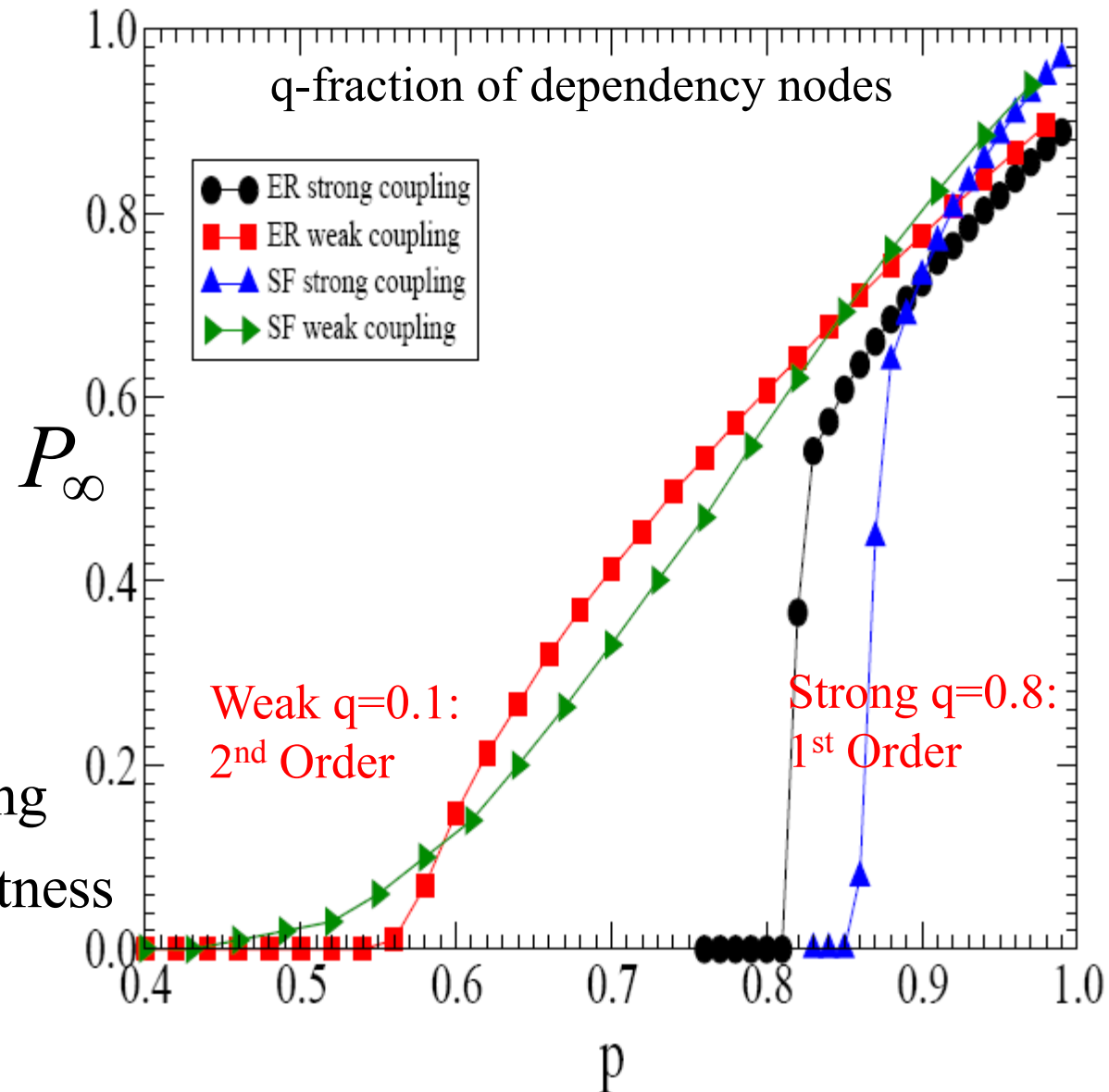
GENERALIZATION: PARTIAL DEPENDENCE: Theory and Simulations



Parshani, Buldyrev, S.H.
PRL, **105**, 048701 (2010)

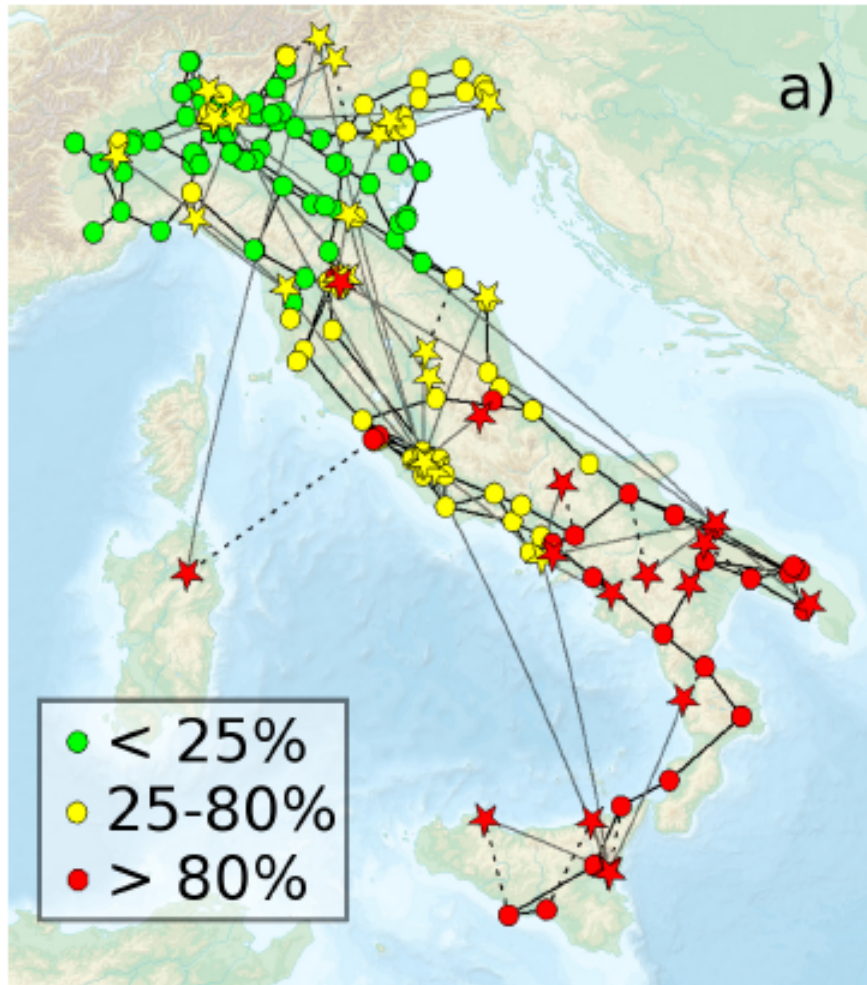
$q_c \cong 0.2$ for random coupling
 $q_c \rightarrow 0.9$ for optimal robustness

Schneider et al
Scientific Reports (2013)

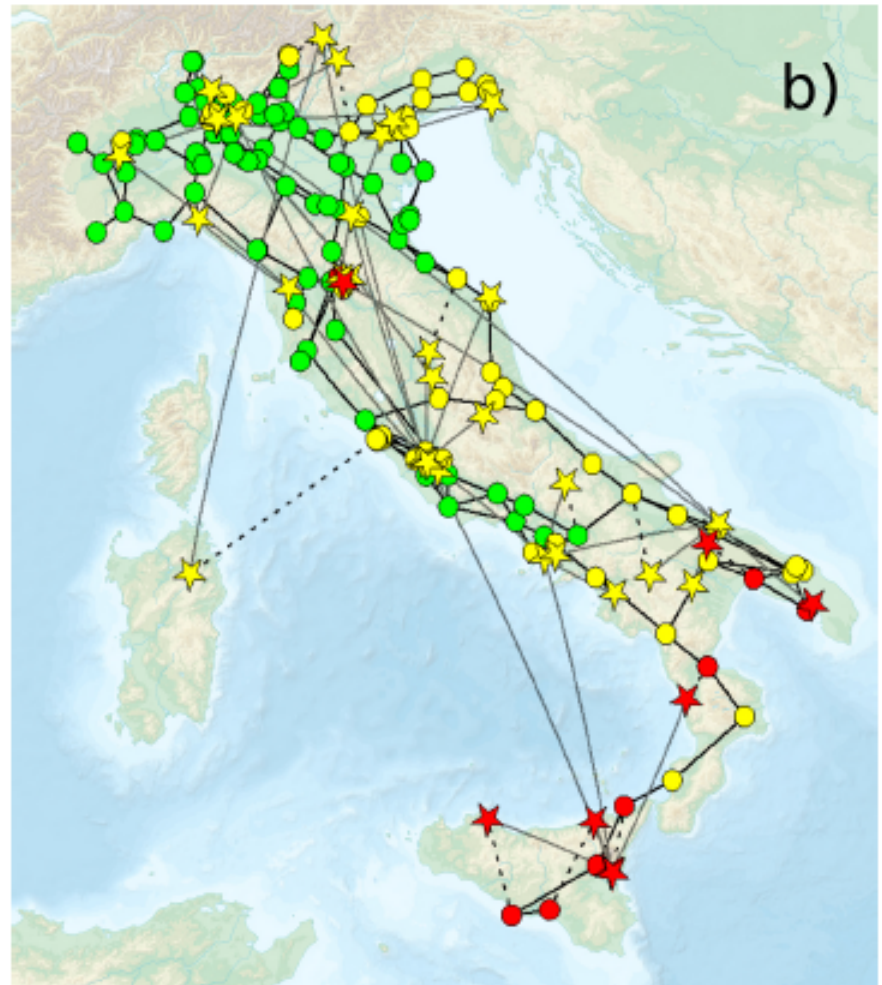


Designing Robust Coupled Networks: Italy 2003 blackout

Random interdependencies

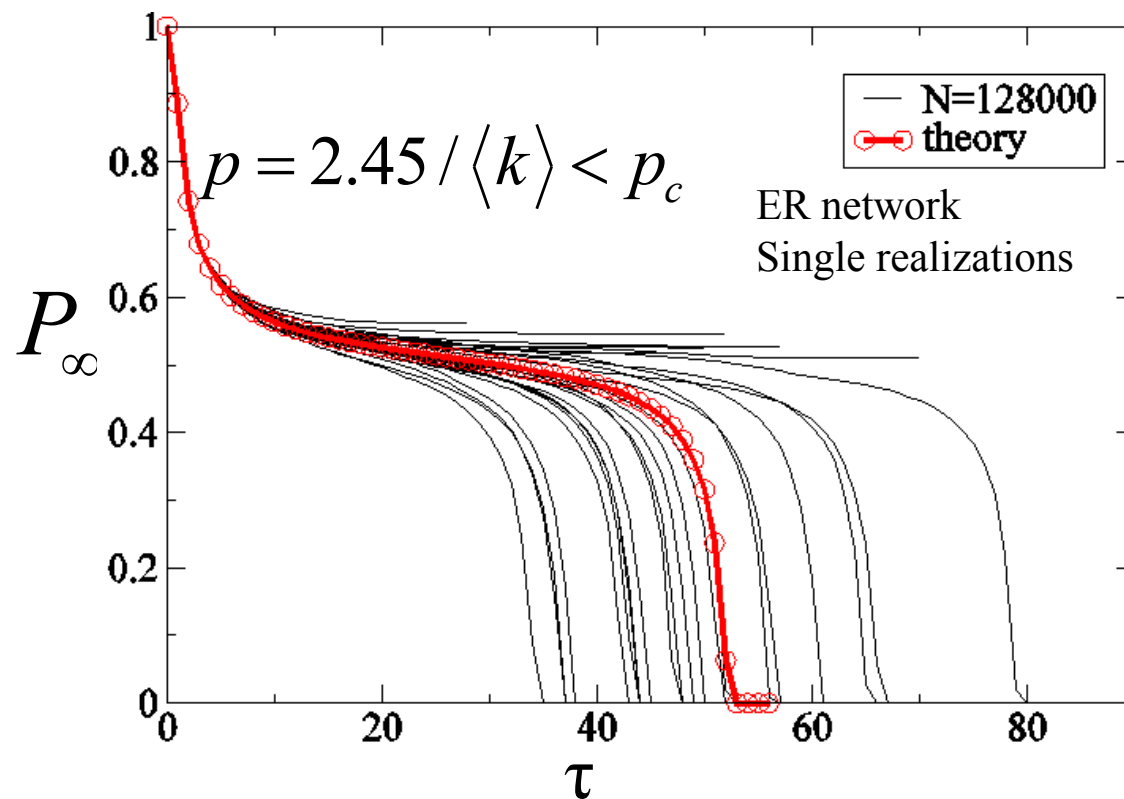


Nearly optimal interdependencies

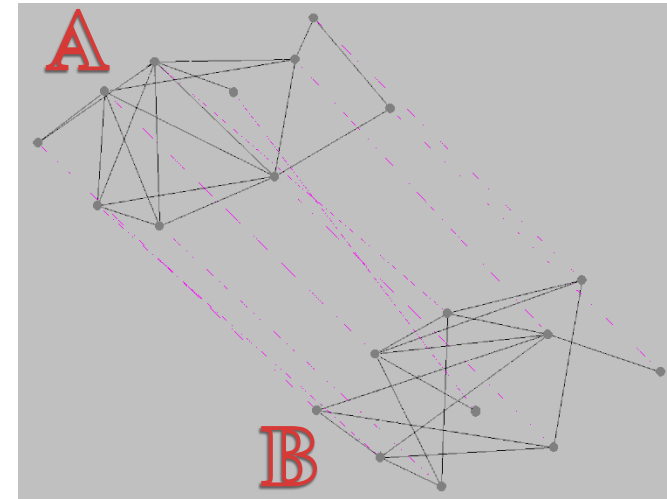


RESULTS: THEORY and SIMULATIONS: ER Networks

P_∞ after τ -cascades of failures



Removing 1-p nodes in A



Catastrophic cascades
just below p_c

ABRUPT TRANSITION (1st order)

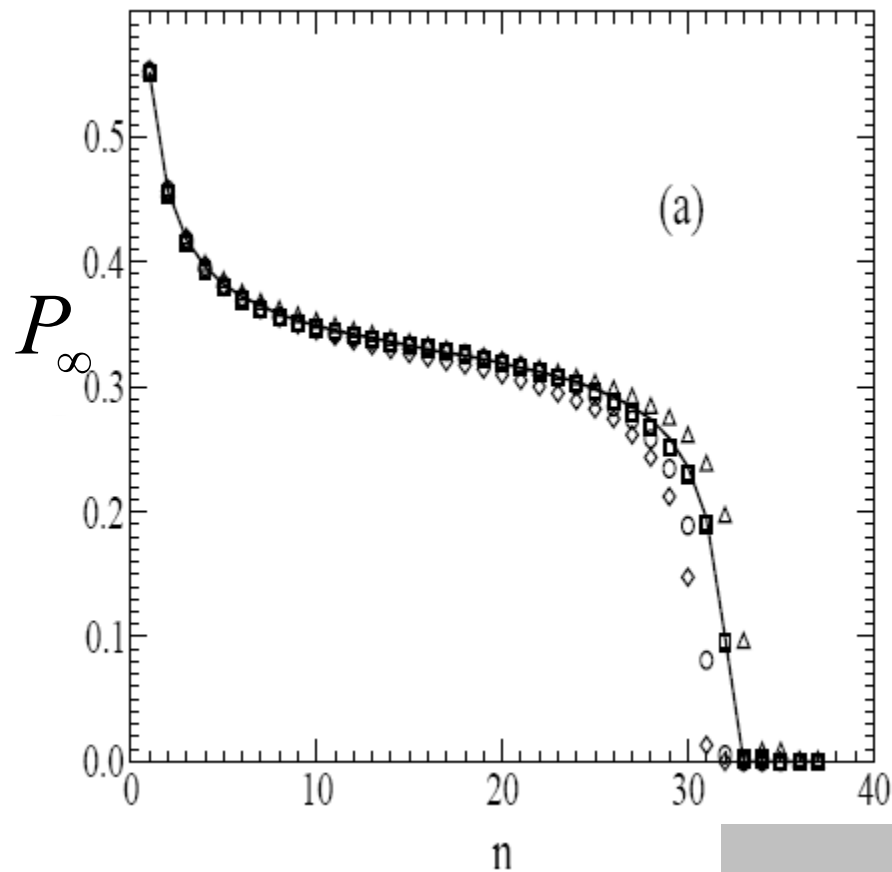
$$p_c = 2.4554 / \langle k \rangle \quad \text{For a single network } p_c = 1 / \langle k \rangle$$

$$\langle k \rangle_{\min} = 2.4554 \quad \text{for single network } \langle k \rangle_{\min} = 1$$

$$\langle \tau \rangle \sim N^{1/3}$$

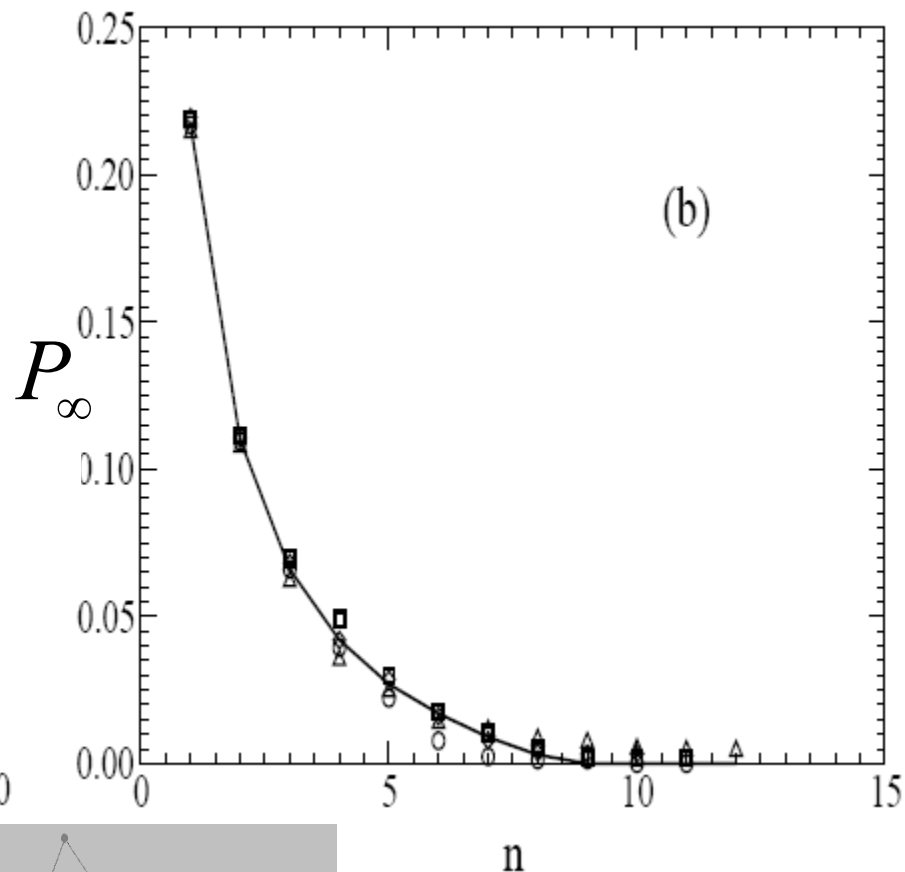
Dong Zhou et al (2013)

Strong Coupling

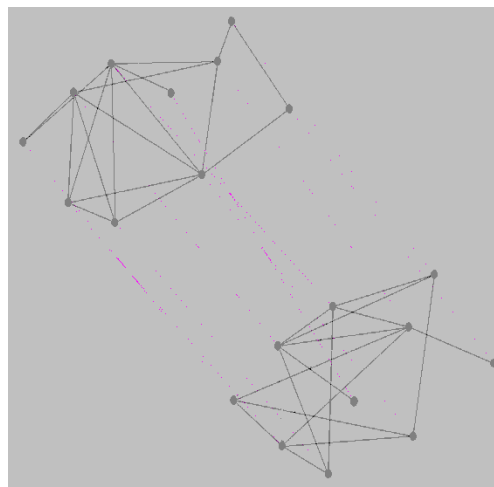


$q=0.8$

Weak Coupling

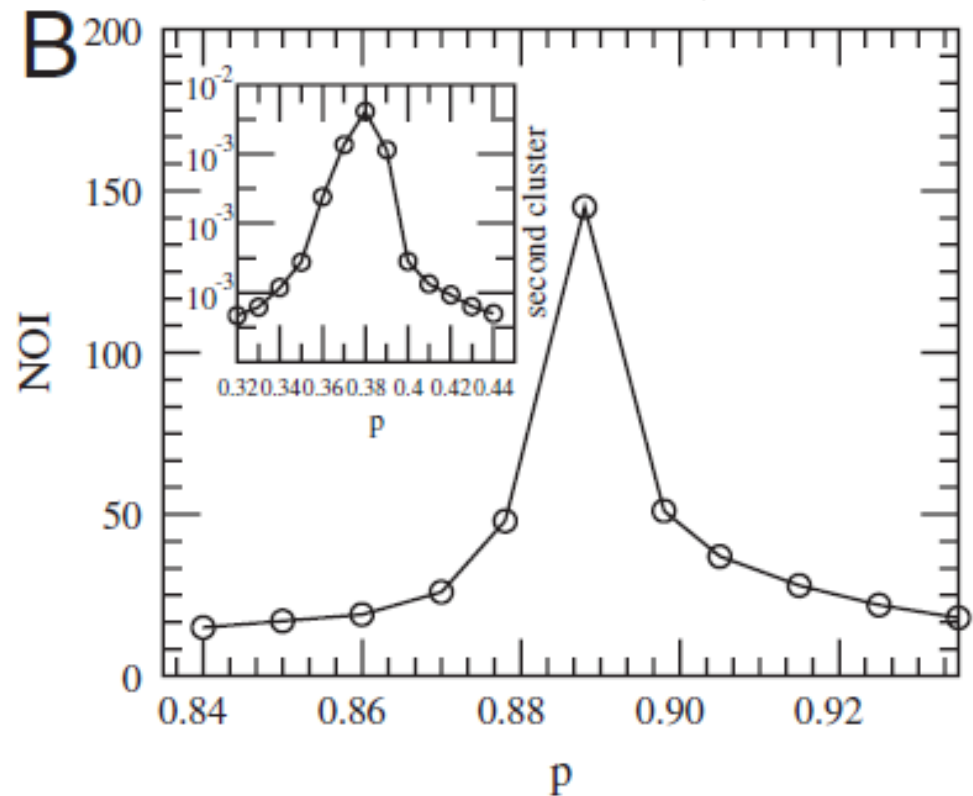
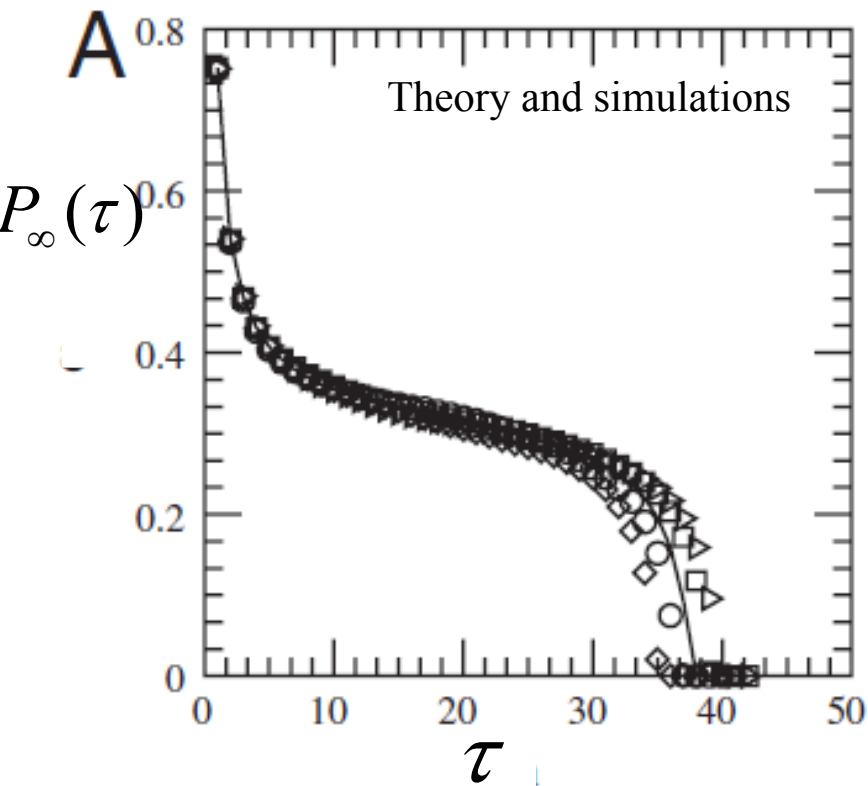
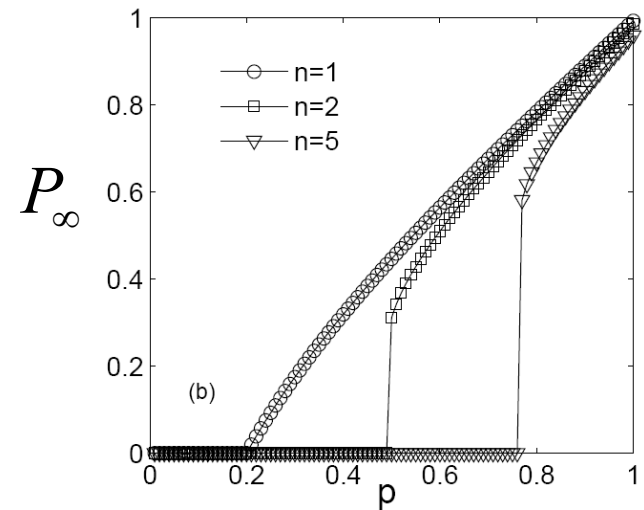
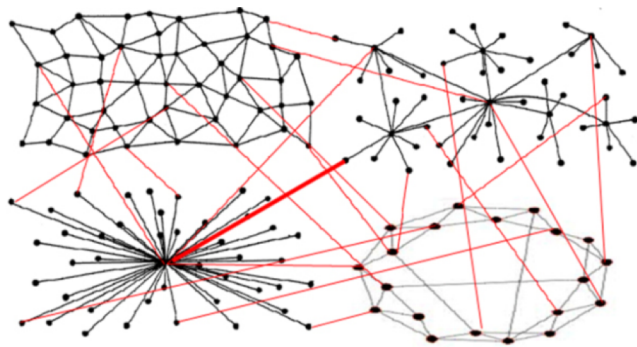


$q=0.1$



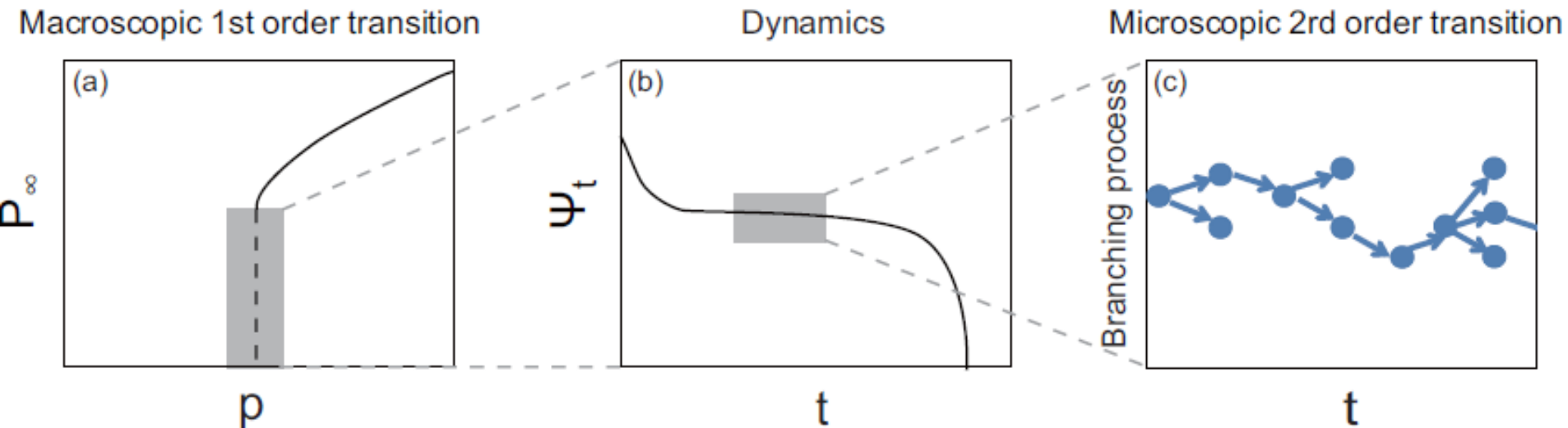
Interdependent Networks

Determining p_c simulations

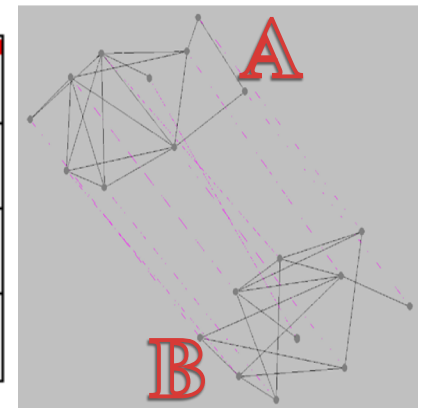
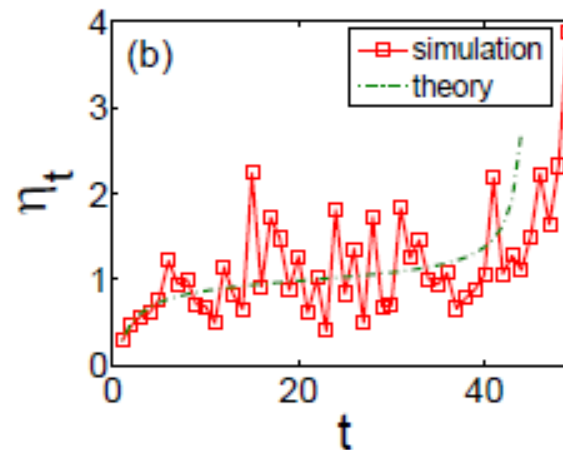
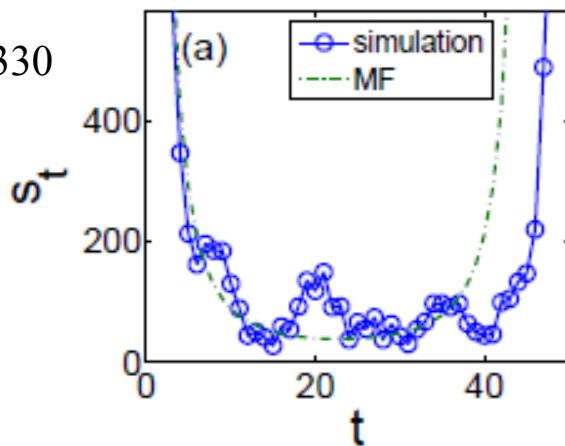


Origin of Plateau

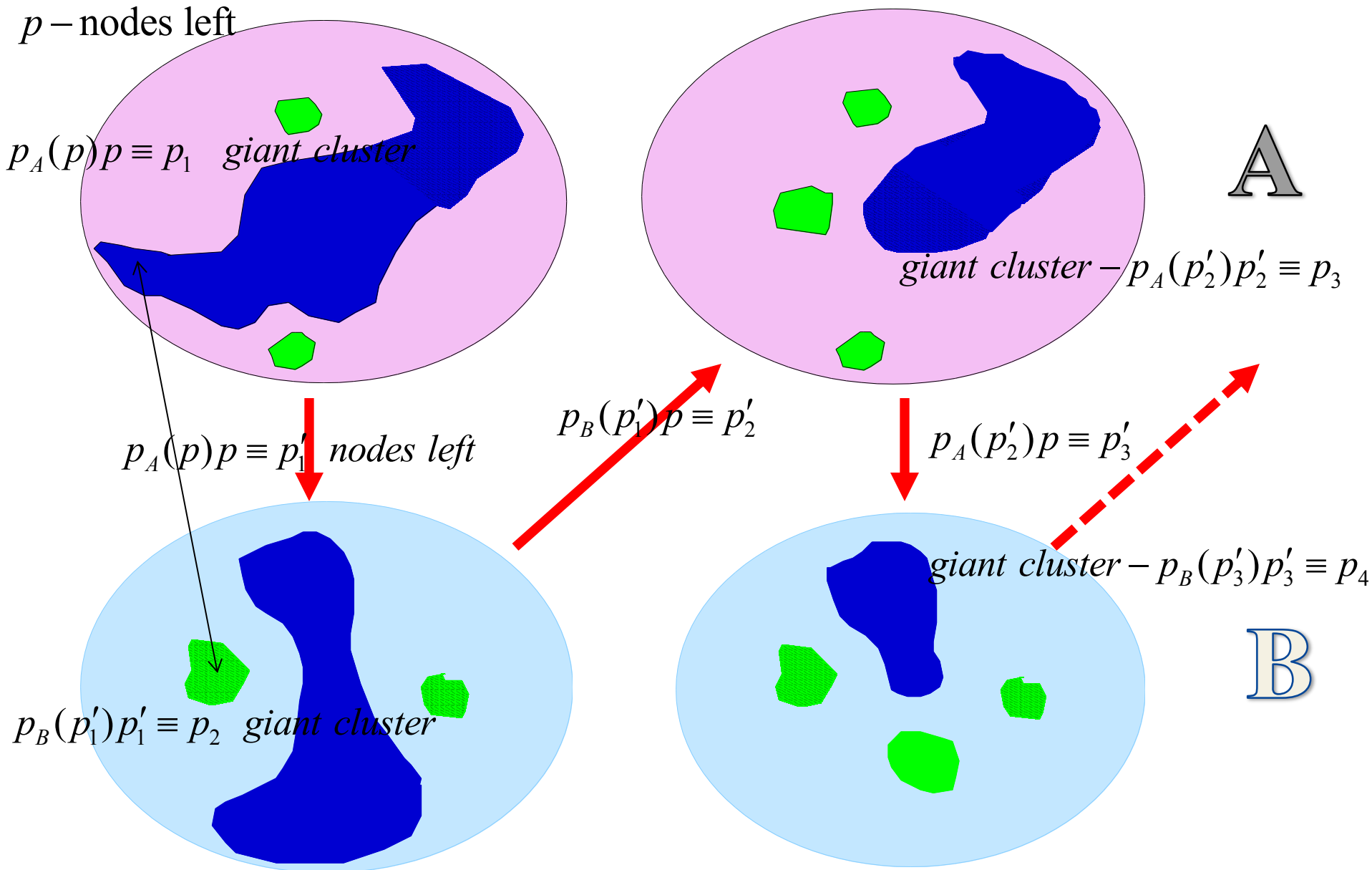
Simultaneous first and second order percolation transitions



Dong et al,
arXiv:1211.2330
PRE (2014)

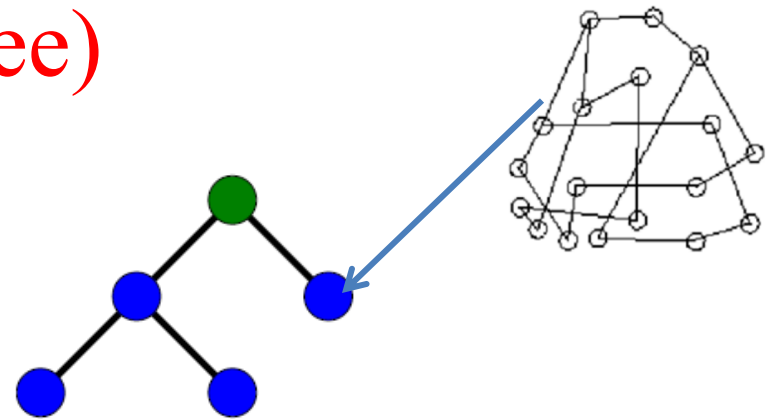
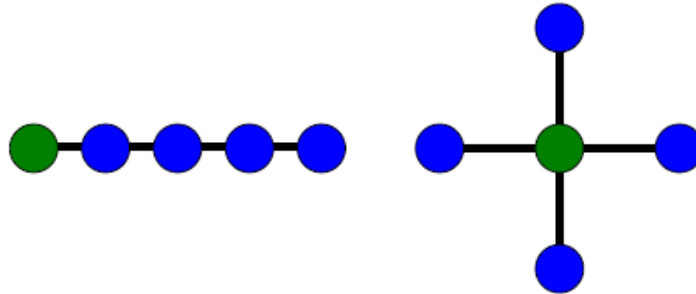


RANDOM REMOVAL – PERCOLATION FRAMEWORK



Network of Networks (tree)

n=5

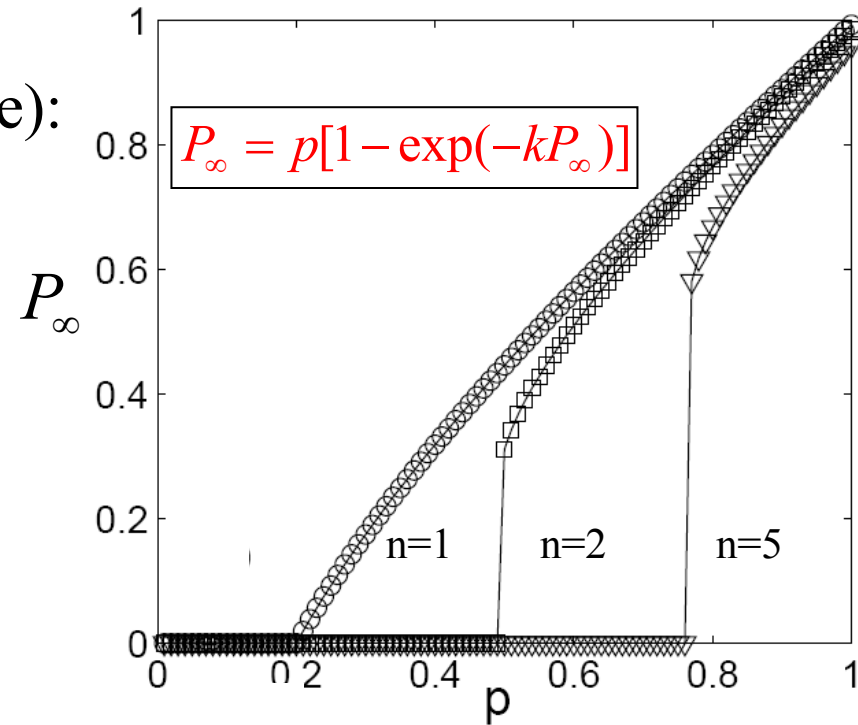


For ER, $\langle k_i \rangle = k$, **full** coupling $q=1$,
ALL loopless topologies (chain, star, tree):

$$P_{\infty} = p[1 - \exp(-kP_{\infty})]^n$$

n=1 known ER- 2nd order

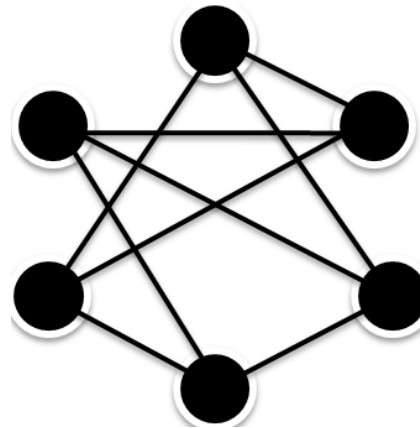
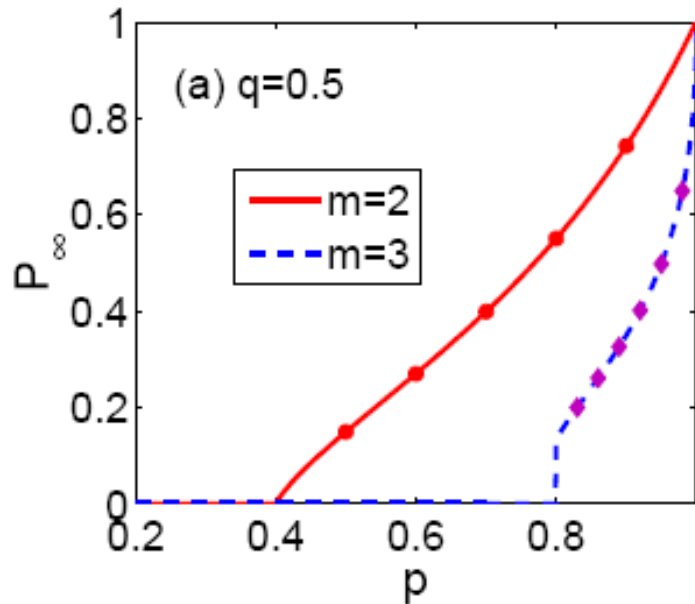
$$p_c = 1 / \langle k \rangle$$



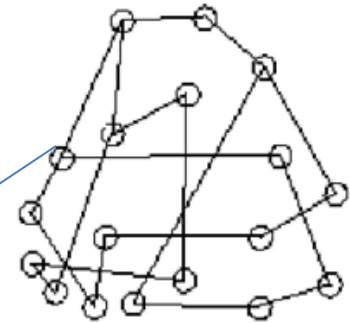
Buldyrev et al, Nature, 464, 1025 (2010)
 Parshani et al, PRL, 105, 0484 (2010)
 Parshani et al, PNAS, 108, 1007 (2011)
 Gao et al PRL (2011)

Vulnerability increases significantly with n

Random Regular Network of ER networks



RR, $m=3$



ER $\langle k \rangle = 2.2$

$$P_\infty = \frac{p}{2^m} (1 - e^{-\langle k \rangle P_\infty}) [1 - q + \sqrt{(1 - q)^2 + 4qP_\infty}]^m$$

$$p_c = \frac{1}{\langle k \rangle (1 - q)^m}$$

$$q_c = \frac{\langle k \rangle + m - \sqrt{m^2 + 2\langle k \rangle m}}{\langle k \rangle}$$

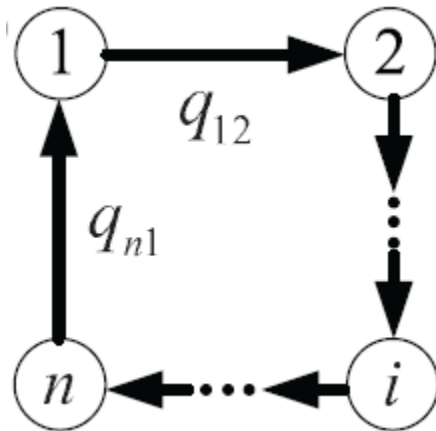
Surprisingly Independent on n !

For $m = 0$ OR $q = 0$
the single network
is obtained!

$$P_\infty = p[1 - \exp(-\langle k \rangle P_\infty)]$$

Network of Networks (loop)

GENERAL FRAMEWORK -- PARTIAL DEPENDENCE



For ER networks:

$$P_{\infty} = p[1 - \exp(-kP_{\infty})(qP_{\infty} - q + 1)]$$

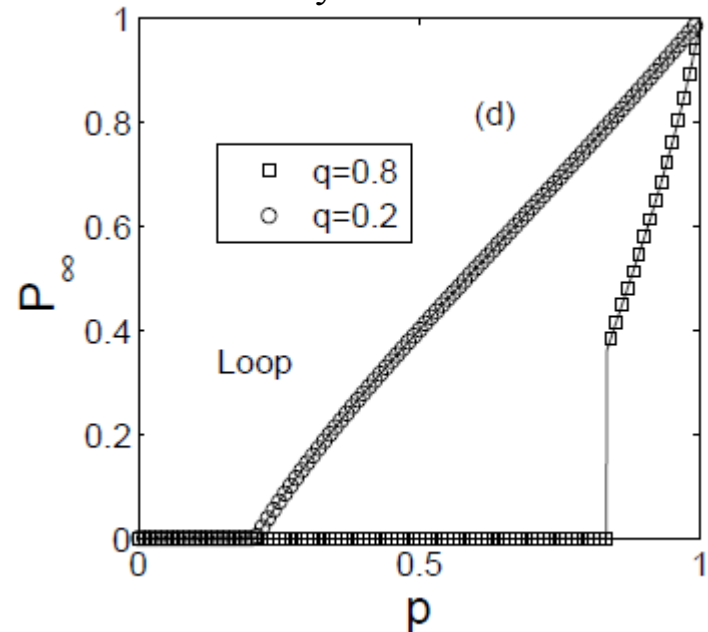
No dependence on m

For $q = 1$, $P_{\infty} = 0$ -no giant component for any p

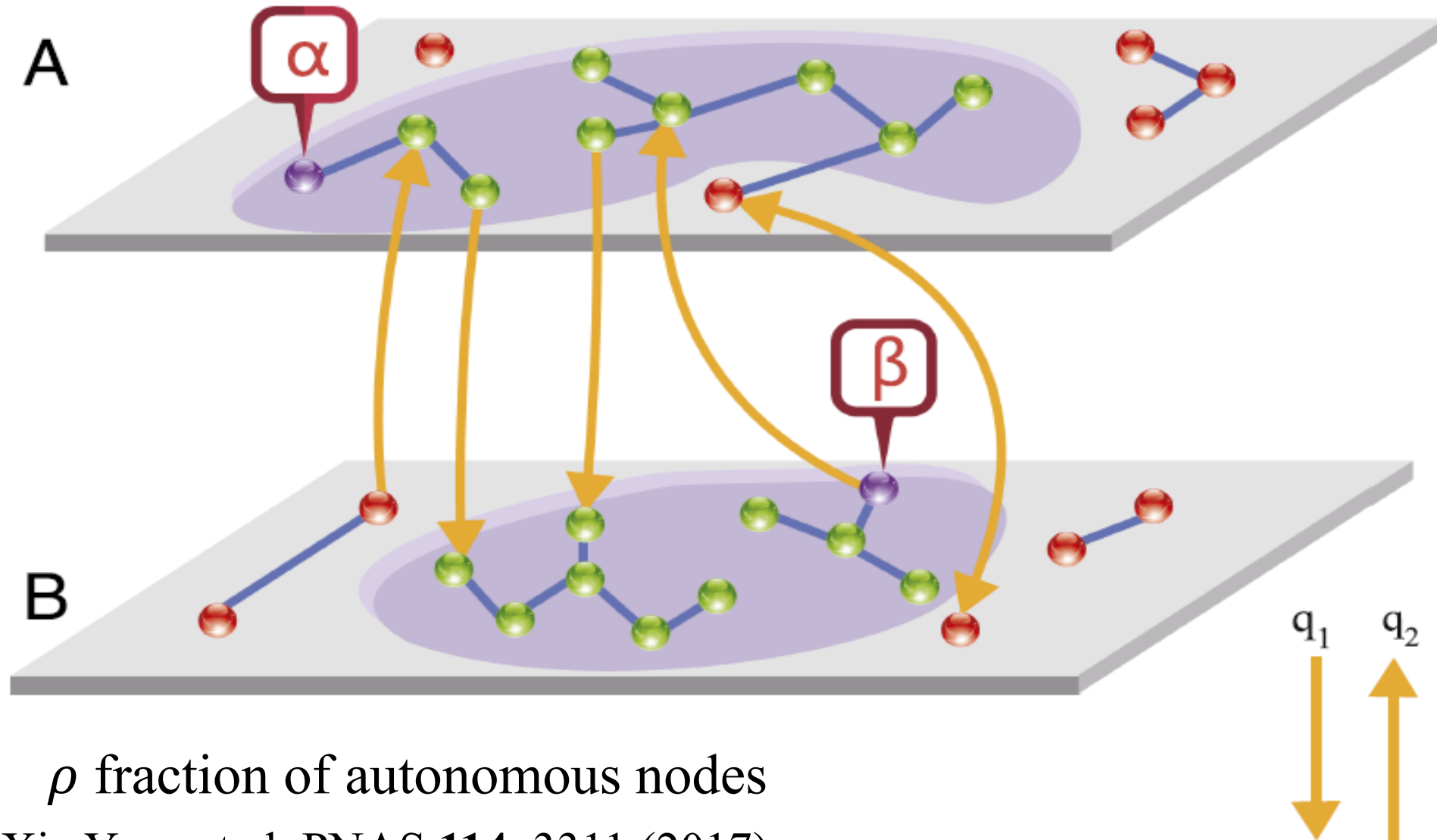
For $q = 0$, the known single network result

Jianxi Gao et al, PRL (2011)

Theory and Simulations



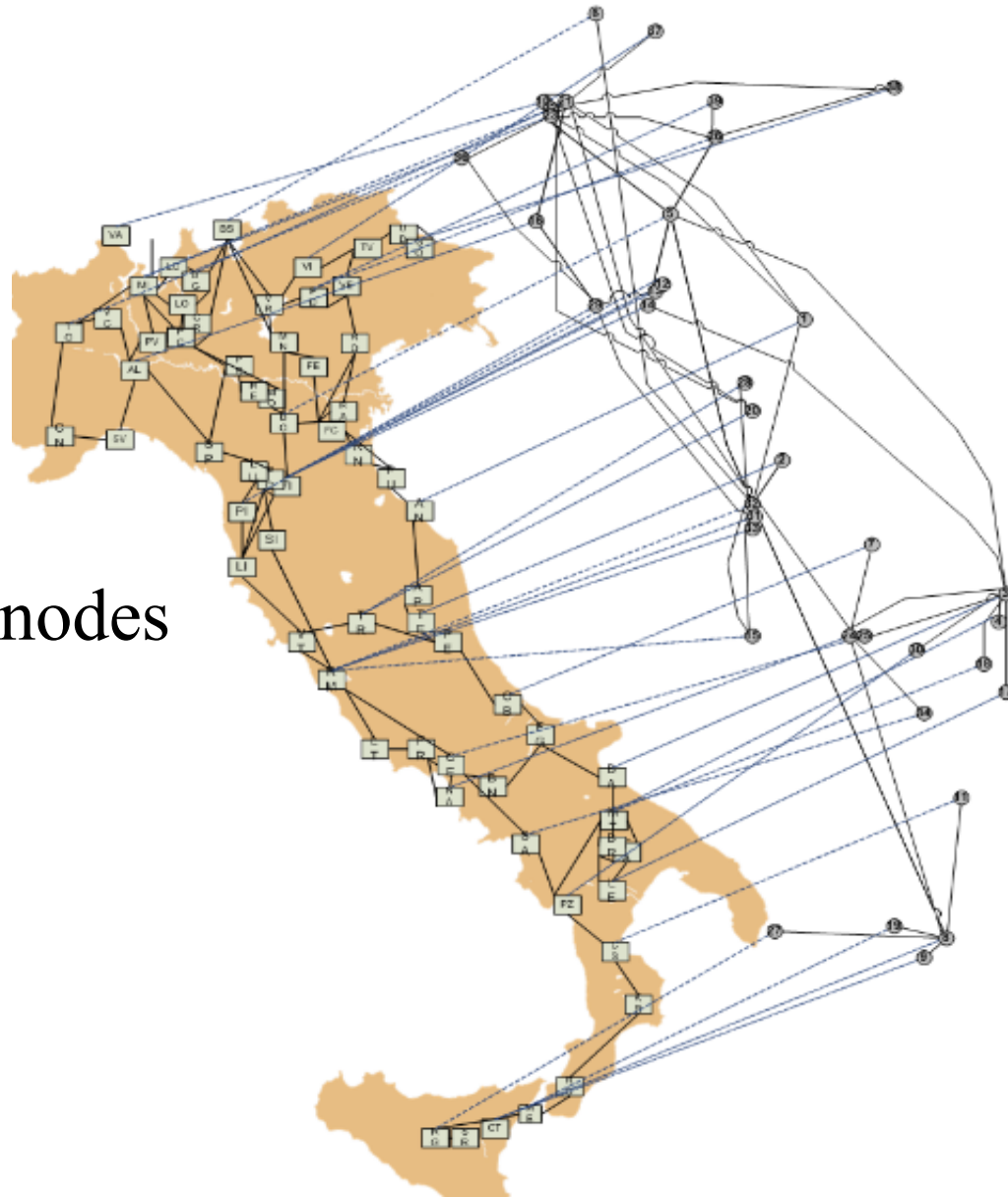
Eradicating abrupt collapse in interdependent networks via reinforced nodes



ρ fraction of autonomous nodes

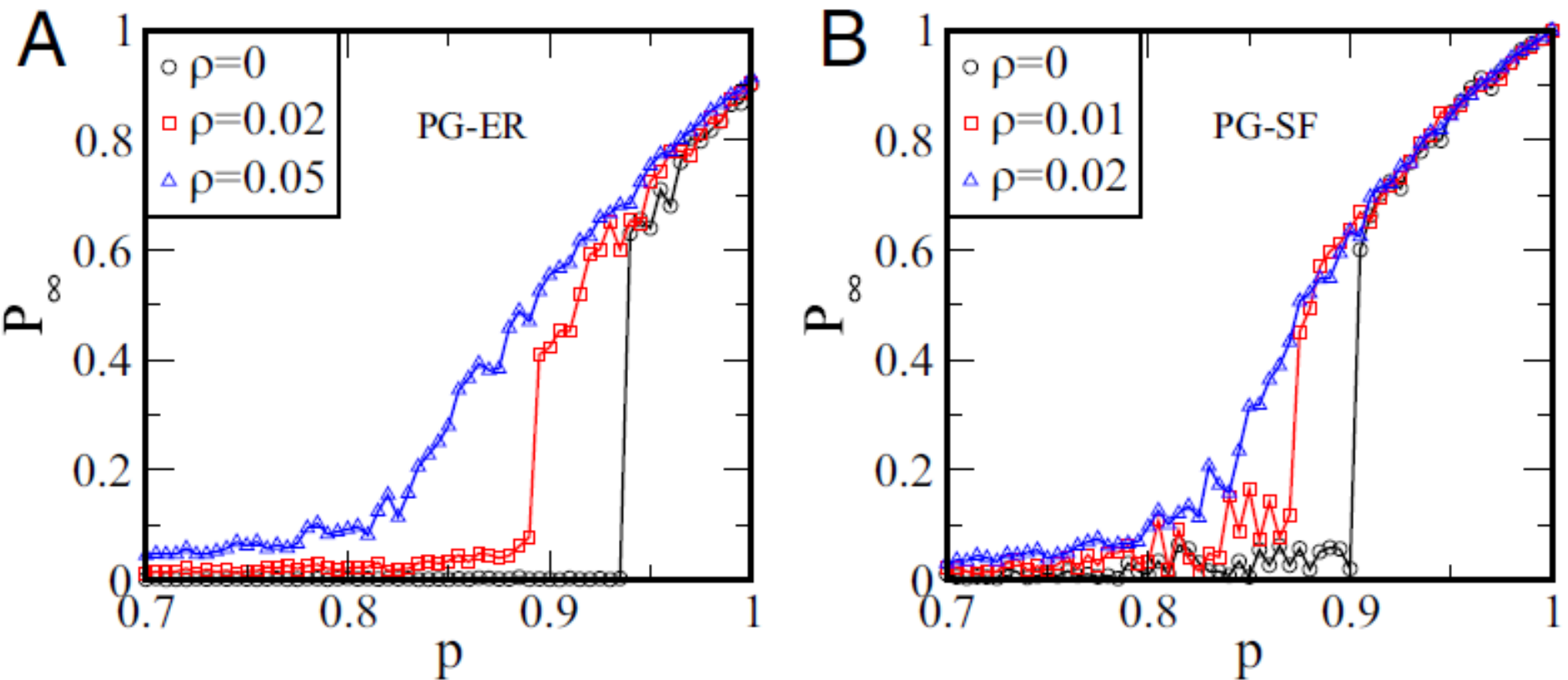
Xin Yuan et al, PNAS **114**, 3311 (2017)

Preventing catastrophic collapse in interdependent networks via reinforced nodes



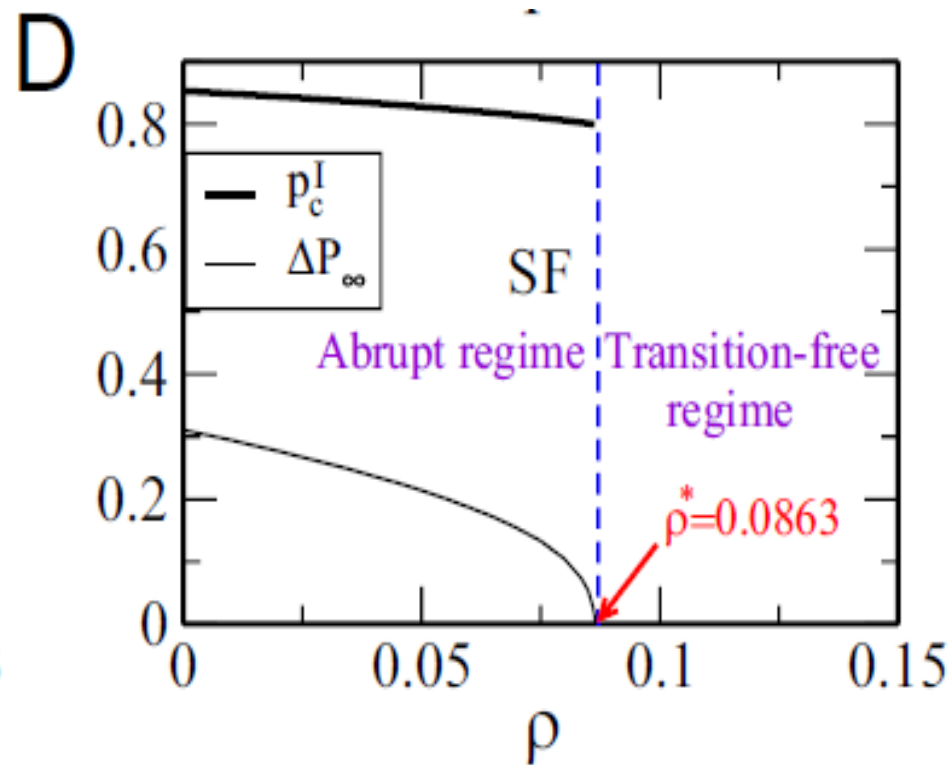
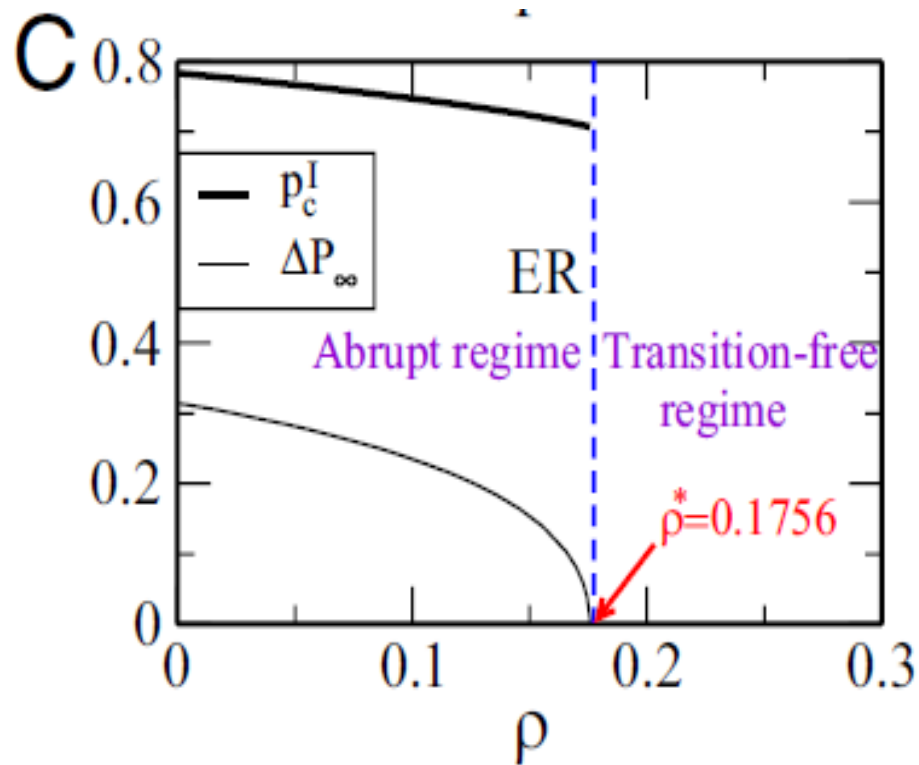
ρ fraction of
autonomous nodes

Eradicating catastrophic collapse in interdependent networks via reinforced nodes- Real Data--- US Power grid



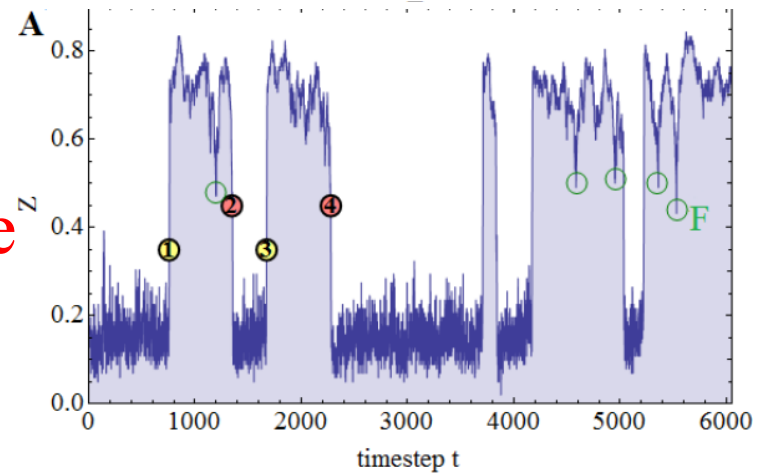
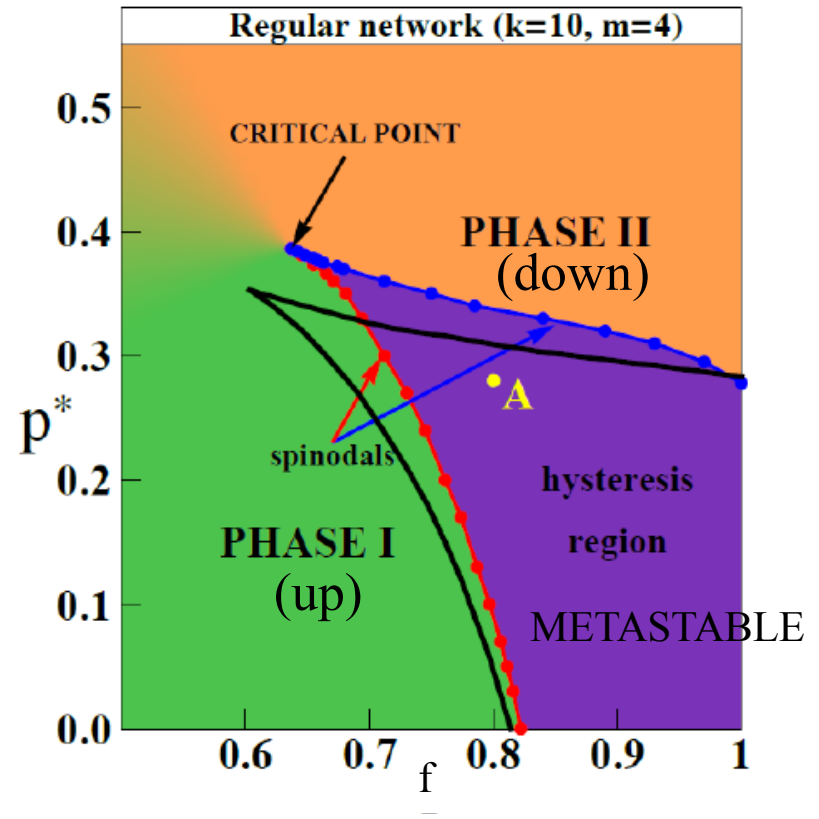
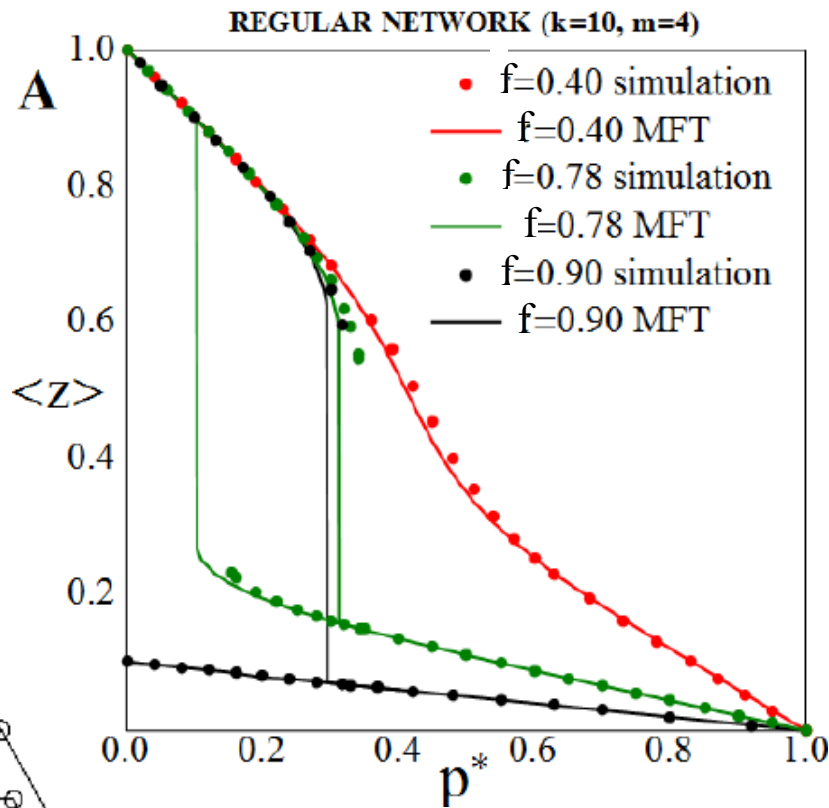
Few percent of autonomous power stations and communication systems can avoid abrupt collapse

Eradicating catastrophic collapse in interdependent networks via reinforced nodes



$$\rho^* = 1 - \frac{\exp \left\{ \frac{1}{2} \left[1 - \langle k \rangle (1 - q)^2 / 2q \right] \right\}}{2 - \sqrt{\langle k \rangle (1 - q)^2 / 2q}}$$

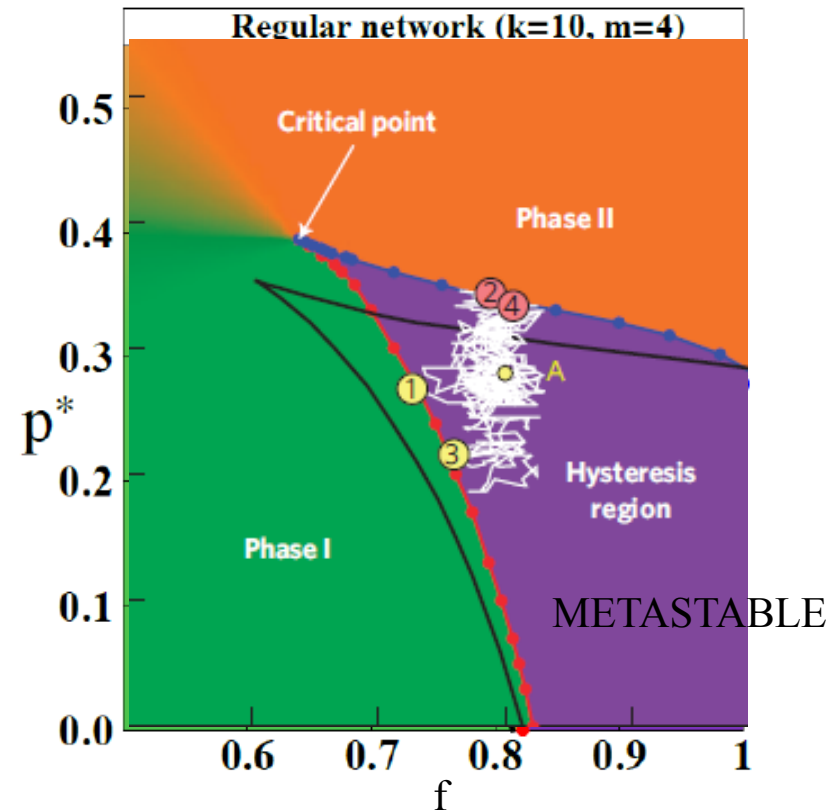
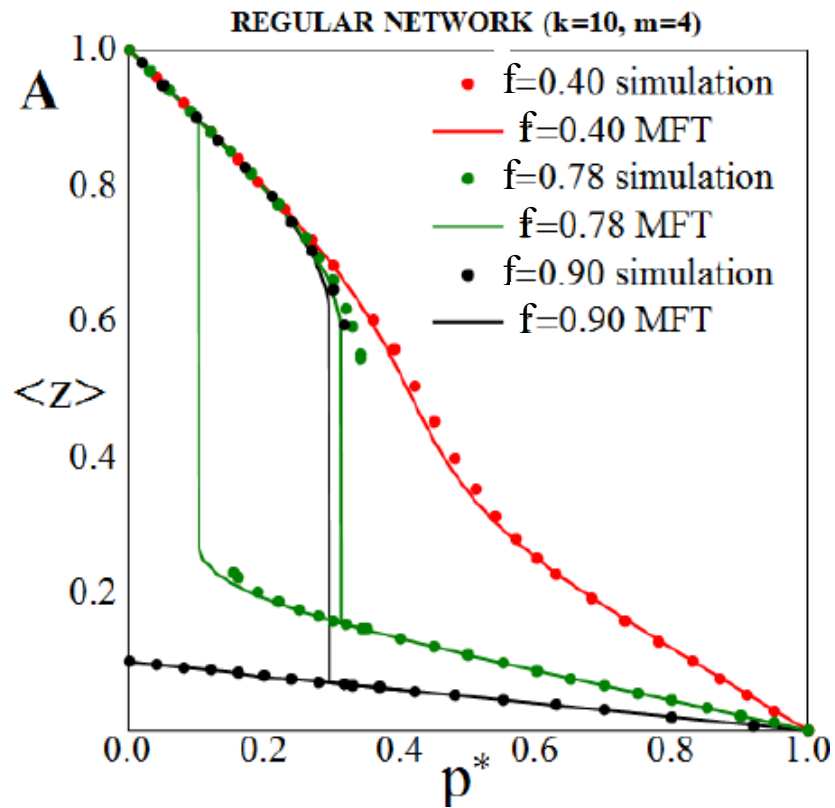
Introducing Recovery-Single Networks



Spontaneous Recovery and Failure

Majdanzik et al Nature Phys. 10, 3438 (2014)

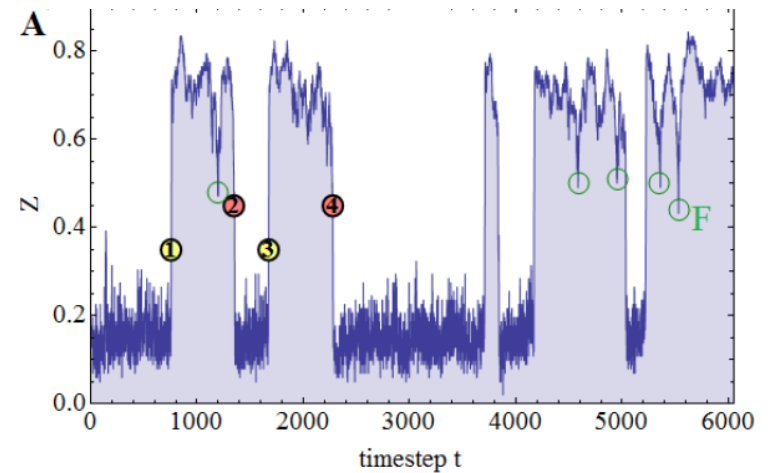
Introducing Recovery-Single Networks



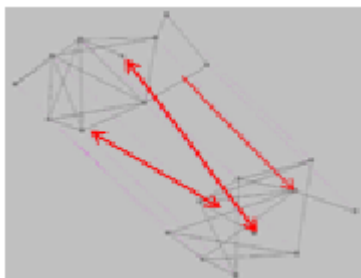
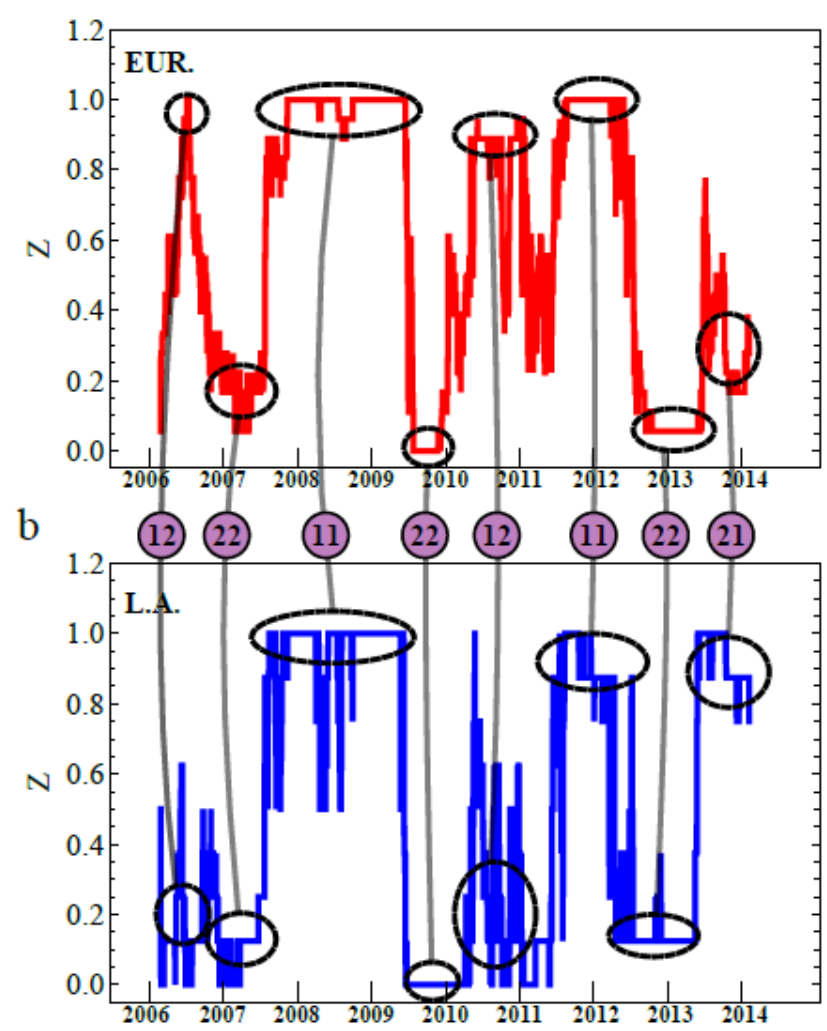
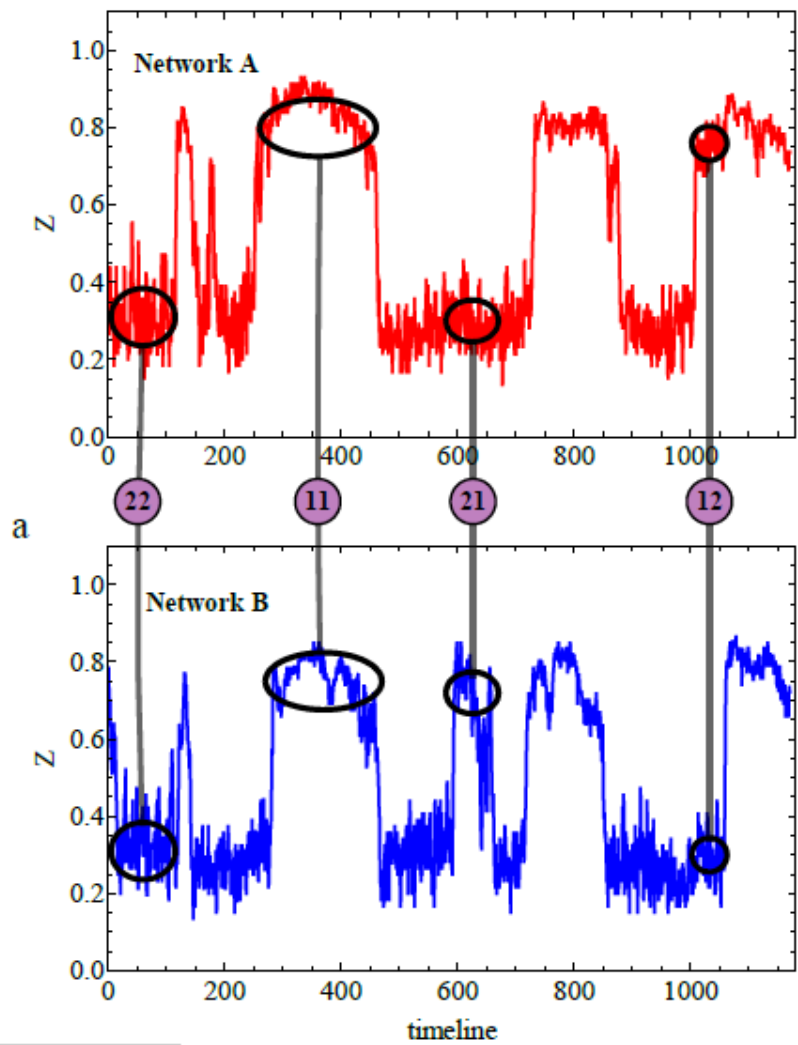
Diffusion of a SYSTEM in phase space

Spontaneous Recovery and Failure

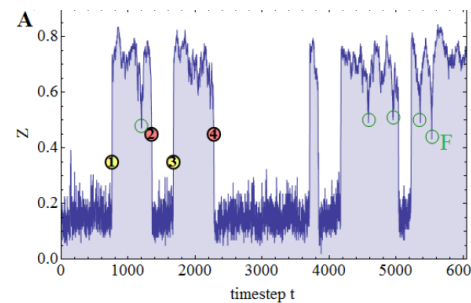
Majdanzik et al Nature Phys. 10, 3438 (2014)



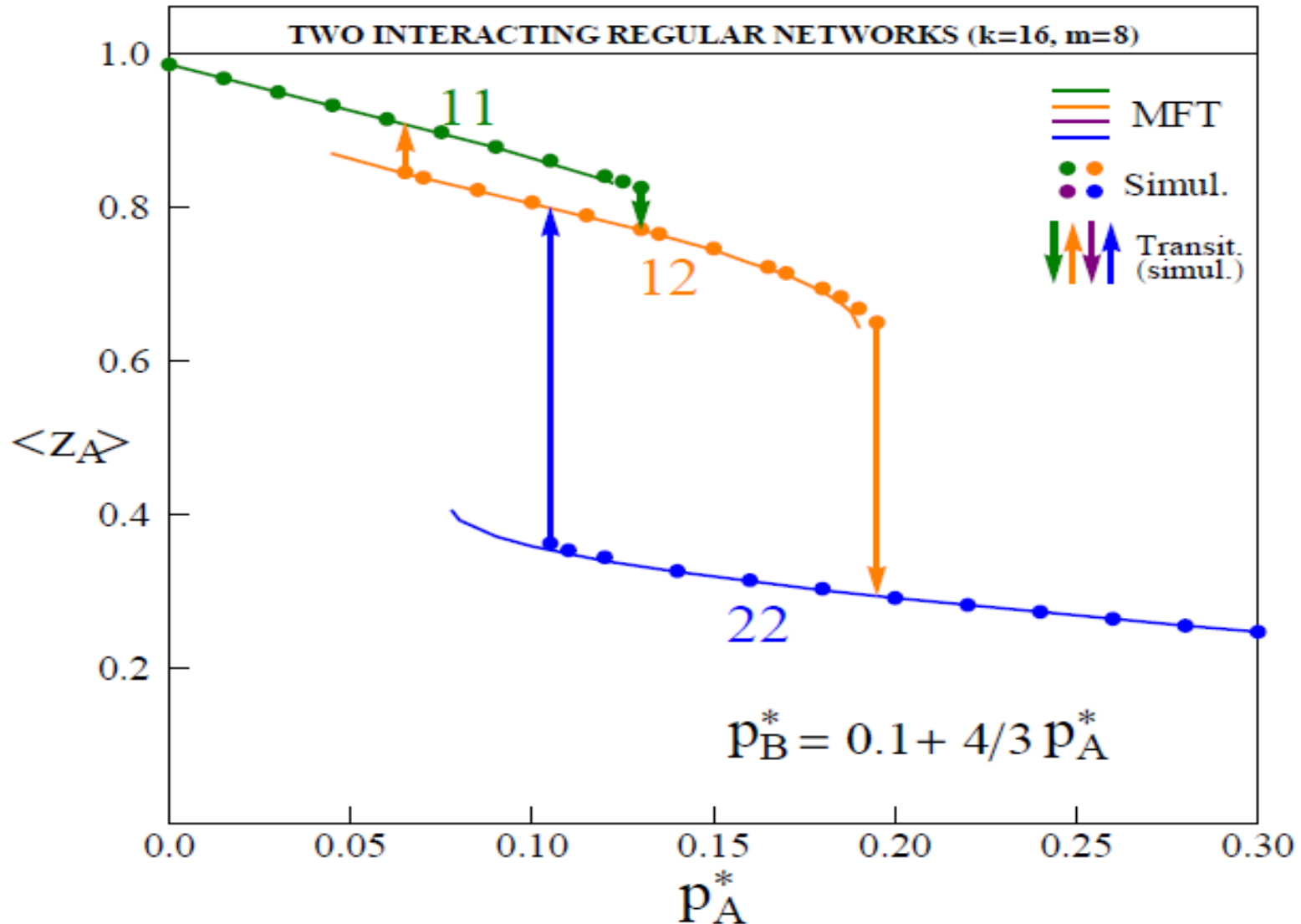
Simultaneous Recovery and Failure of Interdependent Networks



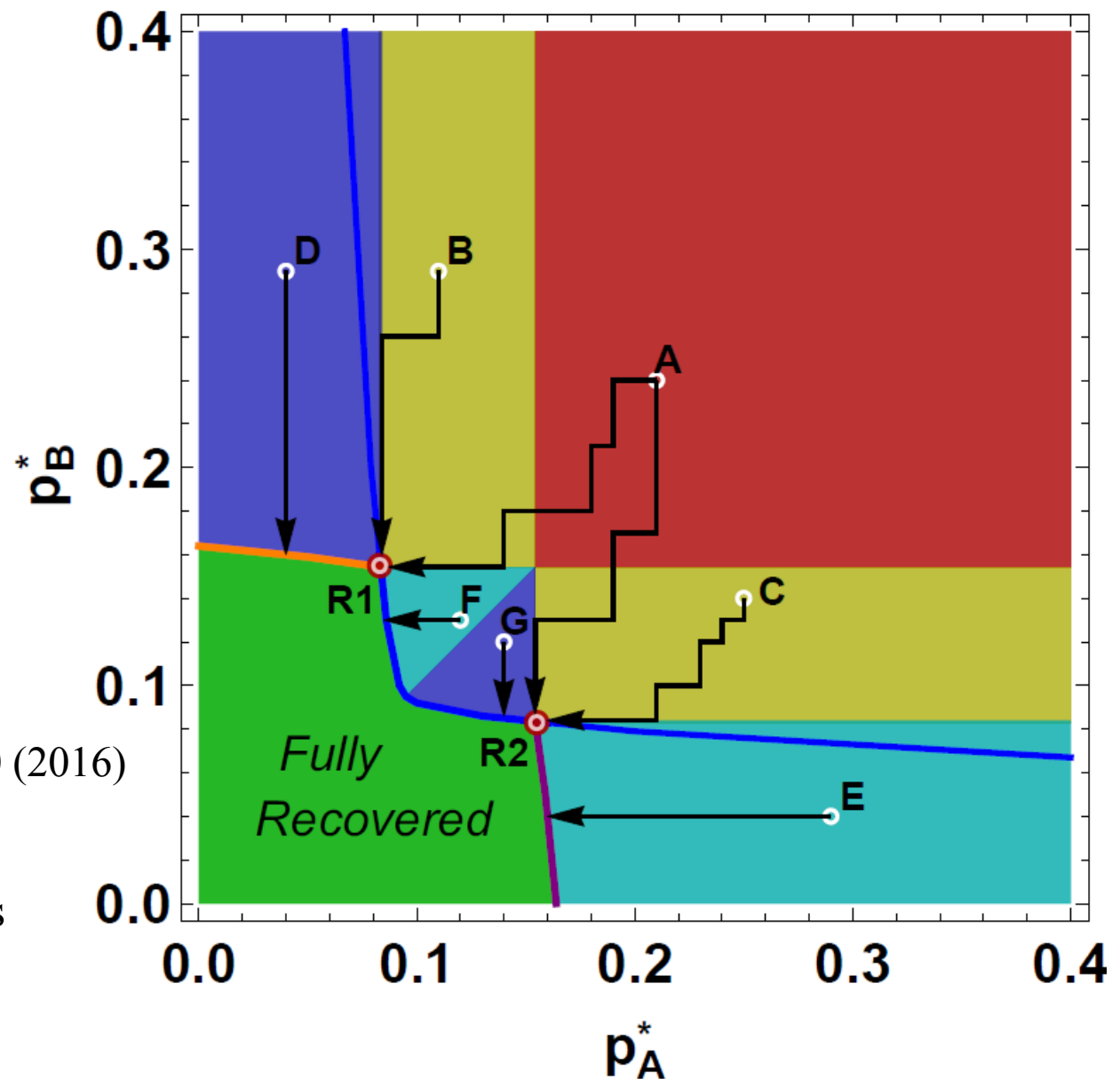
CDS INDEX DATA FROM EUROPE
AND LATIN AMERICA
Majdanzic et al
Nature Comm. 7, 10850 (2016)



Complex Hysteresis-Interdependent Networks



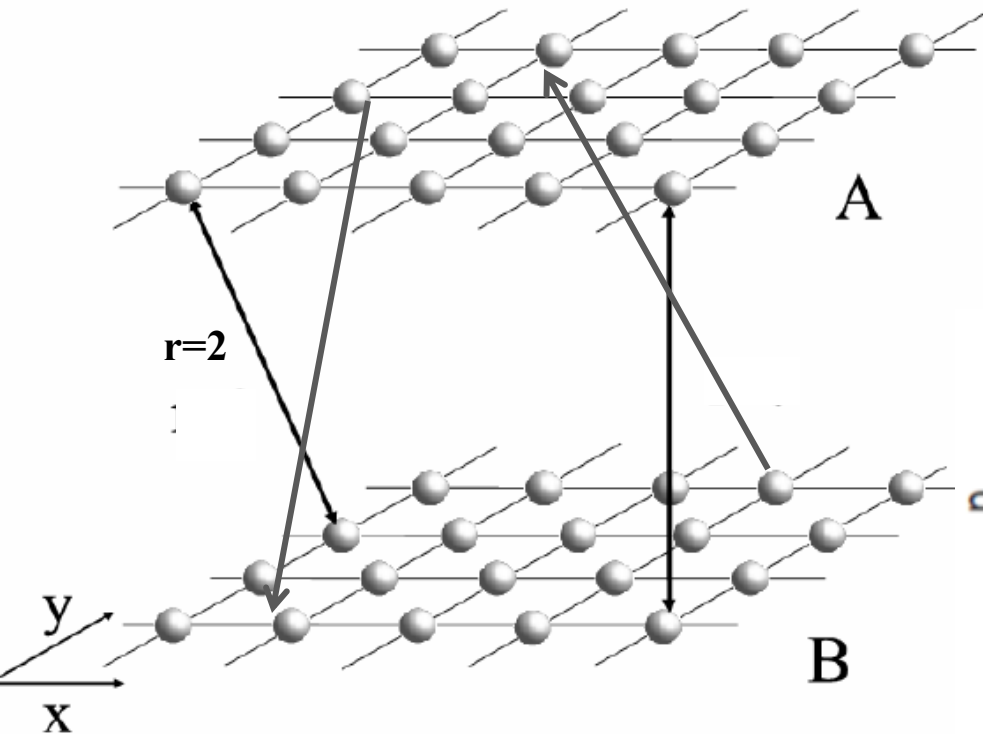
Optimal Repairing Strategies



Majdanzic et al
Nature Comm. 7, 10850 (2016)

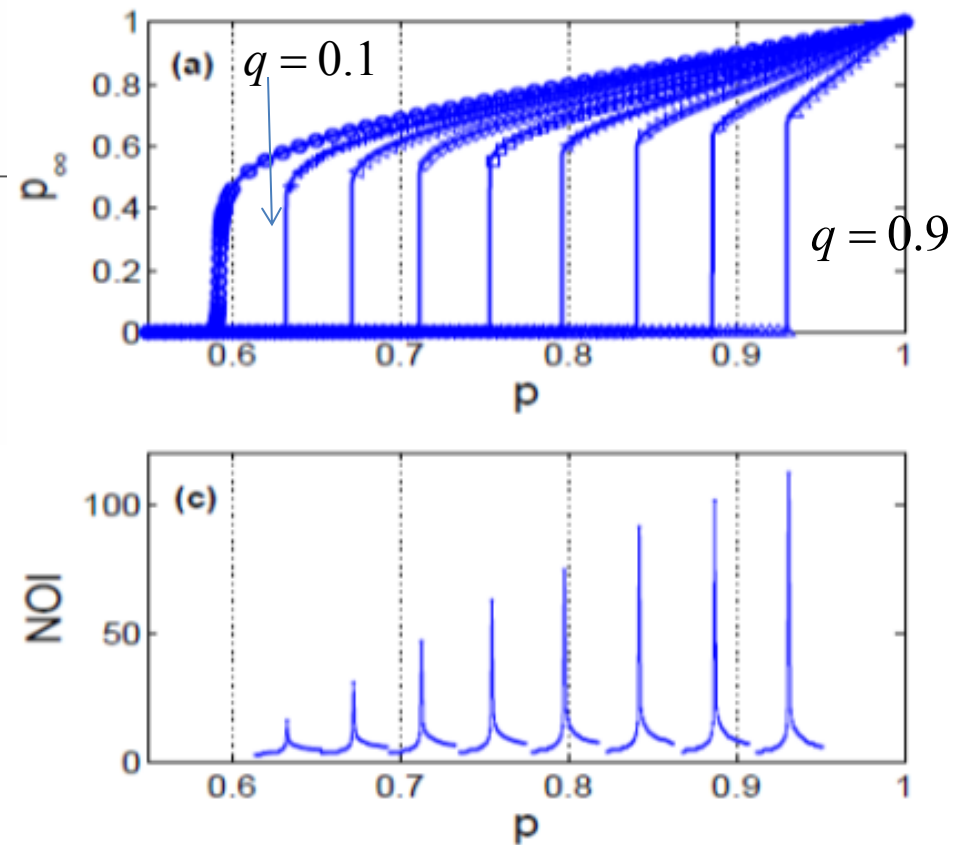
Infrastructure of many
interdependent systems
Species distinction
System collapse

Interdependent Spatially Embedded Networks



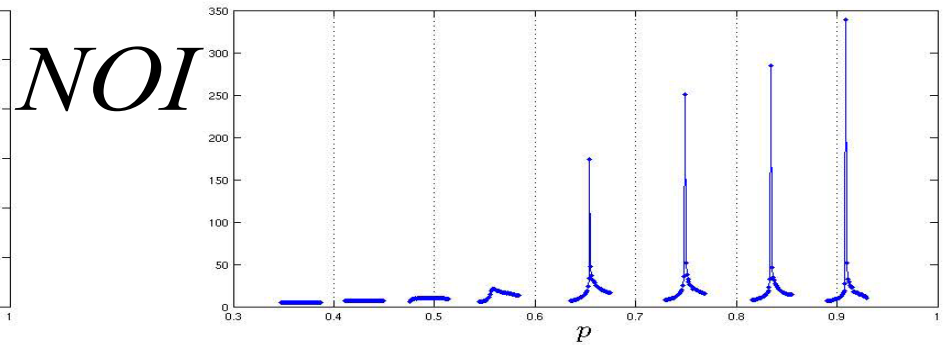
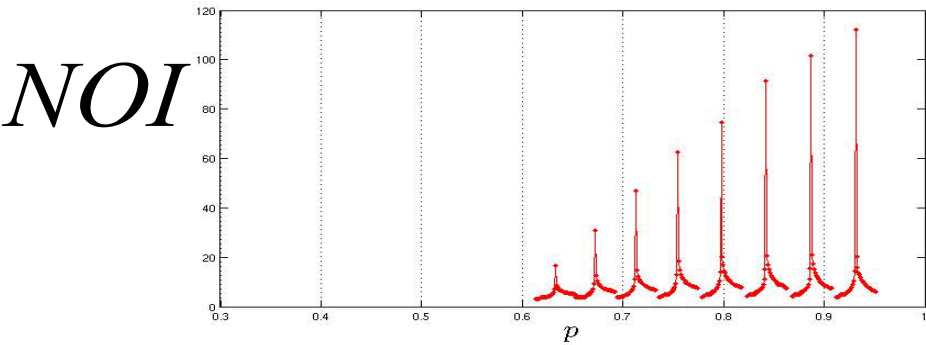
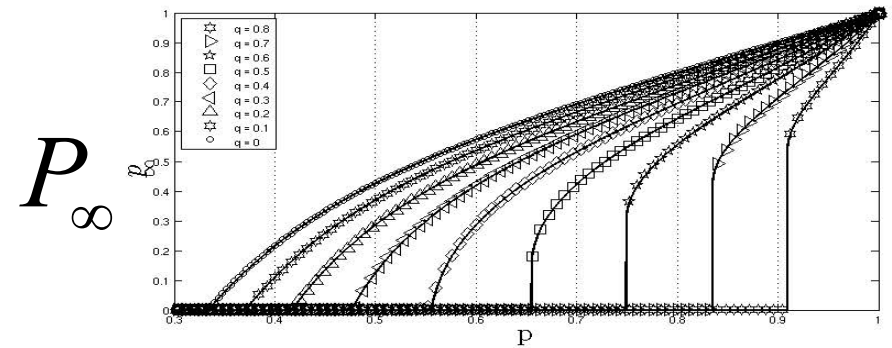
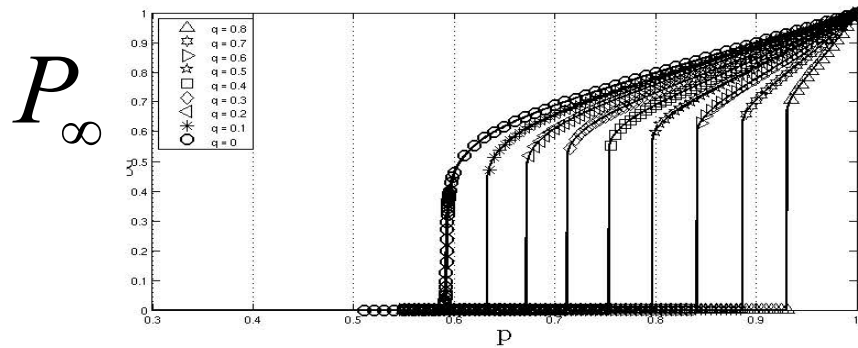
Many networks are spatially embedded:
Internet, Power grid, Transportation etc

Bashan et al, Nature Physics (2013)



Theory (based on critical exponent):
NO continuous transition
for any $q > 0$ -extreme vulnerability!!

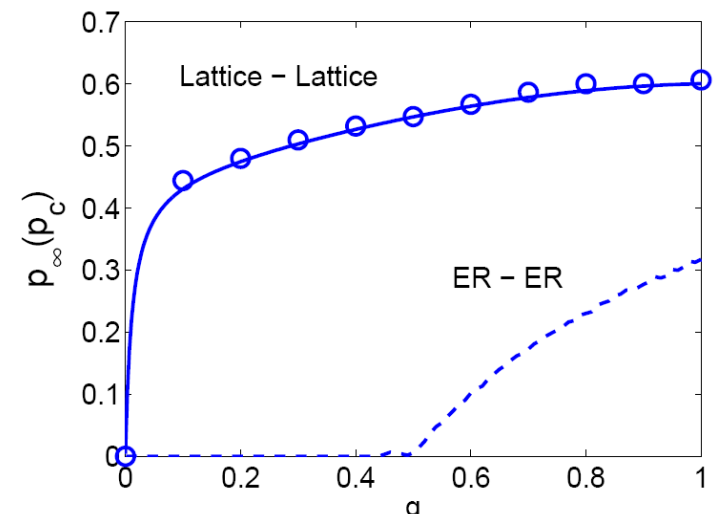
The extreme vulnerability of spatial embedded coupled networks



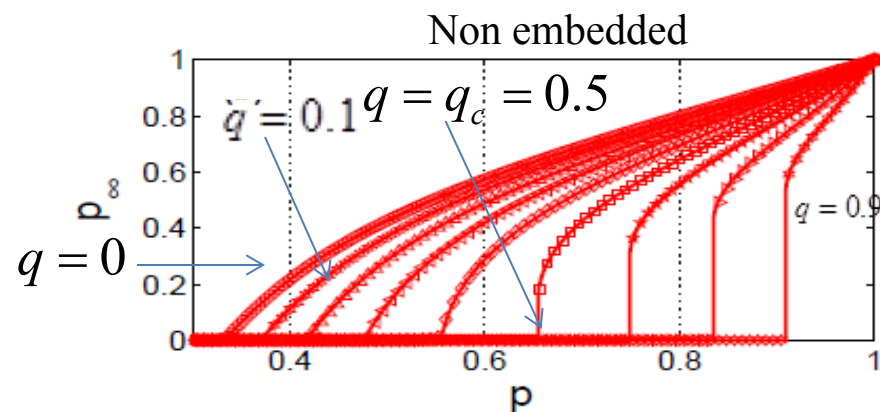
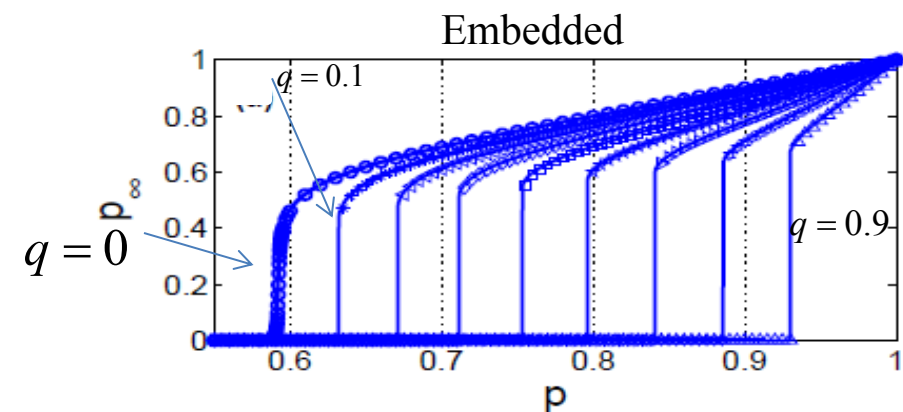
EXTREMELY VULNERABLE!!

Bashan et al
<http://arxiv.org/abs/1206.2062>

$$q_c = 0$$



Spatial embedded compared to random coupled networks when q changes



EXTREMELY VULNERABLE!!

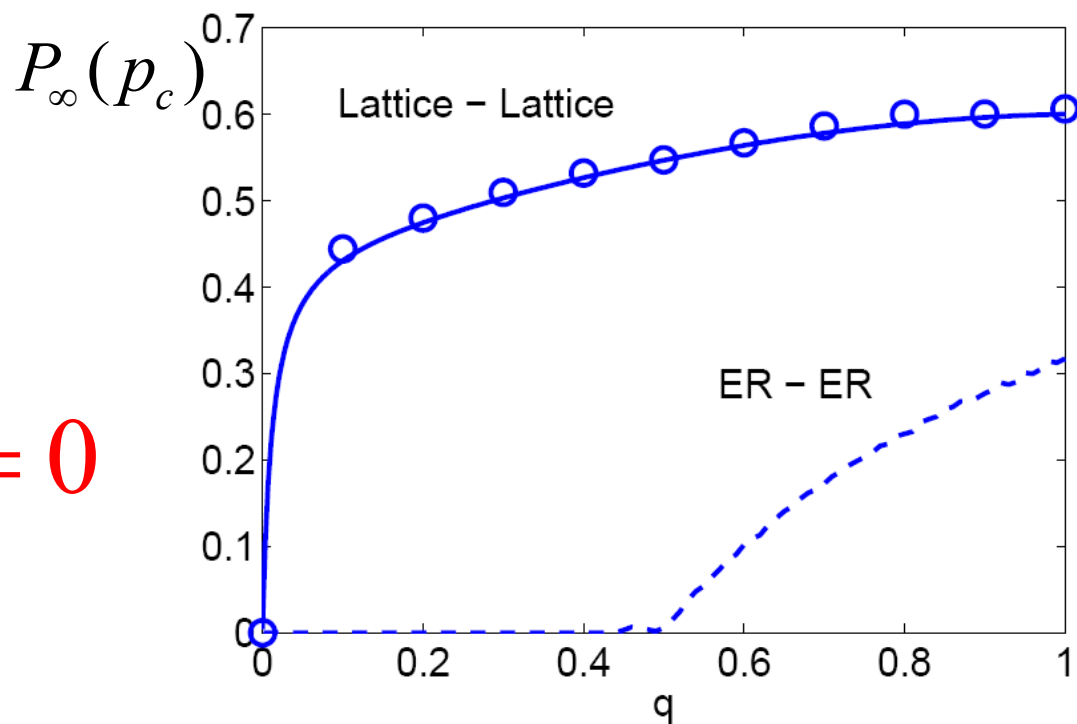
$$1 = p_c q_c P'_\infty(p_c)$$

$$P_\infty \sim (p - p_c)^\beta$$

$$\beta = 5/36 < 1 \text{ for } d=2$$

$$\text{For ER and } d=6, \beta=1$$

$$q_c = 0$$



Bashan et al

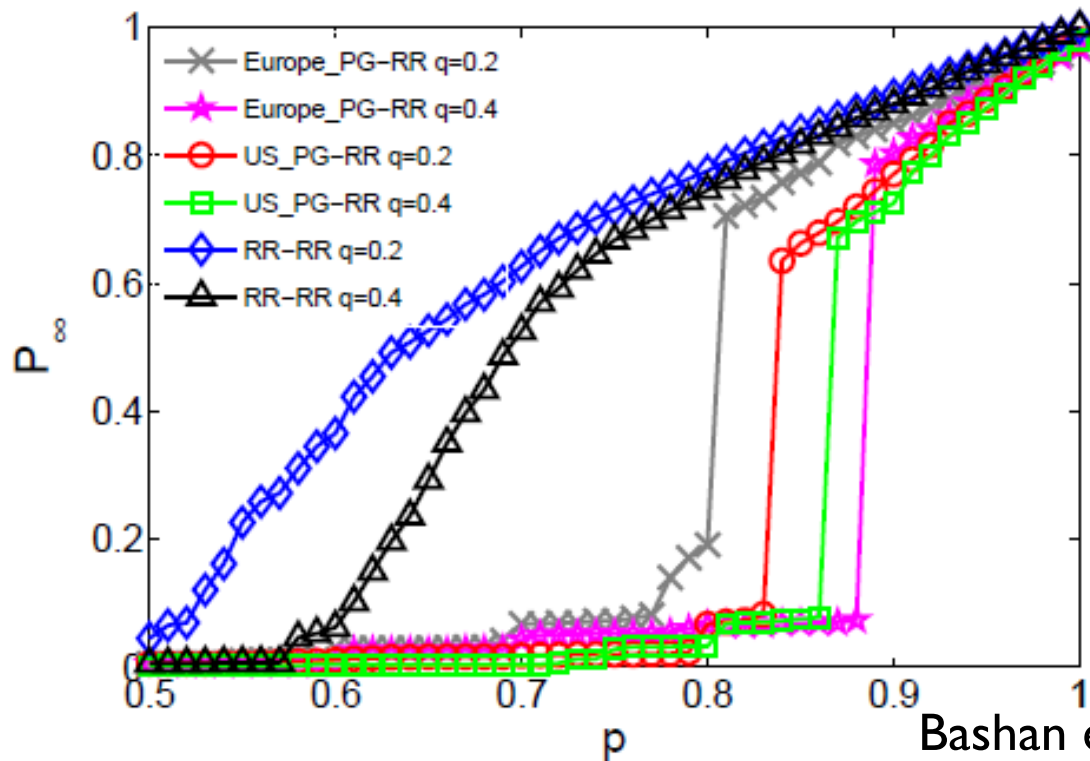
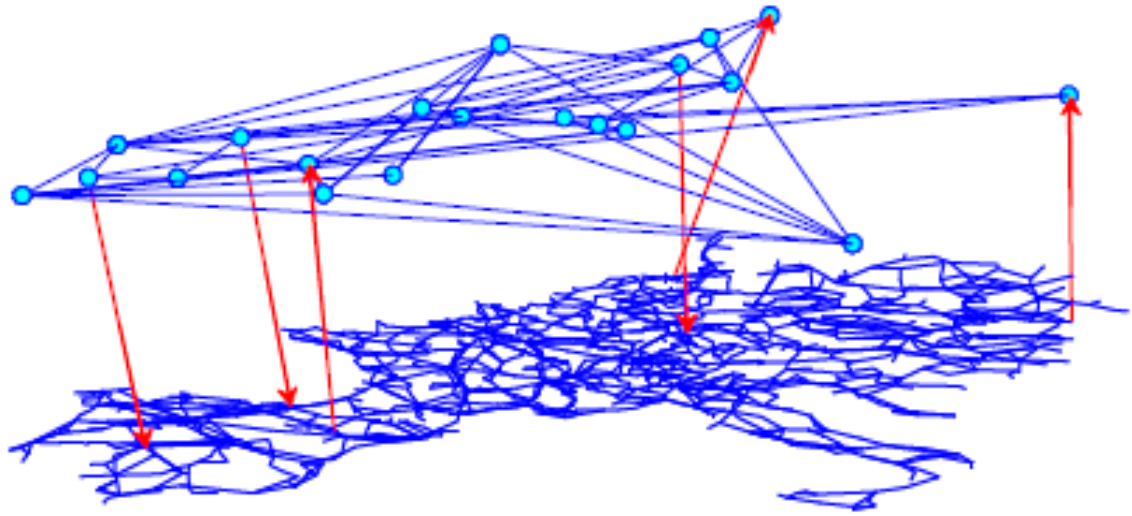
<http://arxiv.org/abs/1206.2062>

Nature Physics, (2013)

Message: our world is extremely unsafe!-no safe zone!

Experimental test on real spatial embedded coupled networks

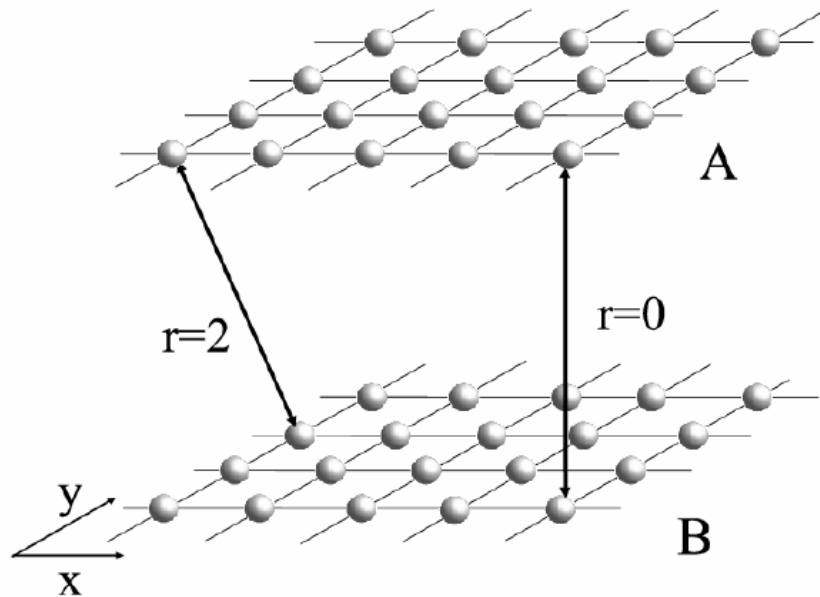
Interdependent European
Communication Network and
Power Grid



Results for European and US
Interdependent
Communication Networks and
Power Grids

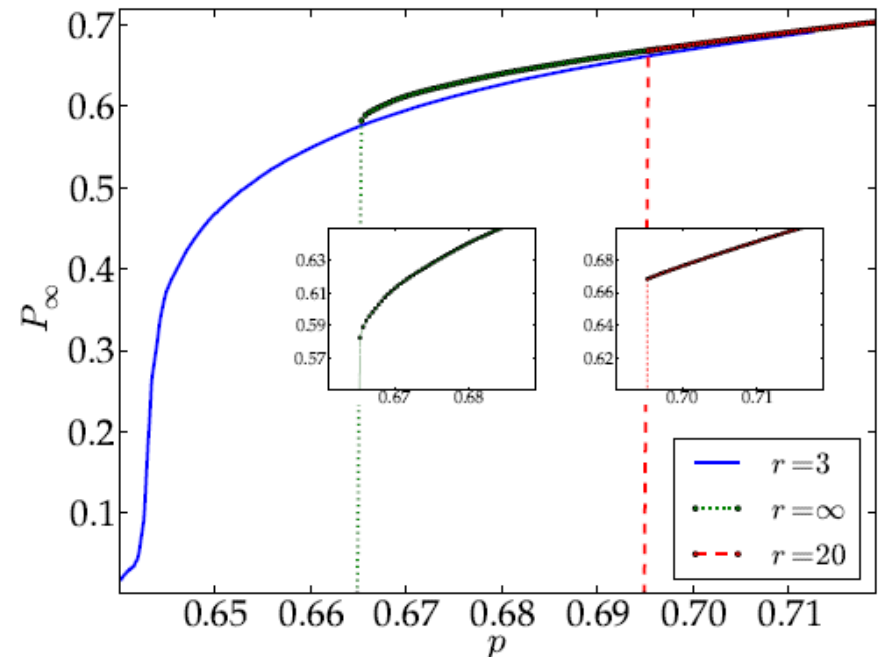
Bashan et al, Nature Physics (2013)

Interdependent Spatially Embedded Networks



Many networks are spatially embedded:
Internet, Power grid, Transportation etc

When connectivity links are limited
in their length---same universality
class as lattices!

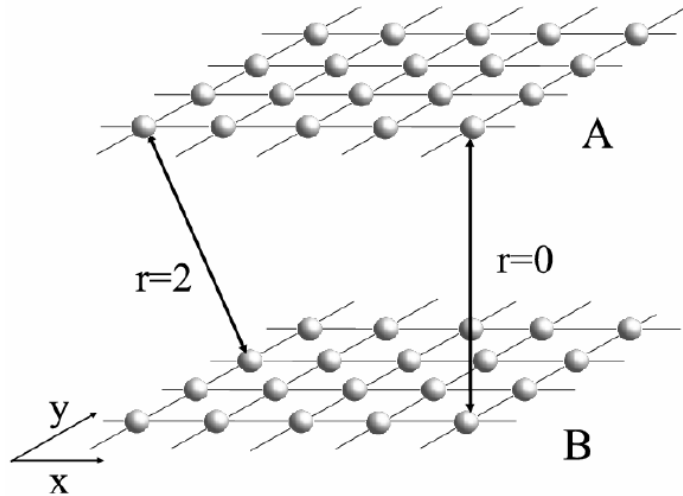


THREE DIFFERENT BEHAVIORS
DEPENDING ON r

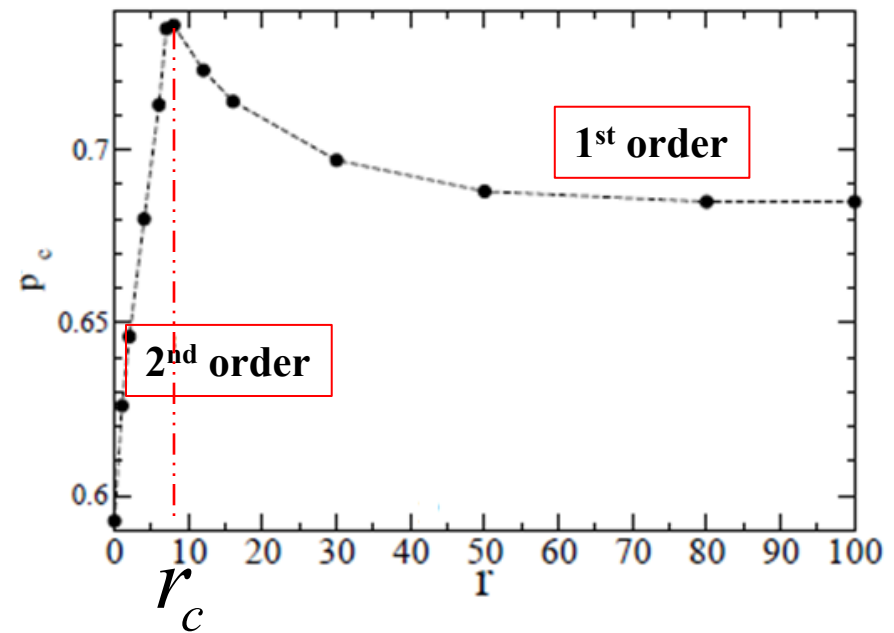
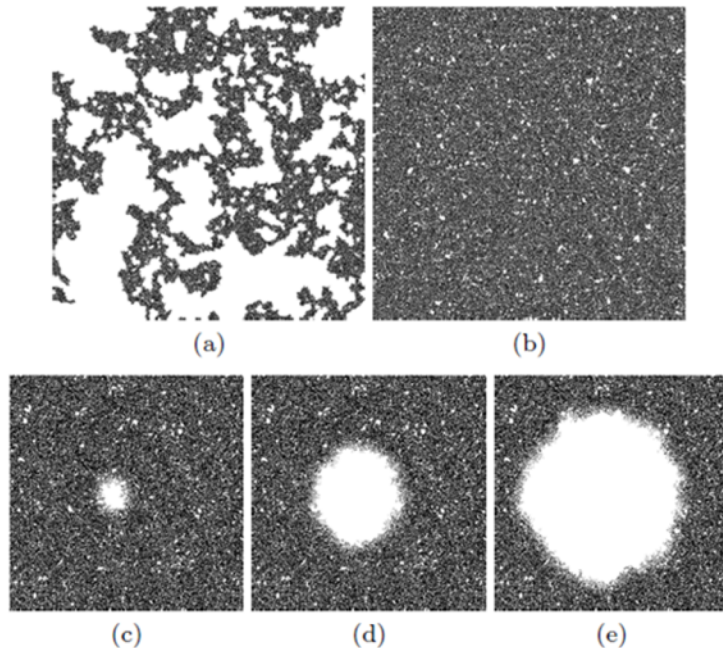
Wei et al, PRL, 108, 228702 (2012)

Bashan et al, Nature Physics (2013)

Interdependent Spatially Embedded Networks



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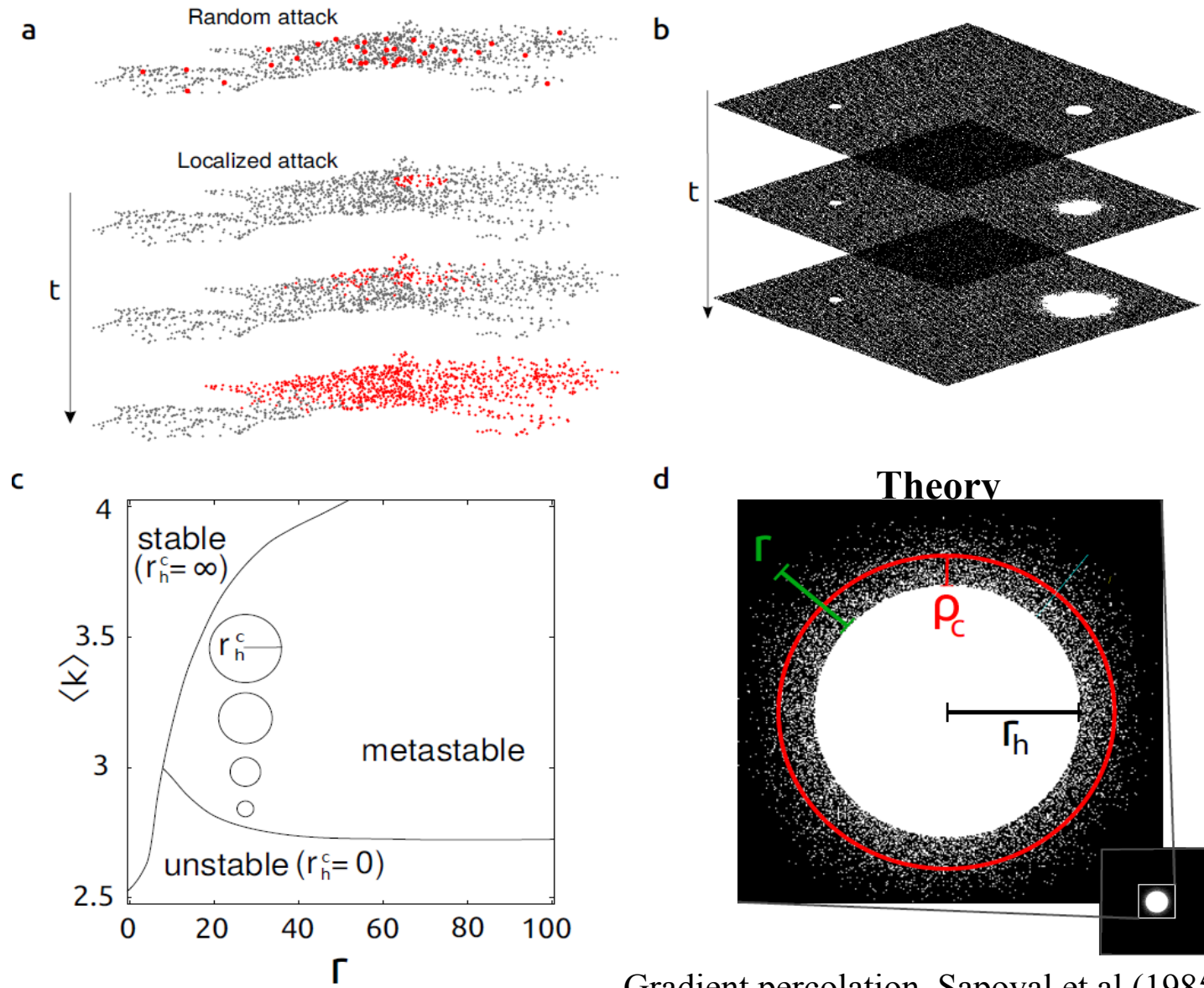
Wei et al, PRL, 108, 228702 (2012)

Bashan et al, <http://arxiv.org/abs/1206.2062>

New percolation-localized attacks

Localized attacks on spatially embedded systems with dependencies: critical size attack

Y. Berezin et al, .
arXiv:1310.0996



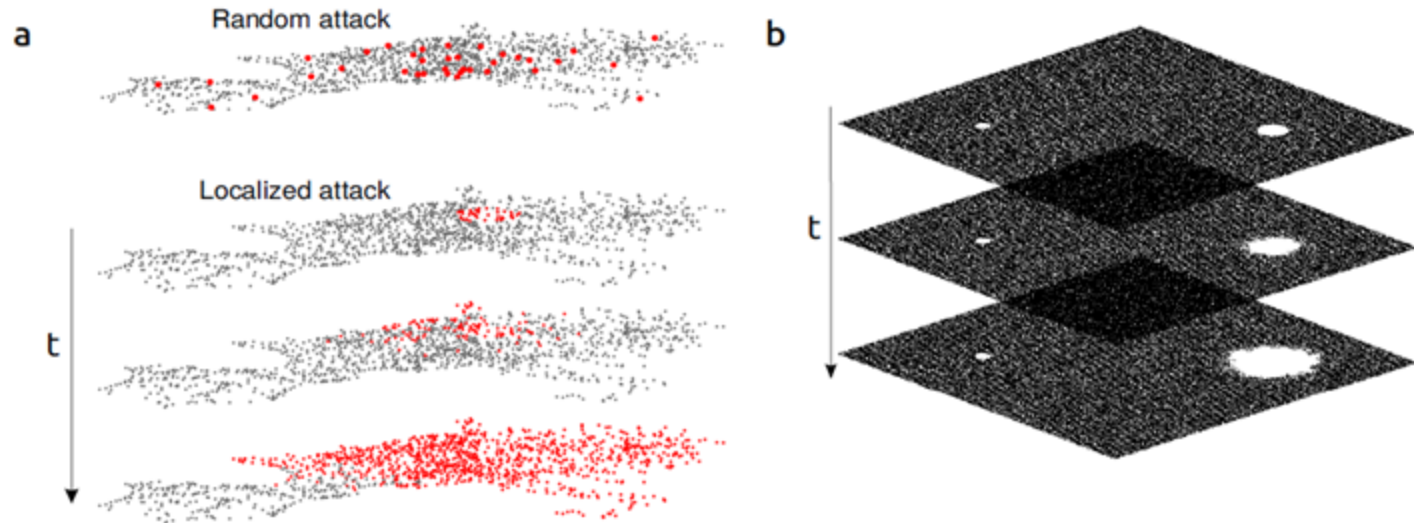
Gradient percolation, Sapoval et al (1985)

New percolation-localized attacks

Localized attacks on spatially embedded systems with dependencies: critical size attack

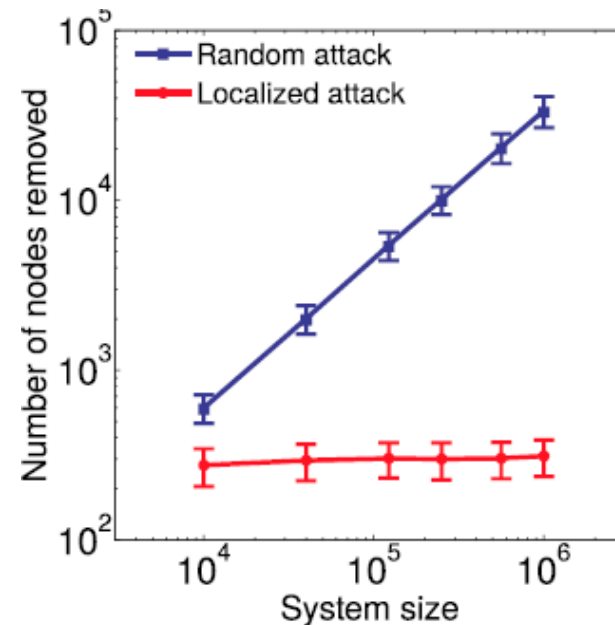
Y. Berezin et al, .
Scientific Reports
(2015)

Europe-power grid



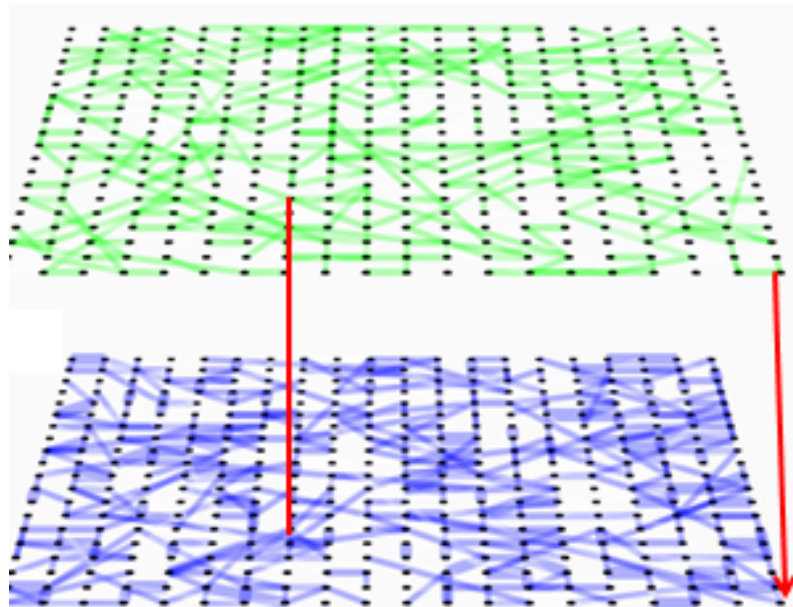
**FINITE SIZE FAILURE
CATASTROPHIC COLLAPSE**

$$p_c = 1$$

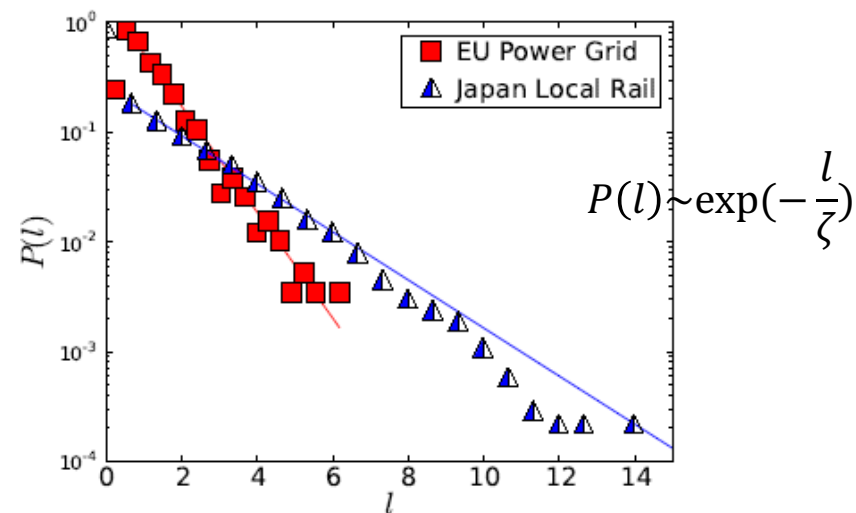
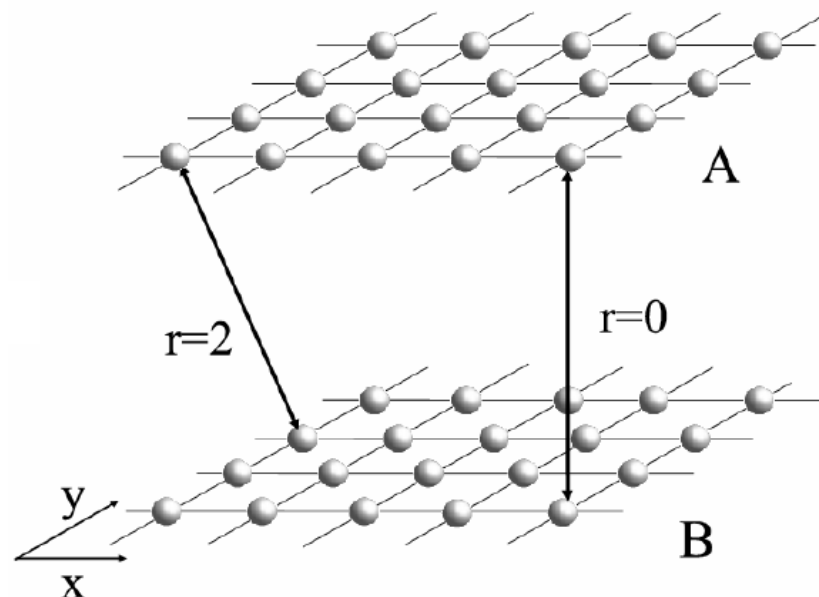


Interdependent Spatially Embedded Networks – Two Models

Connectivity Length (Multiplex)

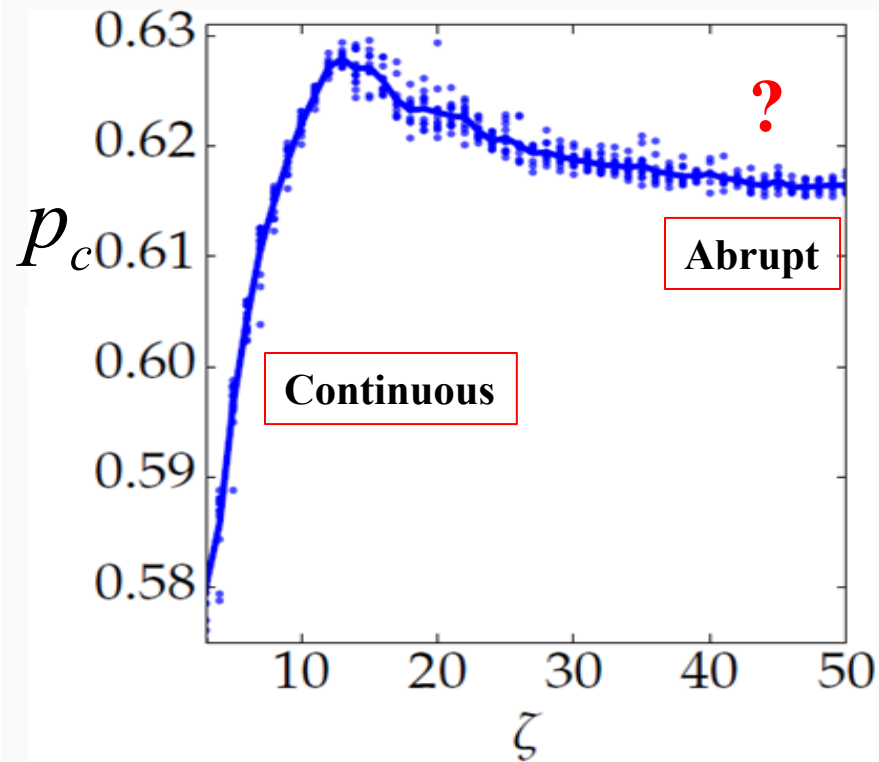


Dependency Length

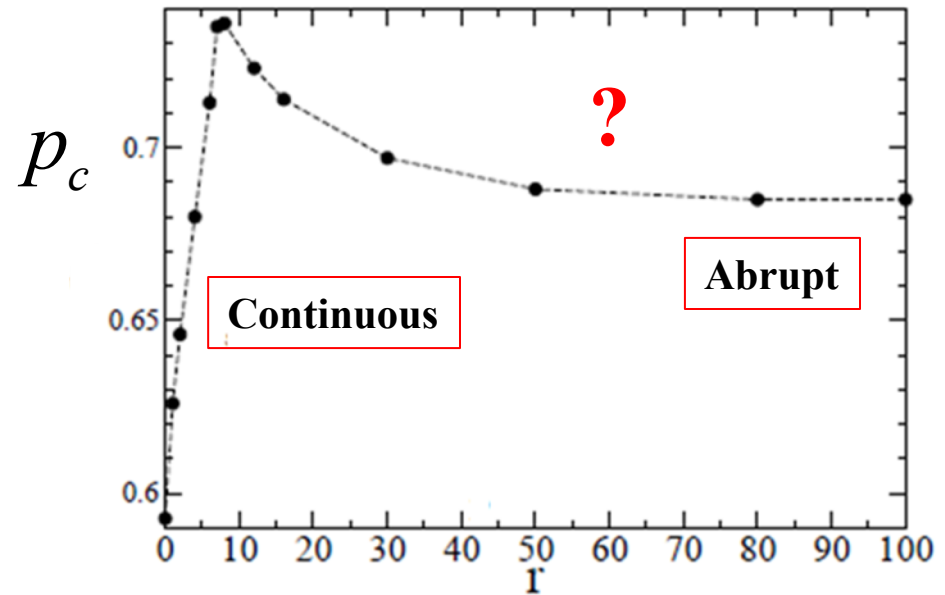


RANDOM FAILURES-TWO MODELS

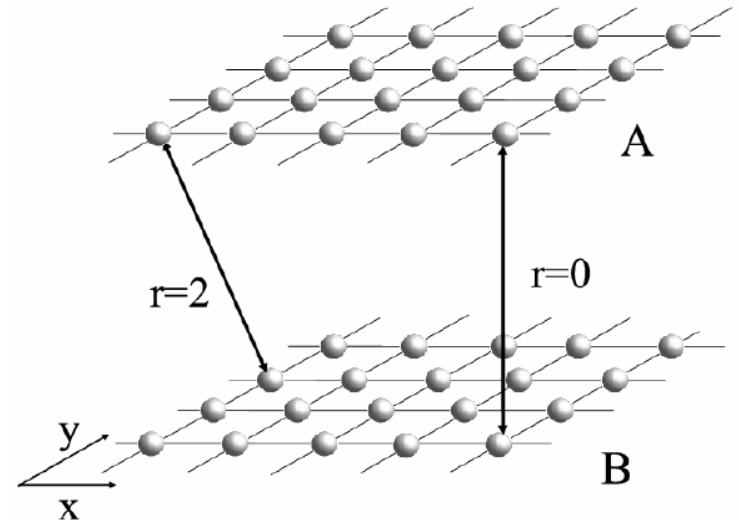
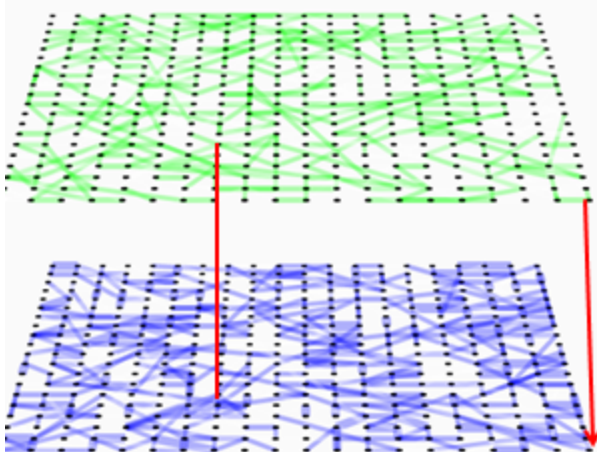
Connectivity Length



Dependency Length

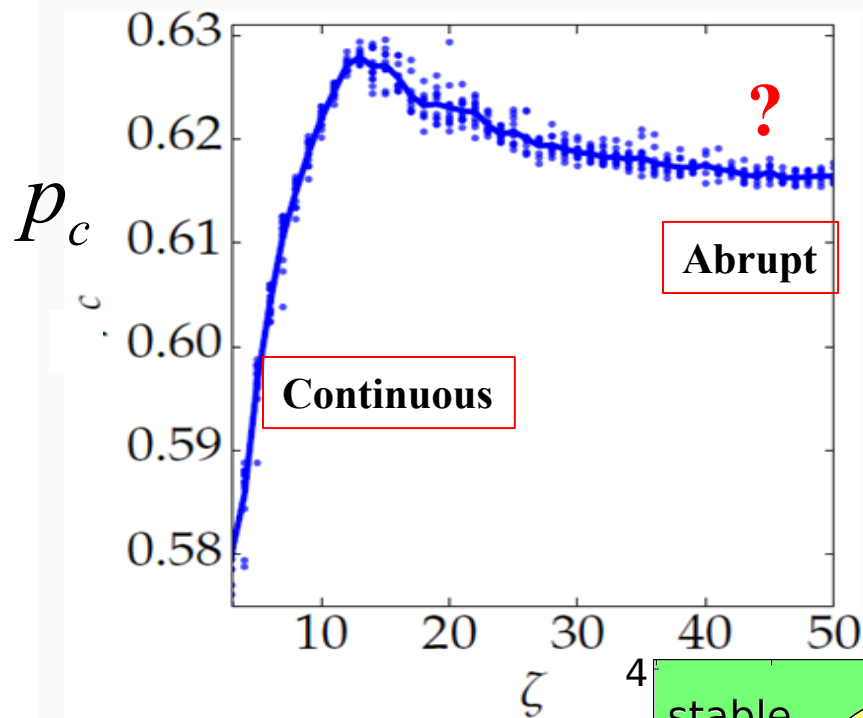


Multiplex
Danziger et al
EPL, 2016
Vaknin et al,
NJP, 2017

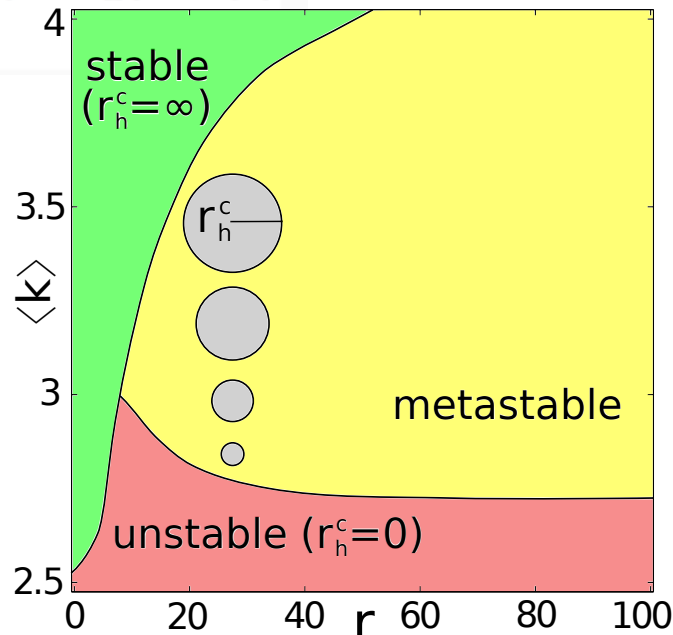
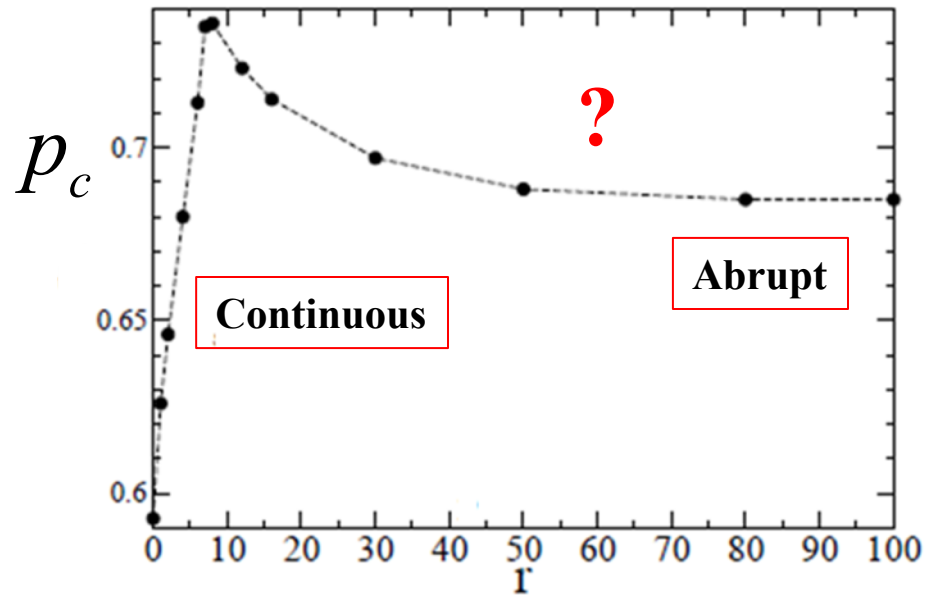


RANDOM FAILURES-Localized attacks

Connectivity Length

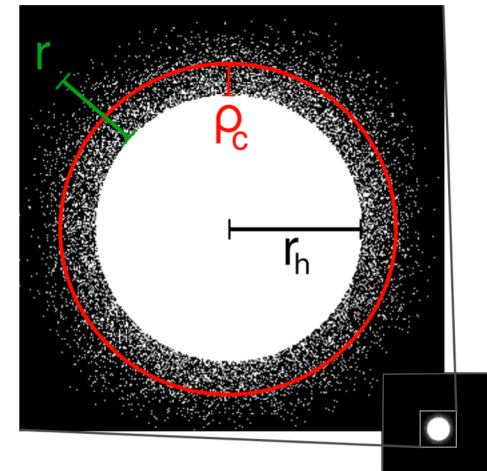
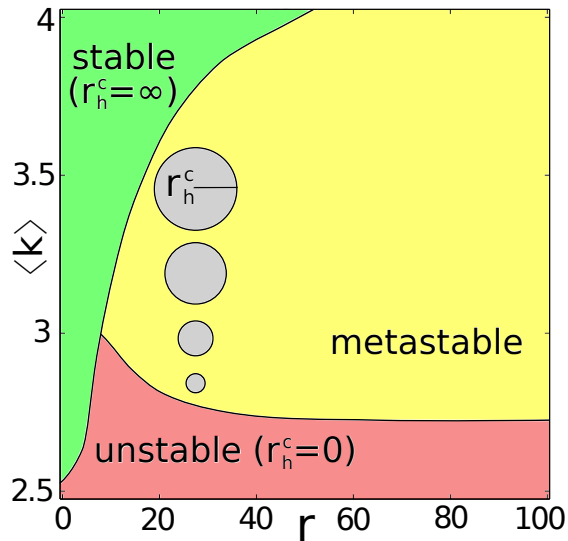
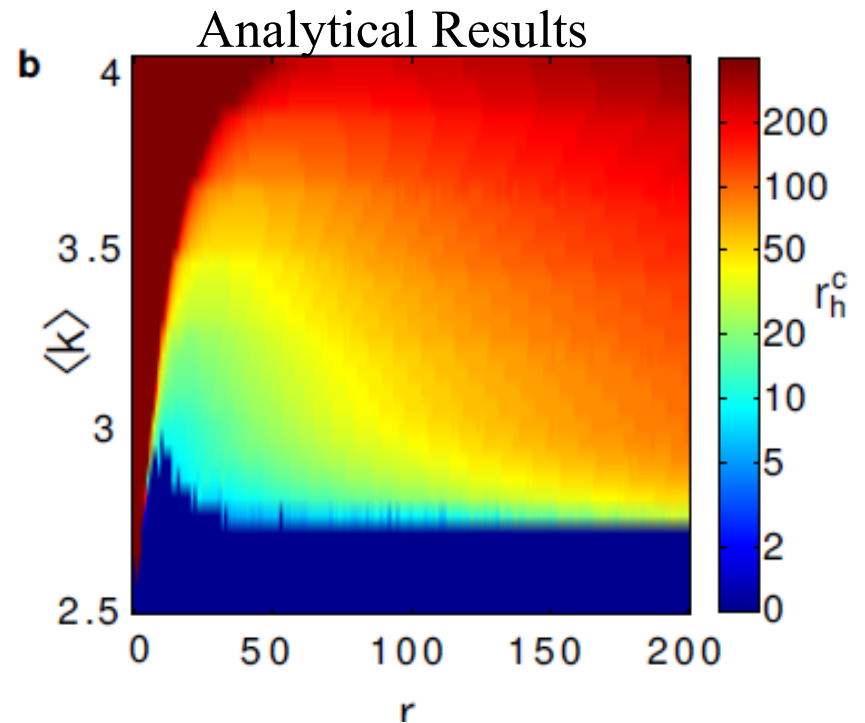
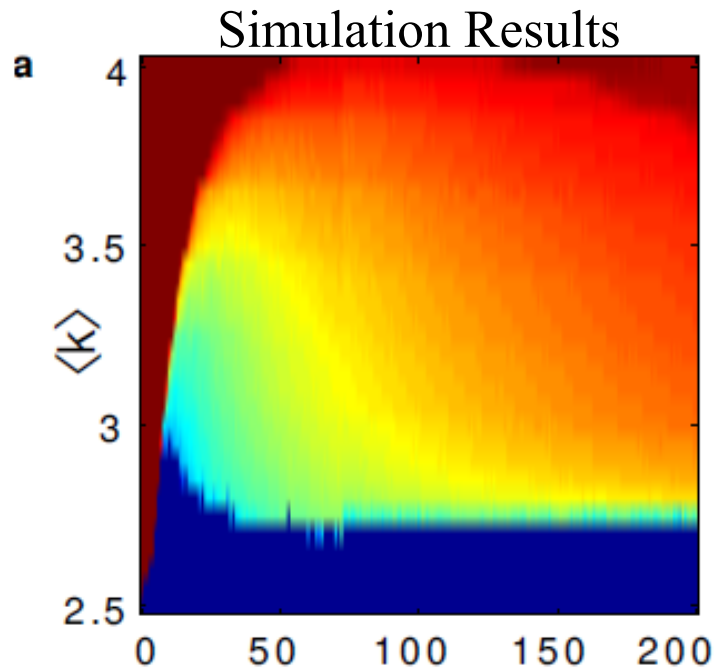


Dependency Length

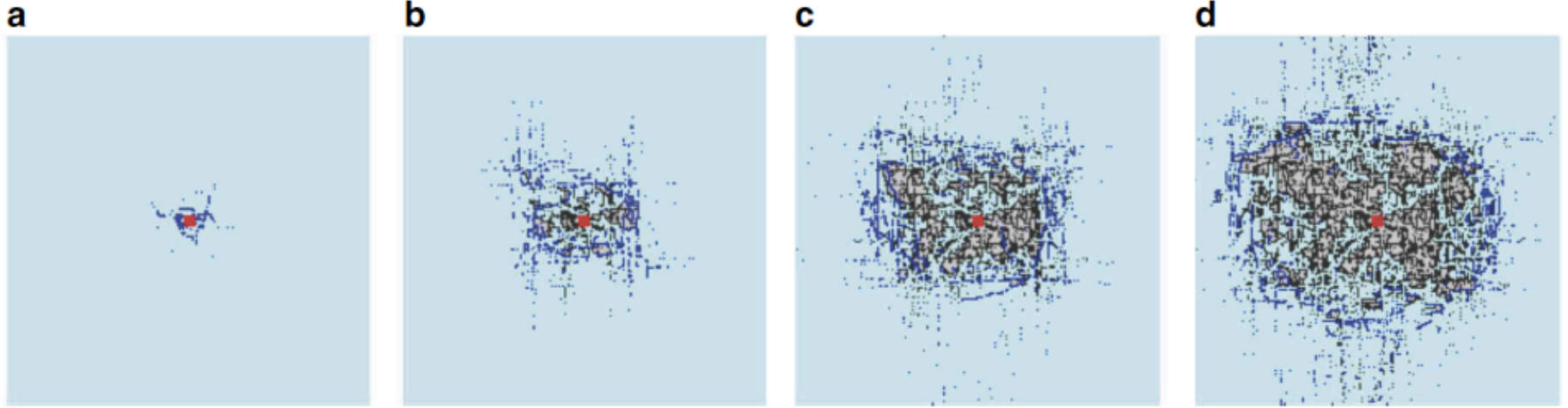


Danziger et al EPL (2016)
Dana Vaknin et al
(NJP, 2017)

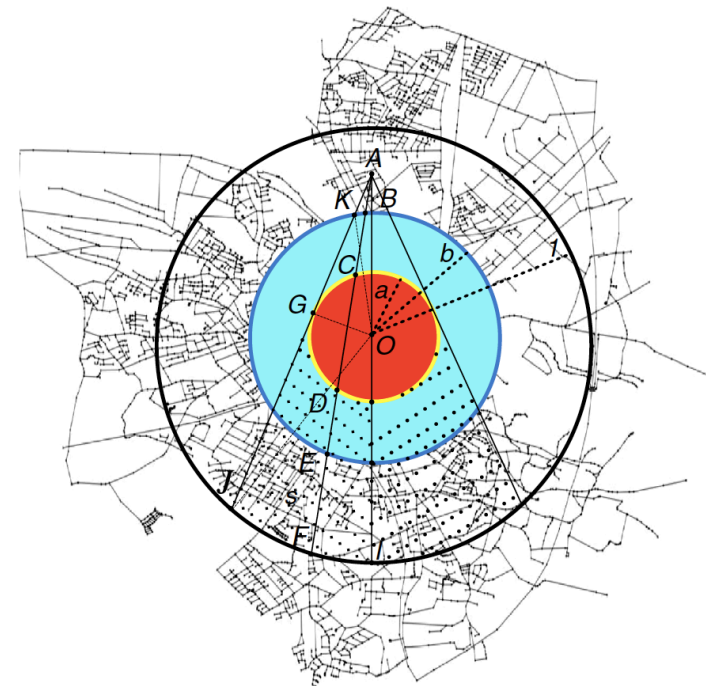
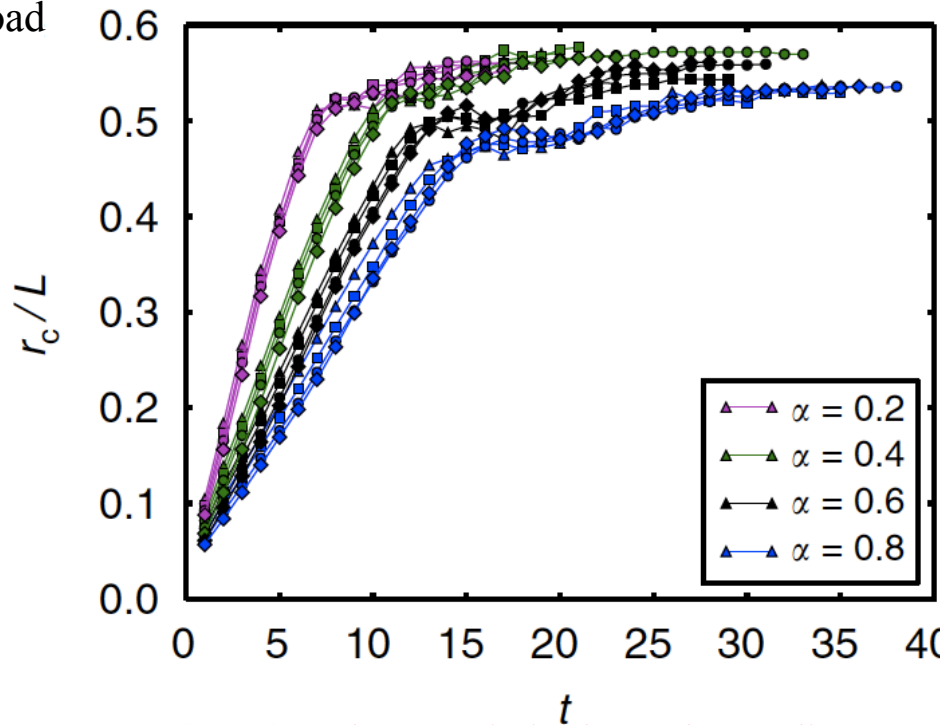
New percolation-localized attacks



Cascading of Overload Failures-Localized Attack



Motter Overload Model



Zhao et al

Nature Comm.7,10094 (2016)—characteristic dependency distance

Summary and Conclusions

- Statistical physics approach for **robustness of Networks** and of **interdependent networks—cascading failures**.
- New paradigm: **abrupt collapse** compared to **continuous** in single network
- Generalization to “**Network of Networks**”: n interdependent networks—**60y of graph theory and percolation is only the limited case, $n=1$!**
- Spontaneous **failure and recovery of system of systems-optimal repairing**
- **Localized attacks-finite size failure- zero fraction; $p_c=1$ -- full collapse!!**

Buldyrev et al., NATURE (2010)
Parshani et al., PRL (2010)
Gao et al, PRL (2011)
Parshani et al, PNAS (2011)
Wei et al, PRL (2012)
Gao et al., Nature Phys. (2012)
Bashan et al, Nature Phys. (2013)
Daqing Li et al, PNAS (2015)
Majdamzic et al Nat. Phys. (2014); Nature Comm. (2016)
Danziger et al, EPL (2016)
Xin Yuan, Yanqing Hu et al, PNAS (2017)

